

Building GPCR signalisation networks. Example of the FSH receptor

Romain Yvinec

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Mathematics of system biology

Romain Yvinec

Systems Biology

Motivation

(Bio)chemical reaction network formalism

Practice!

Outline

Systems Biology

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(Bio)chemical reaction network formalism

Practice :

Systems Biology

- Describe the behaviors and functions of a system (cell, individual, ecosystem) by studying interactions between its constituents (molecules, tissue, individuals): holistic approach, complex system.
- "Systems biology...is about putting together rather than taking apart, integration rather than reduction. It requires that we develop ways of thinking about integration that are as rigorous as our reductionist programmes, but different....It means changing our philosophy, in the full sense of the term" (Denis Noble).

Systems Biology

- Describe the behaviors and functions of a system (cell, individual, ecosystem) by studying interactions between its constituents (molecules, tissue, individuals): holistic approach, complex system.
- "Systems biology...is about putting together rather than taking apart, integration rather than reduction. It requires that we develop ways of thinking about integration that are as rigorous as our reductionist programmes, but different....It means changing our philosophy, in the full sense of the term" (Denis Noble).
- Computer science and Mathematical modeling of complex system biology.
- Theory of dynamical systems applied to molecular biology.

Population dynamics

(Birth and death processes)

$$\emptyset \rightleftarrows A$$

Goal: Understand when a population goes to extinct, survive, invades...

Small networks

(Interaction between population, 'toy' molecular models)

Logistique model

$$\emptyset \to A$$
$$A+A \to \emptyset$$

Lotka-Volterra model

$$\begin{array}{ccc} \varnothing & \to & A \\ A+B & \to & 2B \\ B & \to & \varnothing \end{array}$$

Goal : gives simple description/explanation of yet complex behaviors (oscillation, multi-stability...)

Small networks

(Interaction between population, 'toy' molecular models)

Enzymatic kinetics

$$E + S \rightleftarrows ES \rightleftarrows E + P$$

Pharmacology model

$$R_{i} \rightleftharpoons R_{a}$$

$$A + R_{i} \rightleftharpoons AR_{i}$$

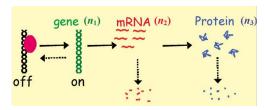
$$A + R_{a} \rightleftharpoons AR_{a}$$

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Goal: gives simple description/explanation of yet complex behaviors (oscillation, multi-stability...)

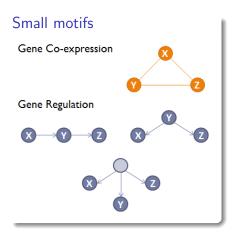
(Single) Gene Expression

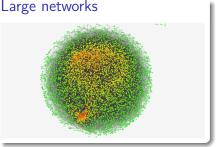
$$\begin{array}{ccc} G & \rightarrow & G+M \\ M & \rightarrow & M+P \\ M & \rightarrow & \varnothing \\ P & \rightarrow & \varnothing \\ G+P & \rightarrow & G_{off} \end{array}$$



Goal : Understand the variability of level of expression between cells

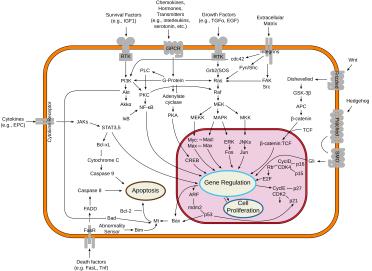
Co-expression genes network





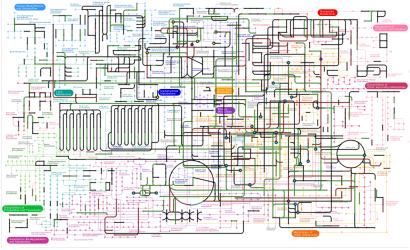
Goal : characterize network topology (and dynamics) associated to certain conditions, diseases, etc.)

Signaling system



Goal: Understand cell response to external stimuli (to control it)

Metabolomic Network



Goal : Understand regulations of key metabolites, explain toxicity or determine phenotype...

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(Bio)chemical reaction network formalism

Practice!

Possible applications of mathematical modelling

- Understand non-trivial behavior of a biological system (by reproducing this behavior with an understandable model)
- Help to identify intermediate molecules and/or give some evidence for direct interactions between molecules
- Quantify some non-observables quantities, in particular : molecules concentrations, reaction rates.

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Today : Compare quantitatively the effect of two Ligands on two signalling pathways : biais signalling

Outline

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Practice

Definition

A chemical reaction network is given by thee sets (S, C, R):

- Species, $S := \{S_1, \dots, S_d\}$: molecules that undergo a serie of chemical reactions.
- Reactant / Product, $C := \{y^1, \dots y^n\}$: Linear combination of species, that represent either 'what is consumed', or 'what is produced', in any reaction.
- Reaction, $\mathcal{R} := \{y^k \to y^{k'}, y^k, y^{k'} \in \mathcal{C}\}$: ensemble of reactions between species or combination of species (directed graph between Reactant / Product).

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- Mass-action law, a function κ : R → R^{*}₊ that gives to any reaction a positive parameter (kinetic rate)

Exemple

$$\varnothing \rightleftarrows A$$

Species $\mathcal{E} := \{A\}$ R / P $\mathcal{C} := \{\varnothing, A\}$ Reaction $\mathcal{R} := \{\varnothing \to A, A \to \varnothing\}$

Exemple B + ESpecies $\mathcal{E} := \{A, B, C, D, E\}$ $R / P C := \{A, 2B, A + C, D, B + E\}$ Reaction $\mathcal{R} := \{A \rightarrow 2B, 2B \rightarrow A, A + C \rightarrow D, D \rightarrow B\}$ $A + C, D \rightarrow B + E, B + E \rightarrow A + C$

Exemple (the one we will consider later on) $FSH + FSHR \Rightarrow FSH/FSHR$ $ATP + FSH/FSHR \rightarrow cAMP + FSH/FSHR$ $cAMP \rightarrow AMP$ species $\mathcal{E} := \{FSH, FSHR, FSH - FSHR, ATP, cAMP, AMP\}$ $R / P C := \{FSH + FSHR, FSH/FSHR, ATP + FSH - FSH, FSH/FSHR, ATP + FSH - FSH, FSH/FSHR, ATP + FSH - FSH/FSHR, ATP + FSH - FSH/FSHR, ATP + FSH/FSH/FSHR, ATP + FSH/FSHR, ATP$ FSHR, cAMP + FSH/FSHR, cAMP, AMP} Reaction $\mathcal{R} := \{FSH + FSHR \rightarrow FSH/FSHR, FSH/FSHR \rightarrow FSH/FSHR, FSH/FSHR \rightarrow FSH/FSHR, FSH/FSHR \rightarrow FSH/FSHR, FSH/FSHR \rightarrow FSH/FSHR$ $FSH + FSHR, ATP + FSH/FSHR \rightarrow$

 $cAMP + FSH/FSHR, cAMP \rightarrow AMP$

Chemical Reaction Network, "real" example

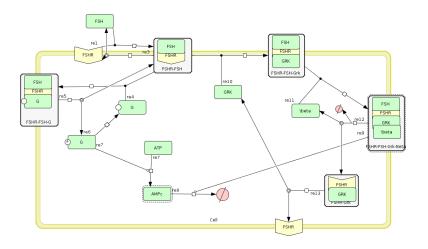


Figure – Classical GPCR models

Chemical Reaction Network, "real" example

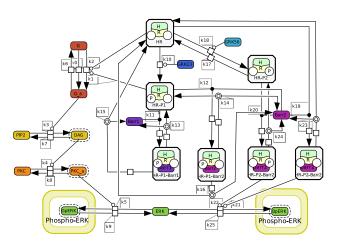


Figure – ERK Phosphorylation pathways, Heitzler et al. MSB 2012

Chemical Reaction Network and Dynamical models

A (deterministic) dynamical model of a Chemical Reaction Network keep track of

- concentration of species : $x_i \in \mathbb{R}_+$, i = 1..d.
- Reactions happens continuously and simultaneously
- [Law of Mass action] The velocity of a reaction is proportional to the concentrations of its reactants.
- Systems of Ordinary Differential Equations.

Chemical Reaction Network and Dynamical models

Exemple

$$\emptyset \stackrel{2}{\underset{0.1}{\rightleftharpoons}} A$$

$$\frac{dx_A}{dt} = 2 - 0.1x_A$$

Chemical Reaction Network and Dynamical models

Exemple

$$A \xrightarrow{100} 2B$$

$$A + C \xrightarrow{100} 100$$

$$D \xrightarrow{1.0} B + E$$

$$\frac{dx_A}{dt} = -0.8x_A + 100x_B^2 - 0.33x_Ax_C,$$

$$\frac{dx_B}{dt} = +0.8x_A - 2 \times 100x_B^2 + x_D,$$

$$\frac{dx_C}{dt} = -0.33x_Ax_C,$$

$$\frac{dx_D}{dt} = 0.33x_Ax_C - x_D,$$

$$\frac{dx_E}{dt} = x_D.$$

The equation

$$\frac{dx}{dt} = v(x),$$

is numerically solved by successive time-step iteration, of small length $\Delta t \ll 1$:

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Final Position = Initial Position + velocity * Time,

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which becomes, in mathematical notations,

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Iterate: To calculate the value of x at the next time step, use

$$x((i+1)*\Delta t) = x(i*\Delta t) + v(x(i*\Delta t))*\Delta t,$$

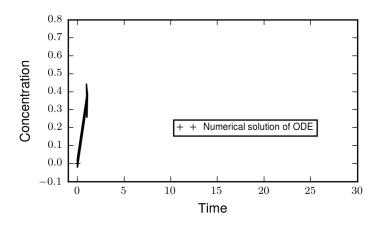


Figure - Solving an ODE

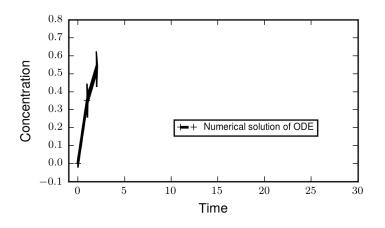


Figure – Solving an ODE

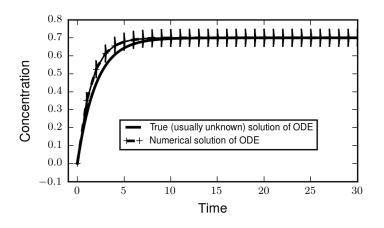


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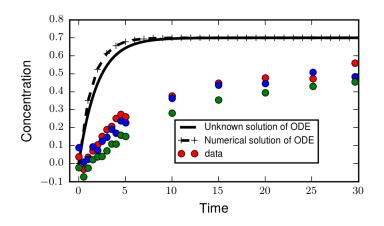


Figure – Solving an ODE

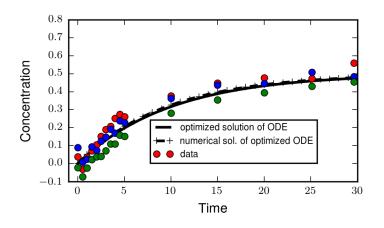


Figure – Solving an ODE

Parameter and network optimization in Chemical Reaction Network

Goal : Given some time series data, find the minimal (biologically plausible) reaction network with its parameter (=reaction rates and initial conditions) that fits consistently the data.

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Strategy 1) From a given network (S, C, R), with given parameter values, solve the ODEs,

$$\frac{dx}{dt} = v(x,k), \quad x(0) = x_0,$$

and compute a distance between the solution and the data.

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- **Strategy** 2) Using **optimization** algorithms, find the best parameter values k, x_0 , to minimize the distance
- **Strategy** 3) If needed, change the reaction network (add or delete species/reactions)

Goal: Given some time series data, find the minimal (biologically plausible) reaction network with its parameter (=reaction rates and initial conditions) that fits consistently the data.

Statistics There exists a well developed statistical theory to assess the quality of a fit and to resolve parameter non-identifiability (-> See Likelihood maximization or Bayesian statistics).

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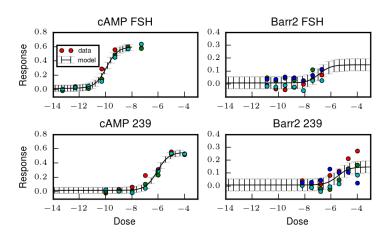


Figure – End-point Dose-response curves

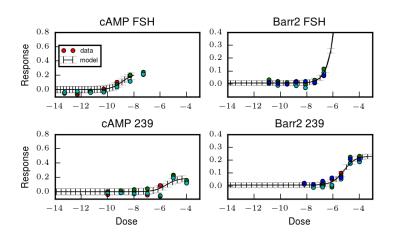


Figure – 2 minutes Dose-response curves

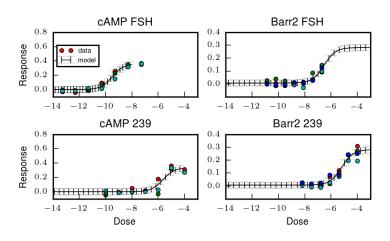


Figure – 5 minutes Dose-response curves

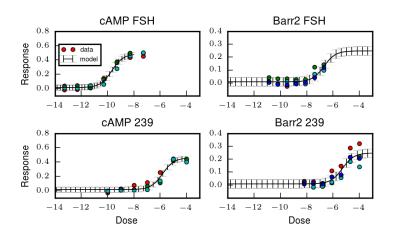


Figure – 10 minutes Dose-response curves

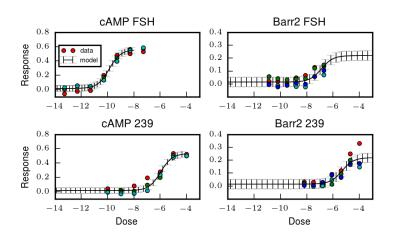


Figure – 20 minutes Dose-response curves

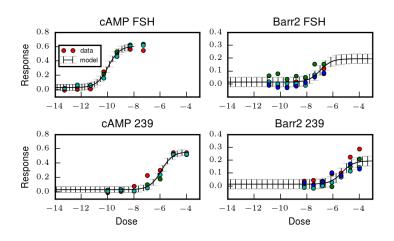


Figure – 30 minutes Dose-response curves

Dose-response curve and kinetic data

- All the analyses of dose-response curves at particular time points might not be consistent with respect to each other!
- See for instance "The role of kinetic context in apparent biased agonism at GPCRs", Klein Herenbrink et al. Nature Communications, 7, 2016.

Dose-response curve and kinetic data

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- See for instance "The role of kinetic context in apparent biased agonism at GPCRs", Klein Herenbrink et al. Nature Communications, 7, 2016.
- Go for a dynamical model!

Reaction network model

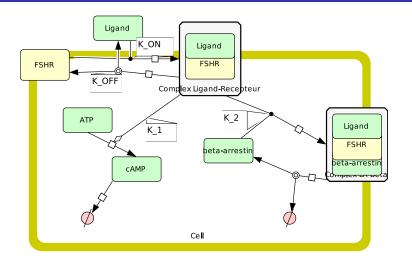


Figure - One possible model

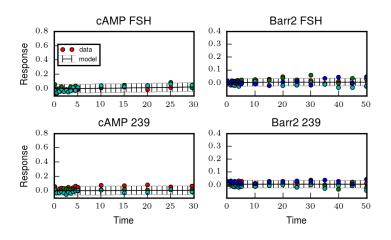


Figure - Dose 1

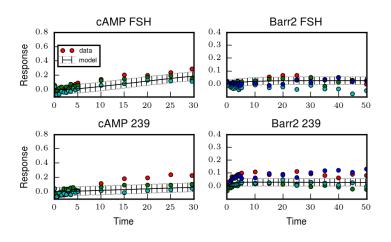


Figure - Dose 2

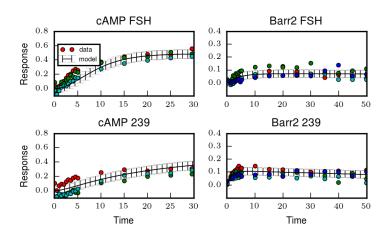


Figure - Dose 3

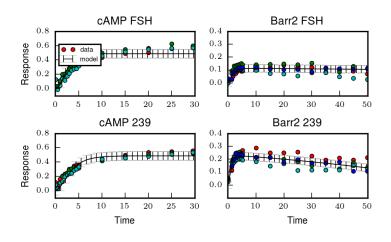


Figure - Dose 4

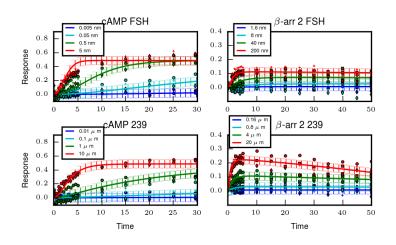


Figure – All doses in one fitted model

Parameter identifiability

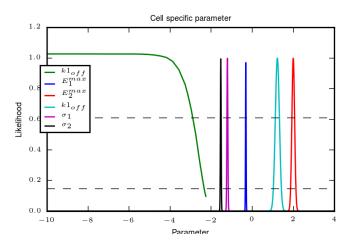


Figure – Cell parameters

Parameter identifiability

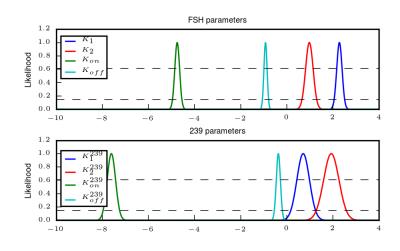


Figure – Ligand specific parameters

Reaction network model: bias between FSH and 239

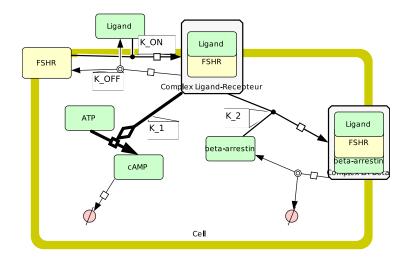


Figure - One possible model for FSH

Reaction network model: bias between FSH and 239

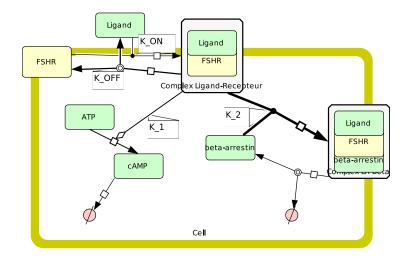


Figure - One possible model for 239