# Does random auditing reduce tax evasion in the lab? 

Mohammed Ali Bchir, Nicolas
Daures, Marc Willinger

## Motivations

- Empirical context
- Water extraction from aquifers in coastal zones
- High risk of saline intrusion
- Under-reporting of water extraction
- Designing mechanisms to reduce misreporting
- Random auditing + Fine
- Collective penalties (e.g. ambiant tax, ...)


## This study

- Authorities have limited information and limited budget
- Objective : minimizing the number of agents who cheat
- Mechanism with probabilistic audit
- Conditionnal audit probability (conditionned on past observed behavior)
Greenberg (1986)


## Assumptions (1)

- In each period, each agent receives a random income y
- Players report income $z \leq y$
- Net income
- If not audited : y - T(z)
(N.B. T(y) $\leq y$ )
- If audited:
- Truthfull reporting : y-T(y)
- Cheating : $y-T(z)-P(y, z)$ with $P(y, z)>T(y)-T(z)$
- Audit probability : $p>0$
- Audit is perfect


## Assumptions (2)

- Agents live an infinite number of periods
- Agents are risk-neutral
- Myopic behaviour
- $p_{i}(y)$ is the smallest audit probability for which player i reports truthfully
- Myopic players cheat for $p<p_{i}(y)$ whatever y
- (there exists $\rho>0$, such that for all $y$ and all i $p_{i}(y)>\rho$ )


## Assumptions (3)

- $r=$ audit probability determined by the tax authorithy's budget constraint (exogenous)
- If $r=1$ all players report truthfully
- If $r<\rho$ all players will cheat
- If $\rho<r<p_{i}(y)^{\text {max }}$ some players will cheat
- $\rightarrow$ they can increase their utility by cheating until they are audited, and then stop cheating
- The tax authorities try to minimize the number of tax evaders in the population $\mathrm{n}_{1}$


## Predictions (1)

No cheating


Audit proba
$\mathrm{p}_{2}<\mathrm{p}_{1}$


Audit proba

$$
\mathrm{p}_{3}=1
$$

## Predictions (2)

\(\left.$$
\begin{array}{c}\begin{array}{c}\text { All players } \\
\text { cheat }\end{array}
$$ <br>
Group 1 <br>
No player <br>

cheats\end{array}\right) \quad\)| No player |
| :---: |
| cheats |

## Experimental design (1)

- Income stream : each subject receives a randomly selected income between 100 and 1000 yens at each period
- Infinite lifetime (cont. prob = 0.9)
- Many lives : each subject experiences several lives.
- Ending : end time announced at the beginning. After end time, no new sequence could start. Running sequence were allowed to be continued during a maximum extra-time of 15 mn .
- Payment : One sequence randomly selected and paid out


## Experimental design (2)

- Two-treatments :
- T1 = low audit probability :

Group 1 : $\mathrm{p}_{1}=1 / 3$
Group 2 : $\mathrm{p}_{2}=1 / 4$

- T2 = high audit probability :

Group 1 : $\mathrm{p}_{1}=1 / 2$
Group 2 : $p_{2}=1 / 3$

- Penalty

$$
P(y, z)=(y-z) \times a
$$

## Summary of the data

|  | Low audit | High audit |
| :--- | :---: | :---: |
| Number of subjects | 36 | 38 |
| Average number of sequences <br> (min/max) | 7 <br> $(3 / 12)$ | 9 <br> $(4 / 16)$ |
| Average number of periods <br> (min/max) | 31 <br> $(21 / 82)$ | 30 <br> $(21 / 82)$ |
| Number of observations | 7630 | 10180 |

## Proportions of subjects in groups

|  | Low audit <br> $\left(p_{1}=1 / 3, p_{2}=1 / 4\right)$ |  | High audit <br> $\left(p_{1}=1 / 2, p_{2}=1 / 3\right)$ |  |
| :--- | :---: | :---: | :---: | :---: |
|  | Predicted | Estimated | Predicted | Estimated |
| Group 1 | $43 \%$ | $50 \%$ | $40 \%$ | $46 \%$ |
| Group 2 | $57 \%$ | $28 \%$ | $60 \%$ | $28 \%$ |
| Group 3 | $0 \%$ | $20 \%$ | $0 \%$ | $26 \%$ |

## Under-reporting



## Beginning and end behaviour

high audit probability


## Evolution of the frequency of fraud with repetition

Low audit

$\square$ group $1 \square$ group 2

High audit


## Frequency of fraud according to income (low audit)



## Frequency of fraud per income level for each group (low audit)



Frequency of fraud according to income (high audit)


## Frequency of fraud per income level for each group (high audit)



## Individual strategies

1. Predicted strategy (15\%)

Group 1 : Fraud the whole income almost always
Group 2 : No fraud (almost always)
2. Predicted strategy for high income only ( $23 \%$ )

Group 1 : Fraud the whole income only for high income
Group 2 : No fraud (almost always)
3. Cheating more frequently as income increases (27\%)

Fraud if income is high in both groups

## Predicted strategy (low audit)

| ID | Group 1 | Group 2 |
| :---: | :---: | :---: |
| 3 | 80,00 | 0,00 |
| 4 | 75,74 | 0,00 |
| 7 | 72,03 | 8,41 |
| 29 | 72,60 | 5,45 |
| 30 | 96,36 | 0,00 |
| 31 | 86,79 | 5,08 |



■ low incomes : y $\leq 350$

- high incomes y $: \geq 750$
middle incomes : $350<y<750$


| ID | Group 1 | Group 2 |
| :---: | :---: | :---: |
| 1 | 47,03 | 2,15 |
| 6 | 41,30 | 5,88 |
| 9 | 48,48 | 3,95 |
| 11 | 46,24 | $10,81^{*}$ |
| 24 | 48,61 | $16,67^{*}$ |
| 27 | 52,88 | 3,16 |
| 34 | 44,04 | 0,00 |

* Below 3,5\% after sequence 1

ㅁ. Low incomes : y $\leq 350$

- High incomes : y $\geq 750$
- Middle incomes :350 < y < 750


## Summary

- Mechanism to minimize fraud based on random auditing and segregation
- Group 1 :subjects fraud less frequently than predicted, and fraud only a part of their income
- Group 2 : subjects fraud too frequently
- In both groups fraud is more frequent as income increases


## Feasibility

$$
p_{1} \alpha+p_{2}(1-\alpha) \leq r \quad \rho \alpha<r
$$

Group 1
$\mathrm{p}_{1}=\frac{\rho}{2}$
$\frac{\rho}{2} \alpha$

## Group 3

$$
\mathrm{p}_{2}=\frac{\alpha}{1-\alpha} \times \frac{\rho}{2}
$$

$$
\frac{\alpha}{(1-\alpha)} \frac{\rho}{2}(1-\alpha)
$$

