



# Coordination problems and the control of epidemics affecting fruit trees

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# Coordination problems and the control of epidemics affecting fruit trees

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# A complex management problem

- production by private owners distributed within a landscape
- economic losses due to the infection outbreak
- diffusion of pathogens intra and inter-patch
- finite horizon, multi-year production
- treatment by (partially inefficient) detection and removal of infected trees, (discrete binary choice)



Figure: Sharka example

# Objective: Understand the decentralized problem

Problem often studied under the centralized perspective.

**Our objective:** understand better the decentralized behavior.

Emerging literature: [Atallah et al., 2017], [Fenichel et al., 2014], [Costello et al., 2017]

We analyze classical questions...

**coordination issues, inefficiency characterization...**

with specific modeling constraints

# Modeling: infection diffusion within a period

Management options:  $\rho_i \in \{0, \rho_{max}\}$ ;  $0 < \rho_{max} < 1$

State variables:

$I_i$  Quantity of infected in patch  $i$ .

$S_i$  Quantity of uninfected trees.

Growth and diffusion of the infection:  $r_{ij}$

**Evolutionary law** (discrete time model), with  $I \ll S$ :

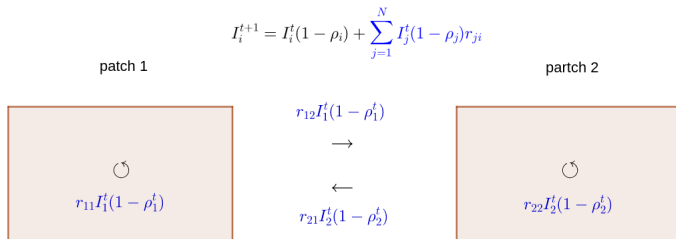
$$(I_i^{t+1}, S_i^{t+1}) = f(S^t, I^t, \rho^t)$$

$$I_i^{t+1} = I_i^t(1 - \rho_i) + \sum_{j=1}^N I_j^t(1 - \rho_j)r_{ji}$$

$$S_i^{t+1} = S_i^t - \sum_{j=1}^N I_j^t(1 - \rho_j)r_{ji}$$

# Modeling: Infection diffusion, two patches model

## Diffusion in a two patches model



# Economic model: profit function

$$\pi_i^t(I^t, S^t, \rho^t) = \left( S_i^{t+1} v_i + I_i^{t+1} u_i - \frac{\rho_i^t}{\rho_{max}} (c_a + c_h A_i) \right)$$

subject to:

$$(I^{t+1}, S^{t+1}) = f(S^t, I^t, \rho^t).$$

$v_i$  production value by an uninfected tree in patch  $i$

$u_i$  production value by an infected tree  $i$

$c_a$  access cost

$c_h$  per  $\text{ha}^{-1}$  inspection cost

$A_i$  patch  $i$  surface

Resolution for the closed loop feedback-Nash equilibrium concept.  
Comparison with the Pareto optimum.



# Results

## Impact of the initial condition in the 2 patches 2 steps model:

- An example of analytical result: zone where  $(\rho_{max}, \rho_{max}, \rho_{max}, \rho_{max})$  is the unique FNE
- Multiplicity of FNE
- Characterization of inefficiency

# Maximal effort as a FNE

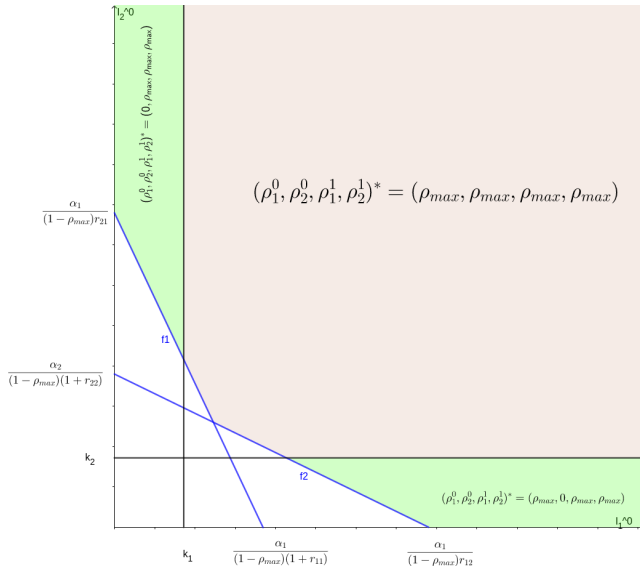
**Proposition:** Within the initial condition state space, there is a zone where initial infection is sufficiently high so that both players do maximal effort:

$(\rho_{max}, \rho_{max}, \rho_{max}, \rho_{max})$  is the unique Nash equilibrium if and only if  $(I_1^0, I_2^0) \in \Delta_{max}$ , where  $\Delta_{max}$  is defined by the set of inequalities:

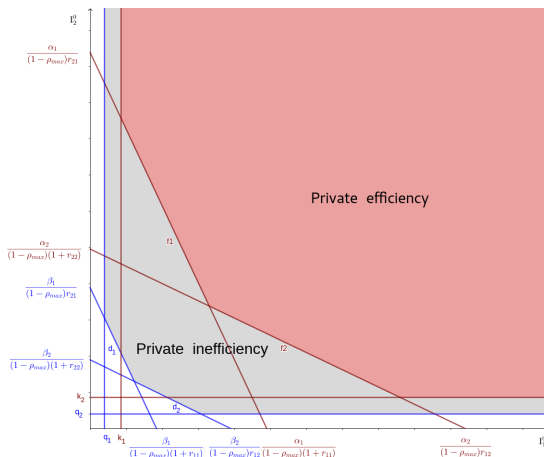
$$\begin{cases} I_2^0 > \frac{\alpha_1 - I_1^0(1 - \rho_{max})(1 + r_{11})}{(1 - \rho_{max})r_{21}} \\ I_2^0 > \frac{\alpha_2 - I_1^0(1 - \rho_{max})r_{12}}{(1 - \rho_{max})(1 + r_{22})} \\ I_2^0 > k_2 \\ I_1^0 > k_1 \end{cases}$$

where  $\alpha_i \equiv \frac{1}{F_i}(c_a + c_h \frac{1}{\rho_{max}} A_i)$  where  $F_i \equiv (v_i - u_i)r_{ii} - u_i$ , and  $k_1$  and  $k_2$  are some constants.

# Private efficiency in the case of maximal effort



# Illustration for $\rho_{max}$ as a unique Nash equilibrium

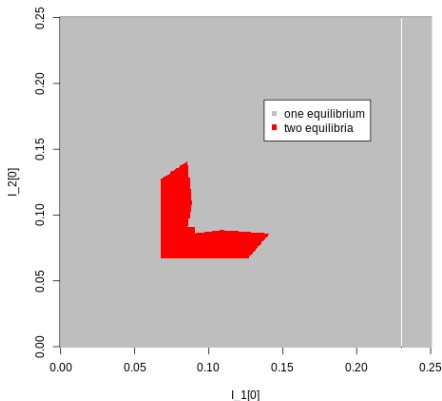


$$\beta_i \equiv \frac{1}{D_i} \left( c_a + c_h \frac{1}{\rho_{max}} A_i \right) \text{ where } D_i \equiv (v_i - u_i)r_{ii} + (v_j - u_j)r_{ij} - u_i$$

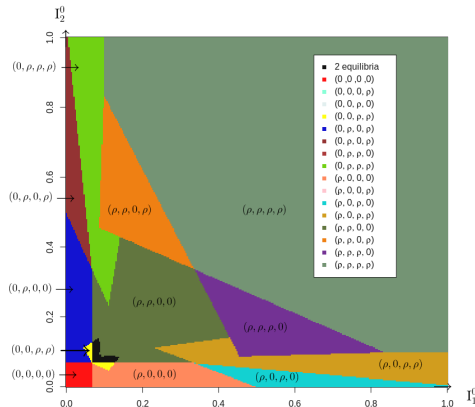
$$\alpha_i \equiv \frac{1}{F_i} \left( c_a + c_h \frac{1}{\rho_{max}} A_i \right) \text{ where } F_i \equiv (v_i - u_i)r_{ii} - u_i$$

# Number of Nash equilibria

**Proposition:** Multiplicity might arise... even in a symmetric case (proof using an example).



# Example, Nash equilibria according to the initial condition



# Symmetric example, inefficiency

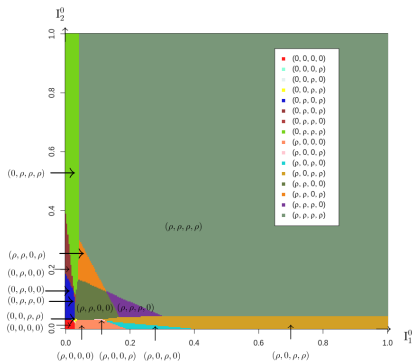


Figure: Pareto optimum, symmetric example

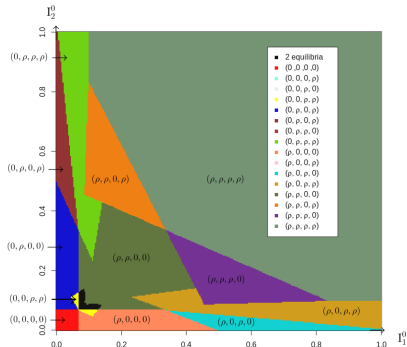
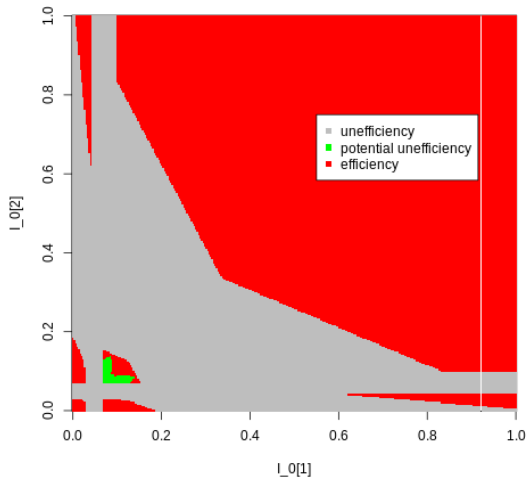


Figure: Nash equilibria, symmetric example

# Symmetric example, inefficiency





# Conclusion

## Main results

When infection is still small, ( $I \ll S$ ), and detection imperfect, and given parameters ( $T, R, U, V \dots$ )

- Nash feedback resolution of the game shows equilibria depending on the initial infection level
- Geometric characterization of efficiency and inefficiency zones as a function of the initial infectious state
- Coordination issues: multiplicity of equilibria for some  $(I_1^0, I_2^0)$

# Conclusion

## Perspectives

- Introduce asymmetry in the case study, look at the impact of other parameters
- Study de-synchronization of production cycles and longer time horizons
- Apply this framework to analyze real life problems (find some data); question large scale management programs using known parameters
- Work on the modeling:  $SI$  model, probabilistic framework...

Thanks for listening !



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Specification of spatial-dynamic externalities and implications for  
strategic behavior in disease control.  
*Land Economics*, 93(2):209–229.



Costello, C., Querou, N., and Tomini, A. (2017).  
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*European Economic Review*, 94:23–44.



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The control of invasive species on private property with  
neighbor-to-neighbor spillovers.  
*Environmental and Resource Economics*, 59(2):231–255.

# Temporal structure

