

How Computers Break (Serious) Puzzles with logic and (a different breed of) learning

Thomas Schiex

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How Computers Break (Serious) Puzzles

with logic and (a different breed of) learning

Thomas Schiex



February 2018 Académie des sciences, Paris, France

Superhuman performances of AI





Human beings

- Easily rely on quick "intuitions" (ill-defined problems)
- Extreme rigor is painful and slow (logic/arithmetic)

Als (computers)

- Accessible to some "intuition" (problems defined by data)
- Fast and extreme rigor is the default (1 billion op./sec)



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It was expected that machines would show superhuman "logical reasoning" performances

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1955: Newell & Simon "Logic Theorist" proved 38 of the 52 theorems in the *Principia Mathematica* (Russel and Whitehead), and even corrected a proof in it.

NP-hard problems

- Some problems seems intrisically hard (for Als at least)
- Worst case asymptotic exponential time (P \neq NP)





NP-hard problems



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- Worst case asymptotic exponential time (P \neq NP)

$\mathit{n}^2 imes \mathit{n}^2$ Sudoku

- NP-complete, 9×9 : 10^{80} cases
- 10^{51} ages of the universe to examine them all
- Fast brute force will fail

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- NP-complete, 9×9 : 10^{80} cases
- 10^{51} ages of the universe to examine them all
- Fast brute force will fail
- Can be solved in milliseconds

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Logic

• We have a set of variables

From a well defined problem to a solution

(Sudoku cells contain a number from 1 to 9)







Logic

From a well defined problem to a solution

- We have a set of variables
- We have a set of properties on these variables

(Sudoku cells contain a number from $1 \mbox{ to } 9)$

(all different rows, columns, super-cells)







Logic

From a well defined problem to a solution

We have a set of variables

(Sudoku cells contain a number from 1 to 9)

- We have a set of properties on these variables (all different rows, columns, super-cells)
- We want to find an input that satisfies all properties (or prove none exists: refutation).



Intuition



Intuition (DL)

From examples to a classifier

- We have a set of digital inputs (in \mathbb{B}^n) and output (class: one bit).
- We want a function that best predicts seen (and unseen) data in most cases.



Intuition



Intuition (DL)

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Technological progress

- Increasingly complex useful objects
- That must be highly reliable (lives at stake)
- We cannot fully get them under control anymore

Increasing system complexity

- Hardware: Pentium FDIV bug (1994, 3.1 million transistors)
- Software: the Therac-25 (radiation-therapy) kills 6 patients
- Tesla cars: said to carry 100 millions lines of codes
- Convolutional NN: may have billions of parameters

planes, computers, software, cars, Als











• Cell (i, j) and (i, j') must be different





More sophisticated/practical function description

- propositions over theories
- non Boolean variables
- numerical output

SAT Modulo Theory9

Constraint Satisfaction, Constraint Programming³⁰

Weighted MaxSAT²⁵/CSP,⁵ Graphical models¹⁸

SAT is the simplest



SAT Modulo Theory⁹

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Weighted MaxSAT²⁵/CSP,⁵ Graphical models¹⁸





NP-complete: can express all NP-complete problems

- the logical puzzles you like (Sudoku, Nonograms...)
- or not (configuration, scheduling, test pattern generation...)
- robot planning
- digital circuit verification (Bounded Model Checking)
- or software verification (FOL, grounding, abstraction)



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NP-complete, so intractable

Standard argument for less realistic problem reformulation, heuristics or stochastic search





NP-complete, so intractable

Standard argument for less realistic problem reformulation, heuristics or stochastic search

Real SAT instances with millions of variables/clauses can be solved (with a proof)

IBM Bounded Model Checking SAT instance (SATLIB)



p cnf 51639 368352 -1 7 0 -1 6 0-150-1 -4 0-1 3 0 -1 2 0-1 -8 0 -9 15 0 -9 14 0 -9 13 0 -9 -12 0 -9 11 0 -9 10 0 -9 -16 0

51, 639 variables, 368, 352 constraints $\neg x_1 \lor x_7$ $\neg x_1 \lor x_6$... 10 Pages later

•••



```
185 -9 0

185 -1 0

177 169 161 153 145 137 129

121 113 105 97 89 81 73 65 57

49 41 33 25 17 9 1 -185 0

186 -187 0

186 -188 0
```

 $(x_{177} \lor x_{169} \lor x_{161} \lor x_{153} \lor \cdots \lor x_{177} \lor x_9 \lor x_1 \lor \neg x_{185})$



```
10236 - 10050 0
10236 - 10051 0
10236 - 10235 0
10008 10009 10010 10011 10012 10013 10014 10015 10016 10017 10018
10019 10020 10021 10022 10023 10024 10025 10026 10027 10028 10029
10030 10031 10032 10033 10034 10035 10036 10037 10086 10087 10088
10089 10090 10091 10092 10093 10094 10095 10096 10097 10098 10099
10100 10101 10102 10103 10104 10105 10106 10107 10108 -55 -54 53 -52
-51 50 10047 10048 10049 10050 10051 10235 -10236 0
10237 - 10008 0
10237 - 10009 0
10237 - 10010 0
```



```
-7 260 0
7 - 260 0
1072 1070 0
-15 -14 -13 -12 -11 -10 0
-15 -14 -13 -12 -11 10 0
-15 -14 -13 -12 11 -10 0
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-7 -6 -5 -4 -3 -2 0
-7 -6 -5 -4 -3 2 0
-7 -6 -5 -4 3 -2 0
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185 0
```

Finally 15,000 Pages later



```
-7 260 0
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-15 -14 -13 -12 -11 10 0
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185 0
```

Search space	
$2^{50,000} \approx 3.1$	$10^{15,051}$

Finally 15,000 Pages later



```
-7 260 0
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1072 1070 0
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Search	space	
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Solved in one second

Finally 15,000 Pages later



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-7 260 0
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Search	space		
$2^{50,000}$	≈ 3.1	$10^{15,051}$	

Solved in one second

How does it work?









• A clause is shortened by one litteral



- A clause is shortened by one litteral
- This may create new unit clauses (propagation)



- A clause is shortened by one litteral
- This may create new unit clauses (propagation)
- If the empty clause □ appears: no solution
Logic: Try to guess and reconsider (DPLL⁷)





SAT state-of-the-art in 1990 Hundreds of variables Thousands of clauses

Logic: Learn from failure



Long line of research in "symbolic" Artificial Intelligence^{3,10,23,24,32}

- Trace back failure to guesses through propagation^a
- Do backward resolution from conflict
- Add a new implied clause to the set of clauses

^aRichard M Stallman and Gerald J Sussman. "Forward reasoning and dependency-directed backtracking in a system for computer-aided circuit analysis". In: Artificial intelligence 9.2 (1977), pp. 135–196.

- Forces to reconsider an earlier guess
- Prevents refailing for a related reason

(safe generalization)

Learns a more effective formulation of the problem as it solves it

Intuition: Choose a variable and try to guess its value



Learning by "Activity based heuristics"26

- On-line estimation of how often a variable is involved in recent clauses/failures
- Try guessing this variable first

Learns weak spots in the problem as it is solved

(safe)

Human intuition based on...

A lot of free data and free code...

- International competitions (> 50,000 benchmarks with many real problems)
- Open source solvers (autocatalytic)





Human intuition based on...

A lot of free data and free code ...

- International competitions (> 50,000 benchmarks with many real problems)
- Open source solvers (autocatalytic)

Strong French presence	MADE IN FRANCE
Award winning solvers	(Glucose, ² toulbar2 ¹⁵)
 Constraint programming solver/startup 	(Choco)
 Strong presence in international conferences 	(# of accepted papers in CP ⁴)







A conjecture in	a combinatorics	∞
When one spli	is $\mathbb N$ in 2 , one part must contain a Pythagorean triple	$(a^2 = b^2 + c^2)$



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When one splits ${\mathbb N}$ in 2 , one part must contain a Pythagorean triple	$(a^2 = b^2 + c^2)$

No known proof, puzzled mathematicians for decades (one offered a 100 \$ reward)



A conjecture in combinatorics	∞
When one splits $\mathbb N$ in 2, one part must contain a Pythagorea	an triple $(a^2 = b^2 + c^2)$

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SAT solver proof^{14,22}

200TB proof, compressed to 86GB (stronger proof system)^a

^aOliver Kullmann. "The Science of Brute Force". In: Communications of the ACM (2017).

A finitized Gödelian flavor

(K. Gödel, 1931) MA

Whether it's maths or not...

Size matters!

- Not only there exists true unprovable statements (in powerful enough consistent sets of axioms¹²)
- There may be true provable statements we will never be able to prove because of their extremely long proofs²⁰



Is it bio-compatible?



Biology

- Many discrete object ($\{A, T/U, G, C\}$, amino acids, genes, alleles, enzymes...)
- Lots of experimental data

Is it bio-compatible?



Biology

- Many discrete object ($\{A, T/U, G, C\}$, amino acids, genes, alleles, enzymes...)
- Lots of experimental data

Exploiting Data + knowledge: Machine Learning

- (Stochastic) models can be built from knowledge and data
- And used to predict a "Most Likely/Optimal State"

 \Rightarrow easily NP-hard

Is it bio-compatible?



Biology

- Many discrete object ($\{A, T/U, G, C\}$, amino acids, genes, alleles, enzymes...)
- Lots of experimental data



Proteins



Most active molecules of life Sequence of "amino-acids", each chosen among a set of 20 natural ones



Transporter, binder, regulator, motor, catalyst... Hemoglobine, TAL effector, ATPase, dehydrogenases...



Most active molecules of life Sequence of "amino-acids", each chosen among a set of $20\ {\rm natural}$ ones



Transporter, binder, regulator, motor, catalyst... Hemoglobine, TAL effector, ATPase, dehydrogenases...

Why is it worth designing new proteins



Eco-friendly chemical/structural nano-agents

- New catalysts for biomass transformation (biofuels, food and feed, cosmetics...),
- New drugs for medicine
- New components for nanotechnologies

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 20^n sequences!

intractable for experimental techniques

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20^n sequences!

intractable for experimental techniques

CPD: From bits to atoms

From information to functional matter

- mind blowing mass 3d printing-like capacities at atomic level (bacterias)
- structural and functional purposes (powerful origami)
- produced new folds,¹⁹ catalysts,³¹ nano-components³⁶



Protein Design as the inverse of folding

Ingredients

- Full atom model of a protein backbone
- $\bullet\,$ Catalog of all 20 amino acids in different conformations
- Full atom energy function
- Maximum stability \equiv Minimum energy



NP-hard²⁸

(assumed to be rigid)







Large input (> 1GB)

Toulbar2 is able to ...

- provide a proven minimum energy solution
- exhaustively enumerate sequences close to it
- in spaces of size $> 10^{200}$



Showed that an highly tuned biased Monte Carlo increasingly fails to find the optimal sequence^a

NP-hard problem

^{*a*}David Simoncini et al. "Guaranteed Discrete Energy Optimization on Large Protein Design Problems". In: *Journal of Chemical Theory and Computation* 11.12 (2015), pp. 5980–5989. DOI: 10.1021/acs.jctc.5b00594.

Unbounded error





Asymptote: Size matters!

Asymptotic convergence can be arbitrarily slow...



C8 pseudo-symetric 20VP symmetrized into a nano-component





8 fold

C8 pseudo-symetric 20VP symmetrized into a nano-component

• Tako: (R)evolution + Rosetta/talaris14

















Asymptotes: size matters

NP is not exactly as we tend to think

- Als have made drastic progress in their logical capacities
- This progress also comes from (gradient-free) learning
- More progress is needed to supplement our limited human capacities

Synergies between Logic and Intuition

- Logic can analyze and exploit learnt models
- Intuition can help logic without tainting it

(not only Neural Nets)

(guidance)

Thanks



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Protein Design

A. Voet (KU Leuven) D. Simoncini (INSA, Toulouse) S. Barbe (INSA, Toulouse) S. Traoré (PhD, CEA) C. Viricel (PhD) RosettaCommons (U. Washington) W. Sheffler (U. Washington) PyRosetta (U. John Hopkins) B. Donald (U. North Carolina) K. Roberts (U. North Carolina) T. Simonson (Polytechnique) J. Cortes (LAAS/CNRS)

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We do not understand the sources of their efficiency

CDCL solvers have an expected polynomial $O(n^k)$ runtime on SAT instances whose primal (Gaifman) graph has treewidth k.

Without ever trying to compute a treewidth/decomposition (NP hard).



Go on a $n \times n$ goban is PSPACE-hard

- PSPACE-hard to decide if there is a winning strategy
- $\bullet~$ AlphaGo 0 does not solve $19\times19~{\rm Go}$
- It plays better than humans (and that's amazing!)





Results of the SAT competition/race winners on the SAT 2009 application benchmarks, 20mn timeout







Additional ingredients (patented for some)

- (I) stops, restarts with a better understanding of the problem¹³
- (I) forgets learnt information predicted as "useless" (Glue clauses²)
- Lazy data structures²⁶
- Absolutely reliable combination of logic and intuition
- but we don't really understand why it can be so efficient^{1,16}


Neural nets and safety critical settings

It doesn't seem too hard to fool a standard Convolutional Neural Net^a

^aChristian Szegedy et al. "Intriguing properties of neural networks". In: arXiv preprint arXiv:1312.6199 (2013).





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From deep Neural Nets to SAT



Binarized Deep NN: ± 1 activations/weights⁶

- Lin: affine transformation with learnt binary weights (float bias).
- Bn: (Batch normalization) rescaling with learnt floats.
- Bin: binarization using the Sign function.



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A learnt block can be described as a SAT^a formula

(SMT(LI)¹⁷ for ReLU)

"Nina Narodytska et al. "Verifying properties of binarized deep neural networks". In: arXiv preprint arXiv:1709.06662 (2017).



Adversarial Robustness of a classifier

A positive test input cannot be slightly modified to change class



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A positive test input cannot be slightly modified to change class

Certified robusteness by SAT

As a SAT formula: Neural Net + input + bounded perturbation + missclassification



Adversarial Robustness of a classifier

A positive test input cannot be slightly modified to change class

Certified robusteness by SAT

As a SAT formula: Neural Net + input + bounded perturbation + missclassification

- MNIST dataset, 4 blocks BNN with 100 to 200 neurons per layer, L_∞ norm
- Millions of clauses: Glucose² certifies (non) robustness for most input in <5' CPU time



Deciphering genomic DNA



Segmenting genomic DNA





Segmenting genomic DNA





Deciphering genomic DNA with EuGene

(Semi-CRF)²¹

- Derived from an actual human processor (S. Rumbauts, PhD)^a
- Discriminative learning (don't try to model evidence!)

Optimization + decomposable probability distribution

• Optimizes an empirical loss function (performance on a testing set: quality is crucial)

^{*a*}S Foissac et al. "Genome Annotation in Plants and Fungi: EuGène as a Model Platform". In: *Current Bioinformatics* 3.2 (2008), pp. 87–97.



...

Prediction is in P Main difficulty: collecting evidence, training and testing.

