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To cite this version:
Anne Davaille, Phillippe Carrez, Patrick Cordier. Fat plumes may reflect the complex rheology of the lower mantle. Geophysical Research Letters, American Geophysical Union, 2018, 45 (3), pp.1349-1354. 10.1002/2017GL076575. hal-02621562

HAL Id: hal-02621562
https://hal.inrae.fr/hal-02621562
Submitted on 26 May 2020

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Fat Plumes May Reflect the Complex Rheology of the Lower Mantle

A. Davaille, Ph. Carrez, and P. Cordier

1. Introduction

Mantle plumes are one of the modes of convection through which the Earth is cooling. As the Earth’s mantle is at least partially heated from below, regions of hot and therefore less dense material can become unstable and rise (e.g., Schubert et al., 2001). Hot spot volcanism (Wilson, 1963) will result from the impact under the lithosphere of these hot instabilities (Morgan, 1971). In a homogeneous and Newtonian fluid, they take the shape of a mushroom (Figure 1), with a big head over a narrower stem (Griffiths & Campbell, 1990; Morgan, 1971; Sleep, 1990). On the Earth’s surface, the hot head would produce traps while the stem would generate long volcanic tracks (Richards et al., 1989). Mantle plumes are therefore explaining first-order observations on a number of hot spots, as well as bringing up to us valuable information on the Earth’s deep interior.

Seismically, these hot plumes should correspond to slow seismic velocity anomalies. Surface wave tomographic models have identified broad (~1,000 km) ponds of slow material down to 200 km depth beneath many hot spots (e.g., Debayle et al., 2005; Ritsma & Allen, 2003; Shapiro & Ritzwoller, 2002) as predicted by models of plume-lithosphere interactions (e.g., Olson, 1990; Ribe & Christensen, 1999; Sleep, 1990). Regional tomographic studies imaged low-velocity anomalies down to the transition zone beneath Afar (Debayle et al., 2001), Kenya (Chang & Van der Lee, 2011), Iceland (Rickers et al., 2013; Shen et al., 2002), the Eifel (Goese et al., 1999), Yellowstone (Schmandt et al., 2012), West Antarctica (Hansen et al., 2014), Galapagos (Villagomez et al., 2007), and Hawaii (Wolf et al., 2009, 2011). Studies using receiver functions show thinner transition zones beneath Cape Verde, Azores, Iceland, Society, Galapagos, and Hawaii, which may reflect the presence of a hot conduit (see Ballmer et al., 2015, for references). In the deeper mantle, short wavelength and slow anomalies are difficult to image because of wavefront healing effects (Nolet & Dahlen, 2000), the uneven distribution of earthquakes, and the lack of dense seismic networks, especially in the oceans. Therefore, the 100 to 200 km thick conduit predicted for the classical plume would not be resolved (French & Romanowicz, 2015; Nolet et al., 2006), and indeed, global tomography models could not detect continuous hot structures under hot spots for years. However, progress in tomography techniques has recently imaged continuous slow structures from the core-mantle boundary to the surface beneath about 10 hot spots (French & Romanowicz, 2015; Montelli et al., 2006; Zhao, 2001). Resolution analysis shows that most plumes would not be visible if their diameter was smaller than about 600 km (French & Romanowicz, 2015; Montelli et al., 2006). Indeed, the imaged plumes in finite frequency models PRI-S05 and PRI-P05 (Montelli et al., 2006) present diameters of at least 600–800 km. And waveform tomography model SEMUCB-WM1 (French & Romanowicz, 2015) recovers columnar structures with diameters 800 to 1,000 km (Figure 2). So hot plumes appear quite wide in the lower mantle, which is at odds with the common view of a hot plume morphology as a balloon head on a thin conduit.

Abstract Recent tomographic imaging of the mantle below major hot spots shows slow seismic velocities extending down to the core-mantle boundary, confirming the existence of mantle plumes. However, these plumes are much thicker than previously thought. Using new laboratory experiments and scaling laws, we show that thermal plumes developing in a visco-plastic fluid present much larger diameters than plumes developing in a Newtonian fluid. Such a rheology requiring a yield stress is consistent with a lower mantle predominantly deforming by pure dislocation climb. Yield stress values between 1 and 10 MPa, implying dislocation densities between 10⁸ and 10¹⁰ m⁻², would be sufficient to reproduce the plumes morphology observed in tomographic images.

Key Points:
• Plumes developing in a visco-plastic fluid present much larger diameters than plumes developing in a Newtonian fluid.
• Such a rheology requiring a yield stress is consistent with a lower mantle predominantly deforming by pure dislocation climb.
• This deformation mechanism could explain the morphology of plumes in the lower mantle recently imaged by seismic tomography.

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In a Newtonian homogeneous fluid, such a thick morphology would correspond either to a hot plume developing at much lower Rayleigh number than present-day mantle convection (Goes et al., 2004) or to a more viscous hot instability intruding in a less viscous mantle (Whitehead & Luther, 1975). It was pointed out that if diffusion creep was the main deformation mode in the lower mantle, the resulting strong increase of the viscosity with the crystal size, and the enhanced crystal growth rate with temperature, could produce hot plumes that are more viscous than the ambient mantle (e.g., Korenaga, 2005; Solomatov, 1996).

Another way to produce fat plume conduits in Newtonian fluids is to introduce compositional heterogeneities (Dannberg & Sobolev, 2015; Davaille et al., 2005; Kumagai et al., 2008; Lin & van Keken, 2006). Then the plume conduit can thicken due to thermo-compositional recirculation within the conduit itself (Kumagai et al., 2008).

We show here using recent laboratory experiments (Davaille et al., 2013; Massmeyer et al., 2013) that there is yet another avenue: thick hot thermal plumes could be produced in the lower mantle if the latter had a viscoplastic rheology, where flow occurs only when the deviatoric stress becomes greater than a critical yield stress. As described in the following, such type of rheology could correspond to the one recently proposed for bridgmanite in the lower mantle by numerical modeling (Boioli et al., 2017). Section 2 presents the laboratory findings, while section 3 describes the occurrence of yield stresses in high-temperature creep mechanisms in the lower mantle. Section 4 discusses the implications for mantle plumes.

**2. Fat Plumes in a Yield Stress Fluid**

We recently studied experimentally the development of thermal plumes out of a localized heat source on the bottom of a tank filled with a Carbopol dispersion. The details of the studies can be found in Davaille et al. (2013) and in Massmeyer et al. (2013). A Carbopol dispersion is a polymeric fluid whose rheology can be described by a Herschel-Bulkley (hereafter “HB”) law (e.g., Di Giuseppe et al., 2015; Piau, 2007). When the stress $\sigma$ exceeds a critical value $\sigma_0$, called yield stress, shear thinning occurs with

$$\sigma = \sigma_0 + K_v \dot{\gamma}^{n_{HB}}$$

(1)
where $\dot{\gamma}$ is the shear rate, $K_v$ is the consistency, and $n_{HB}$ is an exponent between 0.3 and 0.75. So when motions occur, an effective viscosity can be defined for the fluid

$$\eta = \sigma / \dot{\gamma} = \sigma_0 \dot{\gamma}^{-1} + K_v \dot{\gamma}^{n_{HB}-1} \quad (2)$$

Note that the last member of this equation is similar to a dislocation creep where the shear thinning exponent would be $n = 1/n_{HB}$. When local stresses are smaller than $\sigma_0$, the HB model assumes that deformation is zero (e.g., Piau, 2007). In a real material, this is not true, and thermo-elastic stresses have to be considered (e.g., Sgreva & Davaille, 2017).

To describe the system dynamics, the key parameter is the “yield parameter” $Y_0$, which compares the thermally induced stress to the yield stress. Three different regimes are observed. For low $Y_0$, no convection develops and deformation is purely elastic. For intermediate $Y_0$ values, the thermo-elastic stresses generated by heating are big enough to overcome the yield stress: a convection cell appears but remains confined around the heater. For high $Y_0$, the stresses generated by the thermal buoyancy of the hot pocket around the heater become much larger than the yield stress and a thermal plume develops (Figure 1). Its morphology differs from the mushroom shape typically encountered in Newtonian fluids. Combined temperature and velocity field measurements show that a plug flow develops within the plume thermal anomaly and that deformation is strongly localized on its edges. This produces a rising finger shape (Figure 1). Scaling analysis (Davaille et al., 2013; Massmeyer et al., 2013) shows that plume uplift occurs when

$$Y_0 = \frac{gD\Delta \rho}{\sigma_0} > Y_c = 15 \pm 3.6 \quad (3)$$

where $D$ is the plume diameter, the density difference between the plume and the ambient fluid is $\Delta \rho = \alpha \rho \Delta T_{av}$, $\alpha$ is thermal expansion, and $\Delta T_{av}$ is the averaged temperature excess of the plume compared to the ambient fluid. Fat plumes were observed in the laboratory up to $Y_0 \sim 10Y_c$.

3. On Yield Stresses During High-Temperature Creep in the Mantle

The existence (or not) of a yield stress depends on the microstructure of the fluid and the way motion is activated. Our Carbopol solutions are polymeric gels constituted of elastic micron-scale sponges that aggregate and jam. So the yield stress comes from the fact that the microstructure at first resists deformation (Oppong, 2011; Piau, 2007).

In mantle rocks, the yield stress or elastic limit of a crystal is not an intrinsic characteristic, but depends on its defects microstructure. Moreover, the development of a given microstructure is a direct consequence of the mechanism involved during the creep regime. Two processes are commonly considered to account for flow in the mantle: diffusion creep and dislocation creep.

In diffusion creep, strain results directly from the motion of crystal point defects. Since the vacancy concentration close to a grain boundary under tension is greater than that close to a grain boundary under compression, a net flux of matter develops from sources to sinks. At high temperatures, vacancies can diffuse through the bulk of the grain (the Nabarro-Herring creep mechanism) or along the grain boundaries (Coble mechanism). The efficiency of both mechanism is limited by the grain size, which conditions the characteristic distance between sources and sinks (Poirier, 1985). Even before diffusion creep was actually observed experimentally, Nabarro and Herring proposed theoretically a constitutive equation for this process: the main characteristic of diffusion creep is that it is Newtonian viscous ($\sigma \sim \dot{\gamma}$) and grain size dependent. Hence, there would be no yield stress associated with Nabarro-Herring creep.

In dislocation creep, strain is produced by the glide of a fraction of the dislocations that are made free to move owing to two thermally activated recovery mechanisms: cross slip whereby screw dislocations deviate from their initial glide plane, and climb where nonscrew dislocations move out of the glide planes after absorbing
Figure 4. Yield stress allowing the development of fat plumes in the lower mantle as a function of plume temperature anomaly and radius. The dark box outlines the mantle fat plumes domain.

point defects (Poirier, 1985). Frank proposed that dislocations distributed at random among several slip systems form a three-dimensional network that has a characteristic dimension that scales like \( l \approx \rho_d^{-1/2} \), where \( \rho_d \) is the dislocation density (see, for instance, Friedel, 1964). The yield stress can be related to the stress necessary to create new dislocations by activating dislocation sources from dislocations segments of the Frank network. Also, any mobile dislocation will have to overcome the long range elastic stresses produced by the network or the short-range interactions due to crossing with the dislocations of the Frank network. All these mechanisms define a critical stress that scales with

\[
\sigma_y \propto \frac{Gb}{\beta l} = \frac{1}{\rho_d} \frac{G b}{\beta} \rho_d^{1/2}
\]

where \( G \) is the shear modulus, \( b \) the modulus of the Burgers vector, and \( \beta \) is a numerical constant of the order of 1–5 depending on the nature of the interactions (Friedel, 1964). Hence, the yield stress comes from the jammed nature of the population of dislocations. Figure 3 shows how the threshold stress increases as a function of the dislocation density.

In the meantime, we can use the scaling law (equation (3)) to estimate the yield stress (Figure 4) required to generate fat plumes in the mantle as imaged by the recent global tomographic models (Figure 2; French & Romanowicz, 2015; Montelli et al., 2006). Figure 4 shows that yield stresses values between 1 and 10 MPa would allow plumes with diameters ranging from 600 to 1,000 km and averaged temperature anomalies of 50 to 800 °C to develop. According to equation (4) and Figure 3, such yield stress estimates would imply dislocation densities between \( 10^8 \) and \( 10^{10} \) m\(^{-2}\).

4. Discussion and Conclusions

In the previous section, we showed that the dislocation creep mechanism in a crystal always implies the existence of a yield stress scaling on the dislocation density of the crystal. Recent numerical simulations have shown that under pressure and temperature conditions of the lower mantle, dislocation glide is extremely difficult in bridgmanite (Kraych et al., 2016), even under mantle strain rates. Standard dislocation creep involving glide and climb can thus no longer be considered. However, Boioli et al. (2017) have demonstrated that dislocation climb can provide an alternative deformation mechanism. Plastic strain is then produced by dislocation climb induced by emission and absorption of vacancies. The dislocations inside the grains thus play the role of sources and sinks for vacancy diffusion. By introducing a characteristic distance for diffusion smaller than the grain size, pure climb creep is grain size independent, and it is more efficient than the standard Nabarro-Herring (or Coble) creep features (Boioli et al., 2017). It is also worth noticing that even in case of pure climb creep, dislocation multiplication will only occur for stresses higher than the yield stress \( \sigma_y \). Boioli et al. (2017) further showed that dislocation densities between \( 10^8 \) and \( 10^{10} \) m\(^{-2}\) (i.e., section 3) are sufficient to produce deformation at strain rates that correspond to our best estimates of those in the lower mantle \( (10^{-14} – 10^{-16} \text{s}^{-1}) \).

Moreover, since pure climb creep involves no lattice rotation, it does not produce crystal lattice preferred orientation. This could explain why seismic anisotropy has not been detected in most of the lower mantle. The weak anisotropy reported below 2,000 km depths (e.g., De Witt & Trampert, 2015; Montagner & Kennett, 1996) and the strong azimuthal anisotropy observed in the D” layer at the bottom of the mantle (e.g., De Witt & Trampert, 2015; Montagner & Kennett, 1996; Panning & Romanowicz, 2004) would then be due to different minerals (post-perovskite and magnesiowustite) or to the alignment of materials with differing elastic properties through shape-preferred orientation.

The existence of a critical yield stress in the rheology would also have important implications for mantle stirring and mixing. As already seen in section 2, such a rheology strongly localizes motions and shear, while “dead zones” develop in the remaining fluid. Their existence might strongly impede mantle stirring efficiency, leading to the long-term preservation of primitive material. More work is in progress to study this problem quantitatively.
Nevertheless, we demonstrate here that microstructural parameters such as dislocation microstructures at the submillimeter scale can have implications on large-scale processes and features. Unfortunately, compared to other deformations modes, very few studies (especially involving microstructural characterization) have been devoted to materials deforming by pure climb creep (the study of Beauchesne & Poirier, 1990 on KNbO₃ perovskite is one of those). Hence, our knowledge on how dislocation microstructures develop during pure climb creep, and how they respond to loading conditions is too limited. It seems important to carry on such studies in the future to better constrain the rheology of bridgmanite and therefore the rheology of the lower mantle.

**Acknowledgments**

The laboratory experiments have been supported by French ANR PTECTO and CNRS/INSU/CNES Programme de Planetologie. The numerical simulations of the mantle creep have been supported by funding from the Seventh Framework Programme (FP7), ERC grant 290424 - Rheoman. The data used are listed in the references. We thank the Editor and an anonymous reviewer for their comments on the manuscript.

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