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## Meta-analysis for growth and survival data

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► **To cite this version:**

Jeanne Marie J. M. Membré. Meta-analysis for growth and survival data. FoodMicro 2016, University College Dublin (UCD). IRL., Jul 2016, dublin, Ireland. pp.1-26. hal-02799561

**HAL Id: hal-02799561**

**<https://hal.inrae.fr/hal-02799561>**

Submitted on 5 Jun 2020

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# META- ANALYSIS FOR GROWTH AND SURVIVAL DATA

*Jeanne-Marie Membré*

*FoodMicro 2016*



# Introduction

- Meta-analysis enables to **re-analyse “existing” data**, generated previously by scientists working on a comparable subject.
- Since the data have been collected by different research teams, in different laboratories with different experimental set up, there is a **natural heterogeneity between studies**.
- The advantage of the meta-analysis is to take explicitly the heterogeneity due to the study and other co-variables (e.g. strain, media) into account; the **inter-study variation is quantified**.
- As a consequence, **meta-analysis enables to produce a more precise estimate of the effect of a particular treatment** than a statistical analysis where the data are pooled regardless their sources.

# Key steps of meta-analysis

- Define the **objective of the meta-analysis**, the **scope** of the study: e.g. effect of thermal treatment on microbial behaviour, effect of storage conditions... etc
- Define the **criteria on which the studies will be collected**: microbial species, factors of variation, food matrix... etc
- Exhaustive **collection of studies** (e.g. peer-reviewed articles) according criteria
- Remove some of studies, if necessary, due to out-of-scope, methodology not sufficiently described, not enough data... etc
- Extract and **collect data** (store in a database)
- **Statistical analysis**
- **Interpretation of results**

# Fixed or random effects

## Fixed Effects Model

$$Y_i = \theta + e_i,$$

$$e_i \sim N(0, V).$$

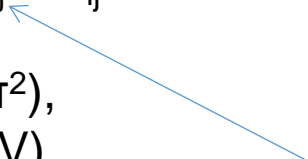
## Random Effects Model

$$Y_{ij} = \theta + \theta_j + e_{ij},$$

$$\theta_j \sim N(0, \tau^2),$$

$$e_{ij} \sim N(0, V)$$

Study  
effect



The Fixed Effects **model** is a description of the studies (whole population)

The Random Effects **model** regards the studies as a sample of a larger universe of studies.

The Random Effects **model** can be used to infer what would likely happen if a new study were performed, the Fixed Effects **model** cannot (Kovalchik, 2013)

**Mixed effect model: combined random and fixed effects in a model**

# Meta-Regression

Mixed Effects Model with a regression: **Meta-Regression**

$$Y_{ij} = \theta + \beta \cdot x_i + \theta_j + e_{ij}$$

$$\theta_j \sim N(0, \tau^2),$$

$$e_{ij} \sim N(0, V).$$

Study  
effect



$X_i$ : Study-level covariates

$Y_{ij}$  and  $X_i$  in growth

$Y_{ij}$ : growth rate, lag time, time to achieve a microbial level

$X_i$ : storage temperature, pH, salt content → Quantitative factors

$X_i$ : food matrix, microbial species, strains → Qualitative factors

$Y_{ij}$  and  $X_i$  in survival

$Y_{ij}$ : D-values, time to achieve a delta log

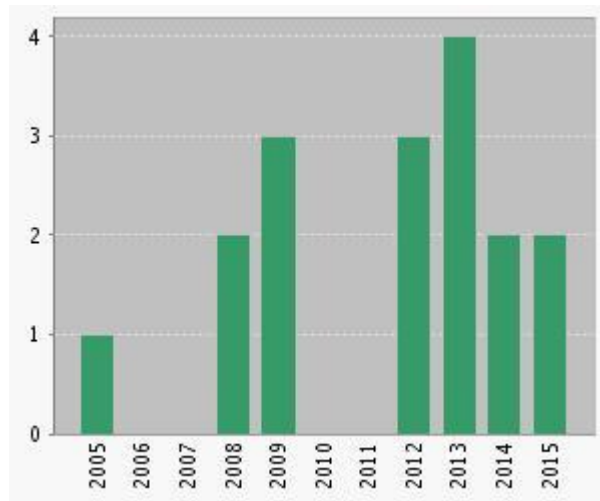
$X_i$ : storage temperature, pH, salt content (stressful conditions) → Quantitative

$X_i$ : process factors, e.g. thermal treatment T, HPP intensity → Quantitative

$X_i$ : food matrix, microbial species, strains → Qualitative factors

# Meta-analysis applied to growth or survival

- Articles in Web of Science
- **[TITLE: meta-analysis AND (growth OR survival OR inactivation OR D-values OR lag OR resistance OR assessment)] AND Topic microbiology**



Only few articles (17):

- relatively recent in the food microbiology area  
(≠ medical area)

Focus on:

- inactivation, decontamination
- antibiotic resistance (recent trend)

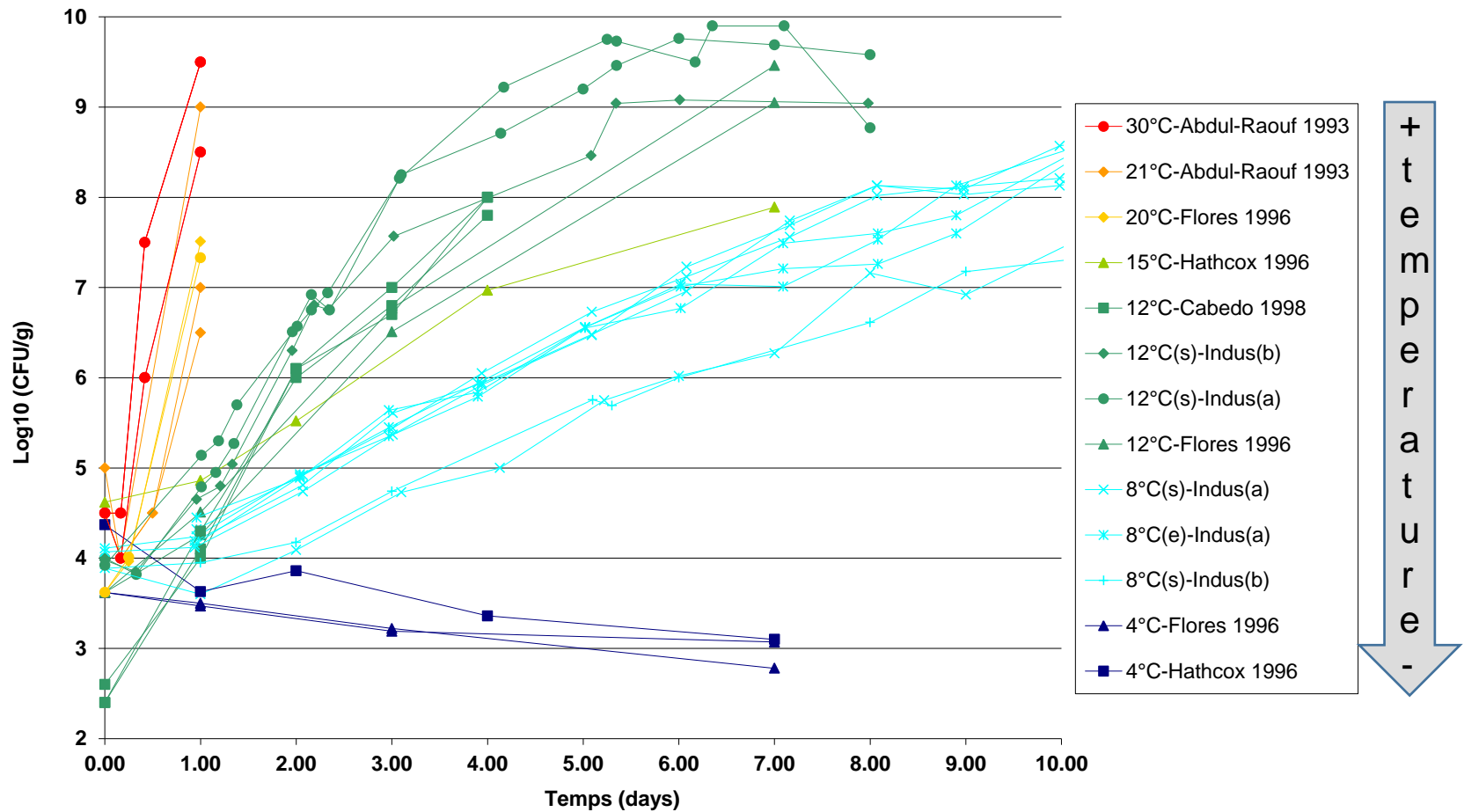
# Examples in growth





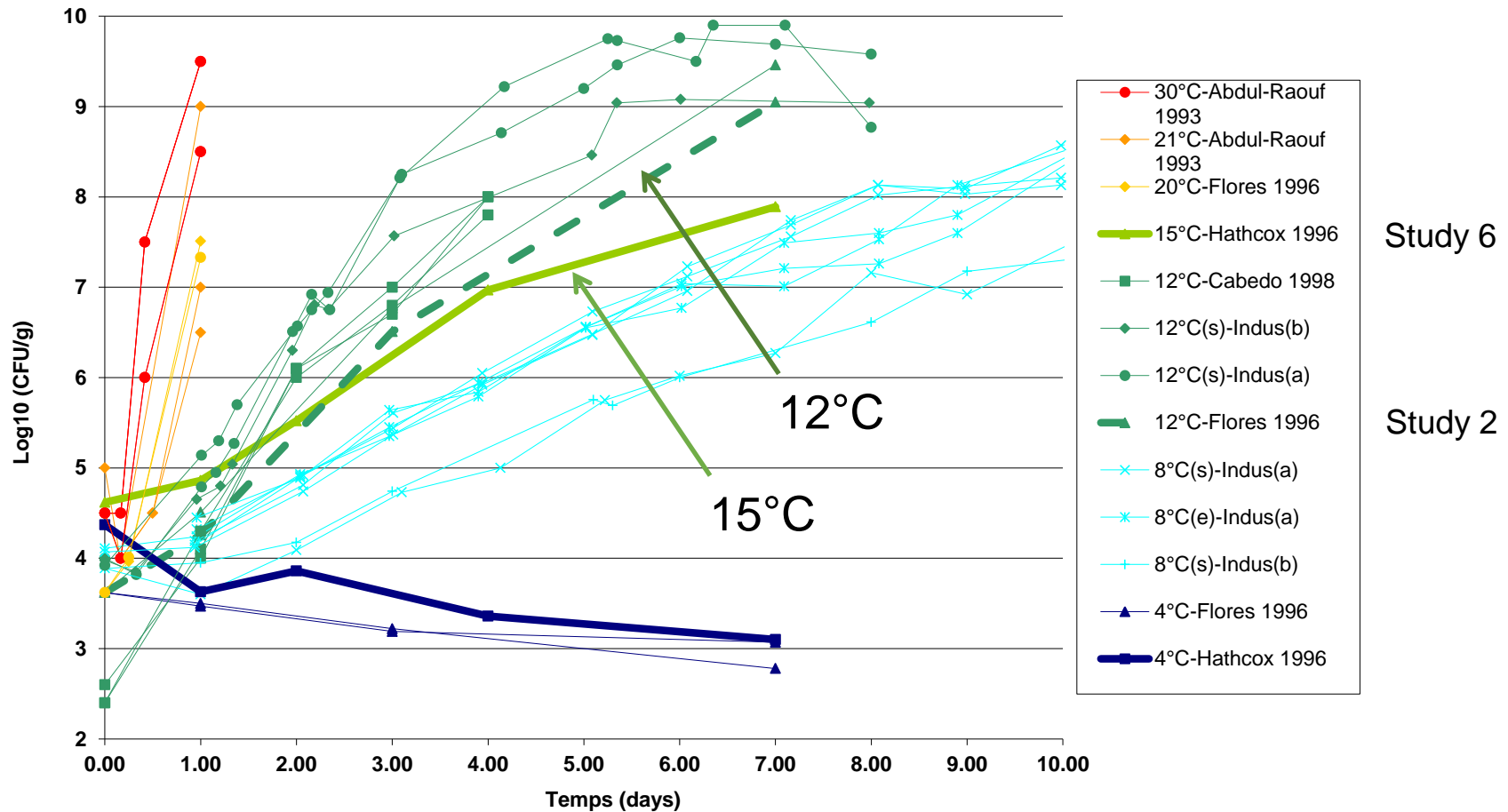
# Meta-regression applied to growth

- Adapted from Vialette et al. Risk Anal. 2005, Vol 25, pp 75-83.



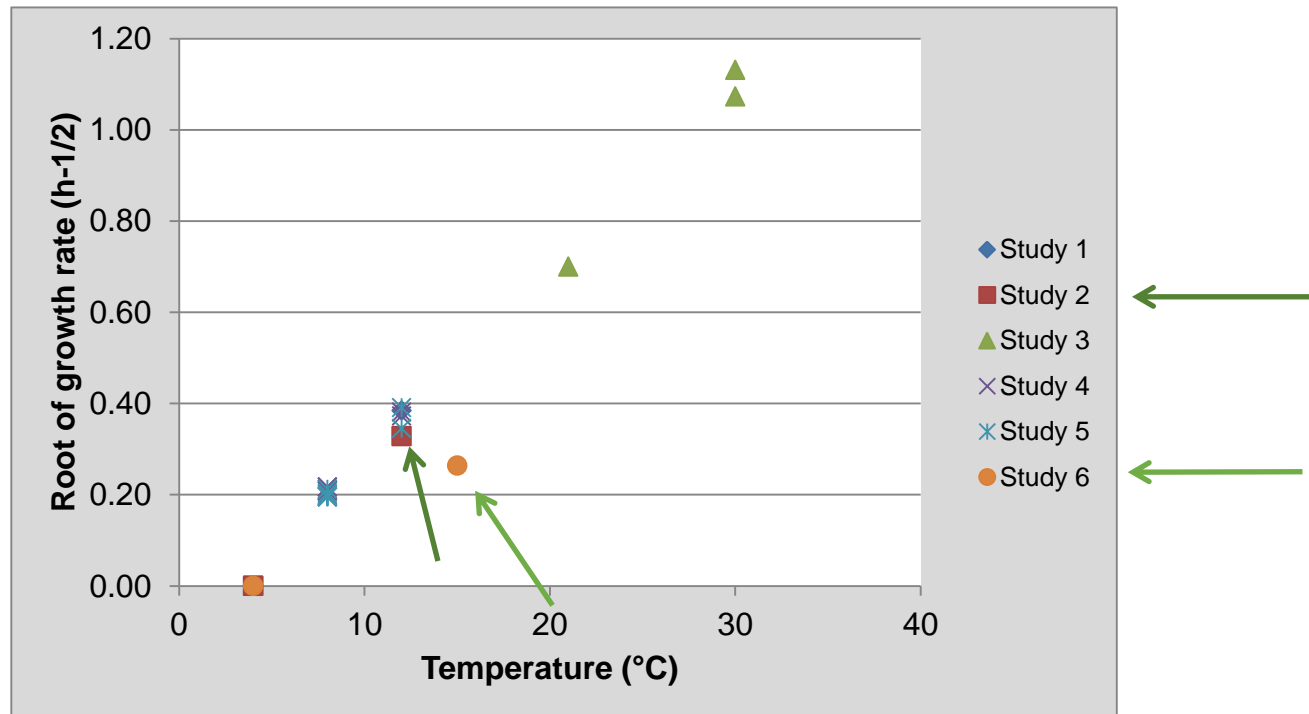
# Meta-regression applied to growth

- Adapted from Vialette et al. Risk Anal. 2005, Vol 25, pp 75-83.



# Meta-regression applied to growth

- Growth rates vs temperature, per study



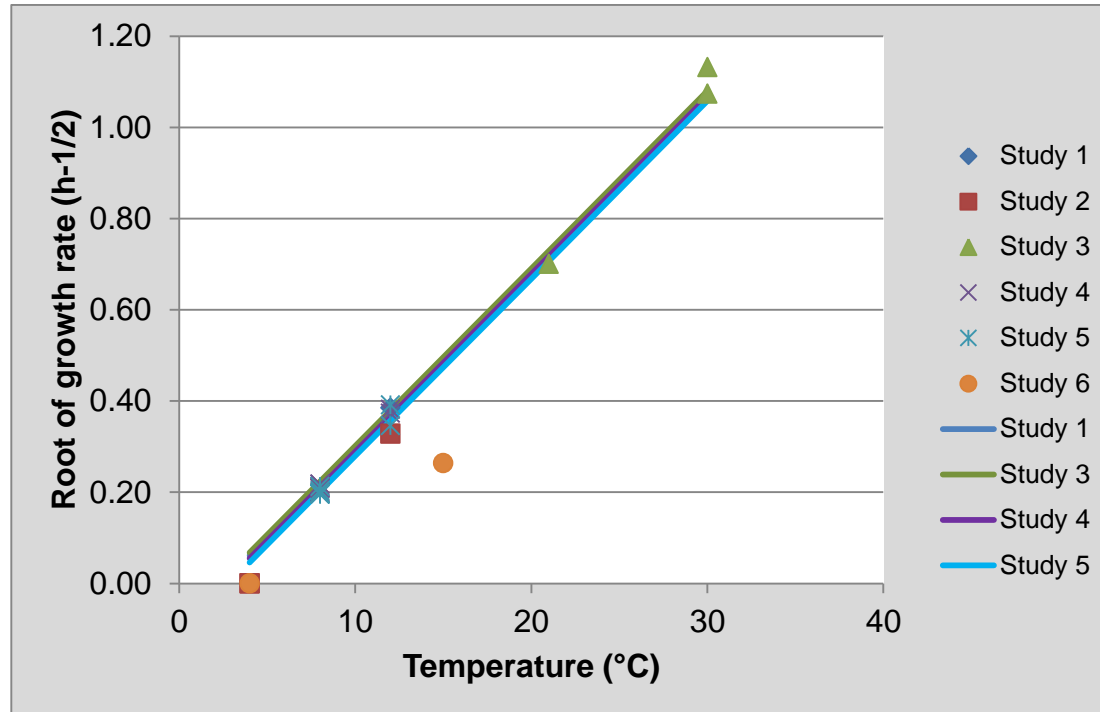
$$\sqrt{\mu_{ij}} = \sqrt{\mu'_{opt}} \times \sqrt{\gamma(T)_i} + a_j + \varepsilon_{ij}$$

j: study, i: data

Study effect

# Meta-regression applied to growth

- Growth rates vs temperature, per study: meta-regression



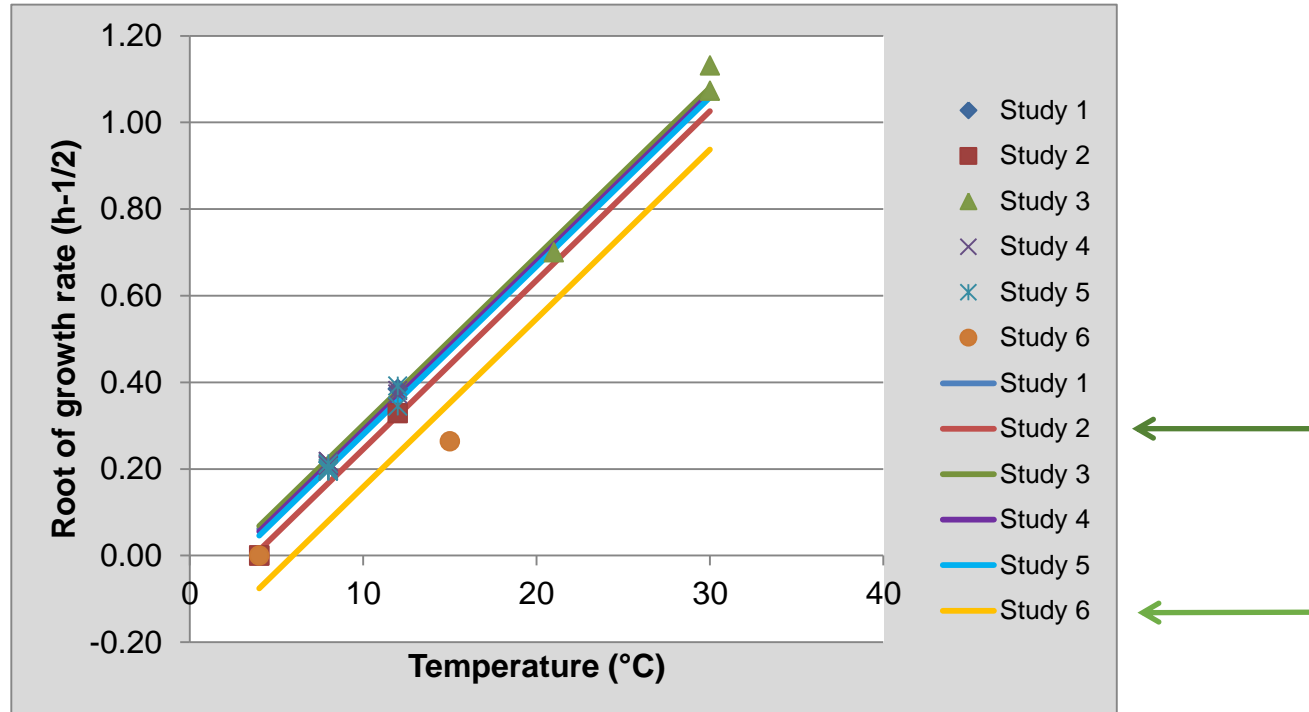
$$\sqrt{\mu_{ij}} = \sqrt{\mu'_{opt}} \times \sqrt{\gamma(T)_i} + a_j + \varepsilon_{ij}$$

j: study, i: data

Study effect

# Meta-regression applied to growth

- Growth rates vs temperature, per study: meta-regression



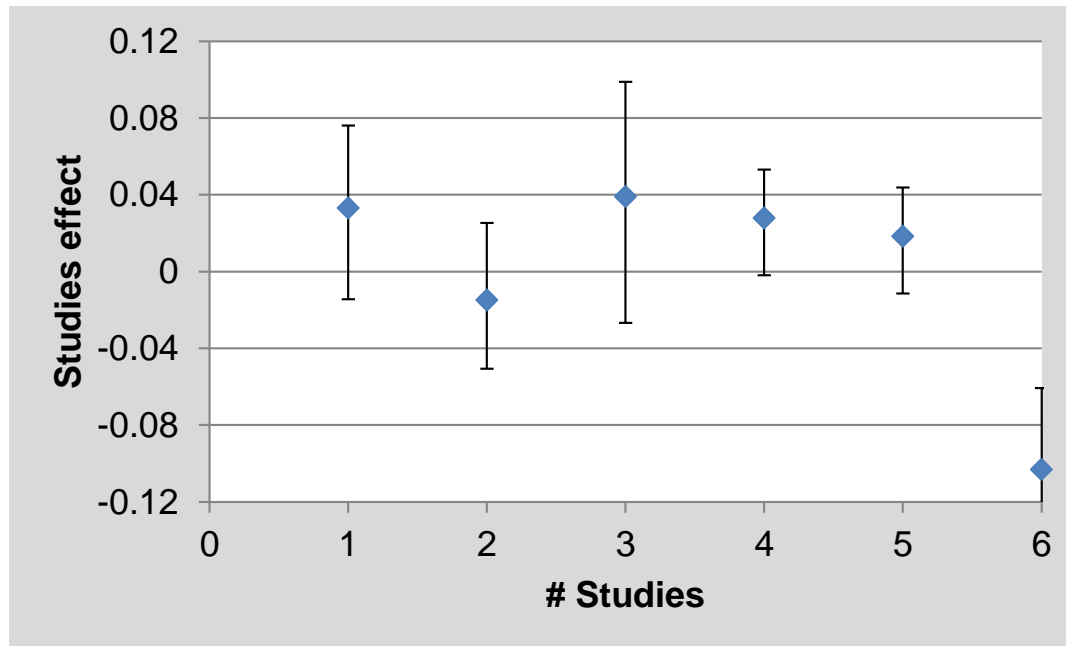
$$\sqrt{\mu_{ij}} = \sqrt{\mu'_{opt}} \times \sqrt{\gamma(T)_i} + a_j + \varepsilon_{ij}$$

j: study, i: data

Study effect

# Meta-regression applied to growth

- Growth rates vs temperature, per study: meta-regression



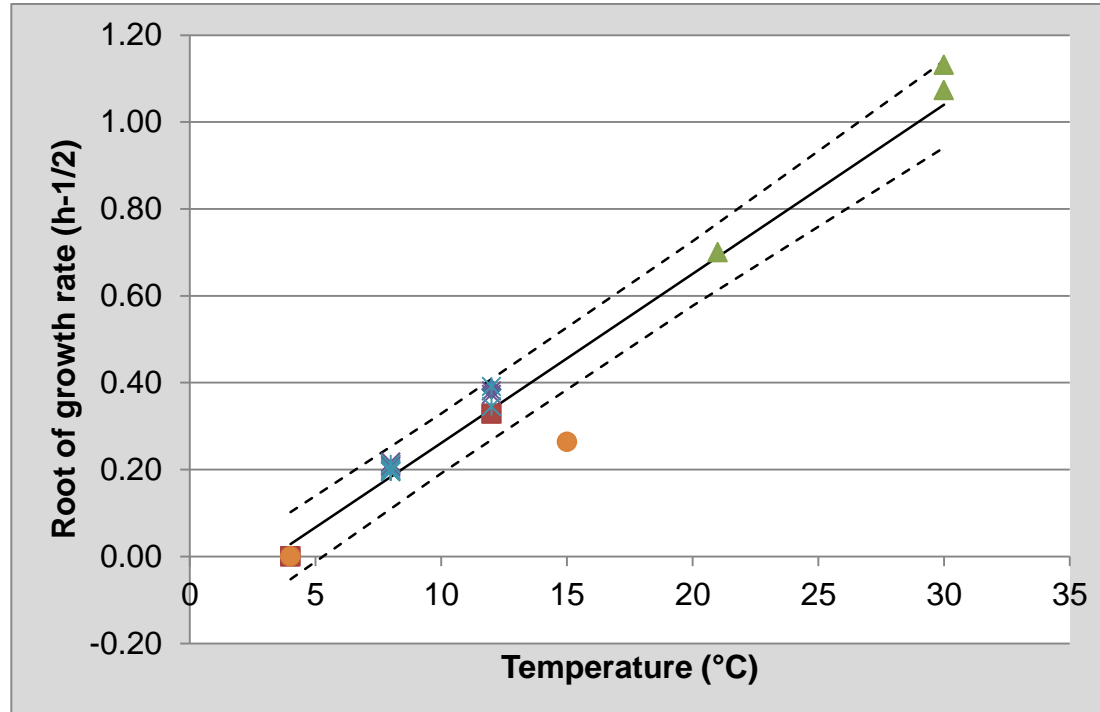
$$\sqrt{\mu_{ij}} = \sqrt{\mu'_{opt}} \times \sqrt{\gamma(T)_i} + a_j + \varepsilon_{ij}$$

j: study, i: data

Study effect

# Meta-regression applied to growth

- Growth rates vs temperature, average effect: meta-regression



$$\sqrt{\mu_{ij}} = \sqrt{\mu'_{opt}} \times \sqrt{\gamma(T)_i} + a_j + \varepsilon_{ij}$$

j: study, i: data

$$\sum a_j = 0$$

# Random effects

## Random Effects Model

$$Y_{ij} = \theta + \theta_j + e_{ij},$$

$$\theta_j \sim N(0, \tau^2),$$

$$e_{ij} \sim N(0, V)$$

Co-variates



The Random Effects model regards the co-variates as a sample of a larger universe of co-variates.

Not only “**studies**” should be considered in the model with a random effect. Very often:

Random effect for:

- **strains**
- **food matrix and/or medium**

Fixed effect:

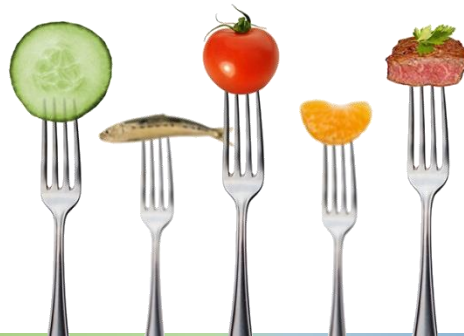
- Species

Choice of random / fixed depends on i) objective of the meta-analysis and ii) process of gathering data

**Mixed effect model: combined random and fixed effects in a model**



# Examples in inactivation



# Meta-regression applied to inactivation

- Ex. adapted from Diao et al. Int J Food Microbiol 174 (2014) 23–30

Objective: thermal treatment effect on inactivation of *C. botulinum* and surrogate

→ **D-values, proteolytic *C. botulinum* and *C. sporogenes* PA 3679**

911 data collected from 38 different studies, 2 species, 11 strains of *C. botulinum*

$$Y_{ij} = \theta + \beta \cdot x_i + \theta_j + e_{ij}$$

$$\theta_j : \alpha_{study} + \beta_{strain(species)} + \delta_{medium} + \eta_{pH}$$

$\beta \cdot x_i$  : effect of temperature (Z-values) depends on the species

Random effect of study, strain and medium

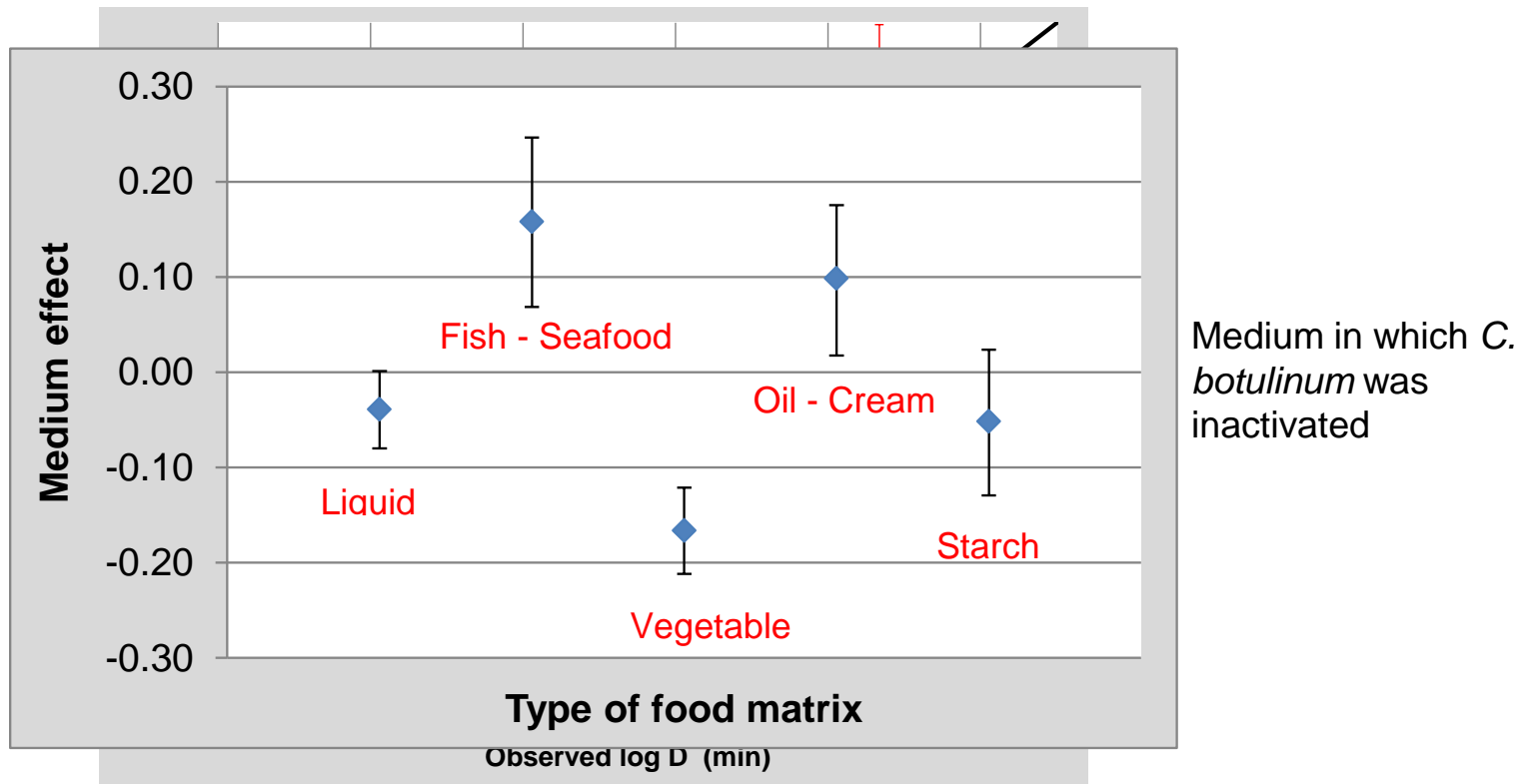
Fixed effect of pH

Hypothesis:  $e_{ij} \sim N(0, V)$ ,  $V$  identical among the two species

→ **Hierarchical mixed effect model**

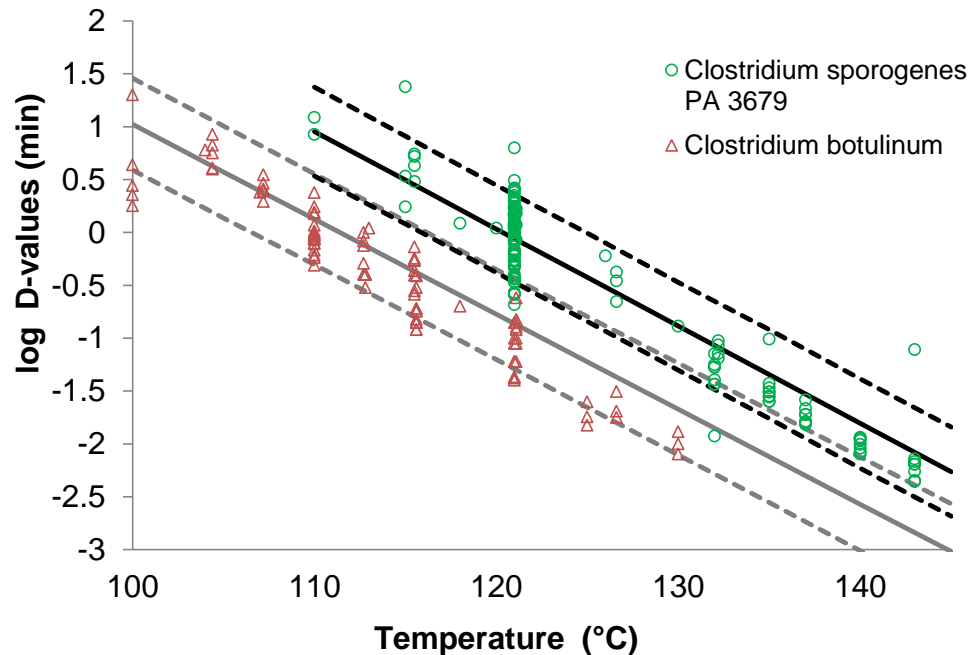
# Meta-regression applied to inactivation

- Adapted from Diao et al. Int J Food Microbiol 174 (2014) 23–30



# Meta-regression applied to inactivation

- Adapted from Diao et al. Int J Food Microbiol 174 (2014) 23–30



Inactivation  
in Vegetable

$$\log D_{ave} = \text{Log } D^* + \alpha_{study} + \beta_{strain(species)} + \delta_{medium} + \eta_{pH}$$

Slope (Z) depends on the species

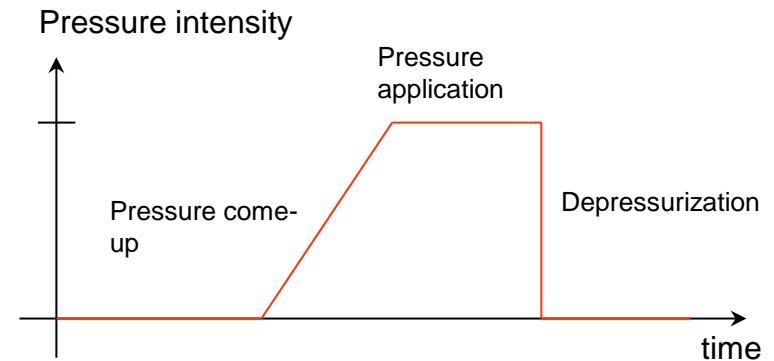
# Example in HPP inactivation



# Meta-regression applied to inactivation

Many factors might influence *microbial* inactivation:

- Depending on the process application
  - Kinetics of pressurization
  - Treatment duration
  - Pressure intensity
  - Temperature (cold, mild)
- Depending on the product itself
  - Quantity of fat, pH, water activity, chemical composition
- Depending on the microorganism
  - Species, strains...
  - Physiological state
- Depending on microorganism / product (contamination route)
  - Inoculum



# Meta-regression applied to inactivation

- **High Pressure Processing**

Response ( $Y_{ij}$ ): Time to obtain 3 log reduction

- **Focus on three main foodborne pathogens :**  
*Listeria monocytogenes, Salmonella and Staphylococcus aureus*
- Objective : To identify which factors influence *L. mono*, *Salmonella*, *S. aureus* inactivation
- **54 studies, 248 data**

# Meta-regression applied to inactivation

## Hierarchical mixed effect model

Response ( $Y_{ij}$ ): Time to obtain 3 log reduction:

- Depending on the process application
  - Kinetics of pressurization X
  - Pressure intensity ✓
  - Temperature (cold, mild) ✓
- Depending on the product itself
  - Quantity of fat, pH, water activity , chemical composition ✓
- Depending on the microorganism
  - Species, strains... ✓
  - Physiological state ✓
- Depending on microorganism / product (contamination route)
  - Inoculum ✓

On-going work, to be published in IJFM, Guillou et al.



# Conclusion



# Conclusion

- Microbial growth and survival: abundant literature, many data available
- **Meta-analysis is a powerful tool to integrate data from  $\neq$  studies**
  - Well adapted to growth, survival, inactivation  $\rightarrow$  Meta-regression on  $\mu$ ,  $\log D$ ...
  - Enable to identify significant effects and to build a predictive model
- It takes **explicitly the heterogeneity due to the study into account**; the inter-study variation is quantified.
- Meta-regression is a statistical technique, based on “mixed effect model”, with or without a hierarchical structure:
  - Fixed effect factor: e.g. temperature, species...
  - **Random effect factor: e.g. studies, strains, medium....**
- Should be encouraged among the food microbiologist community: statistically robust, relatively easy to implement, **faster (less labour intensive) and cheaper than lab experiments**



**Thank you!**

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