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1 Sequential Preprocessing through ORThogonalization (SPORT) 2 and its application to Near Infrared Spectroscopy

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8 Abstract

9 In spectroscopy, multivariate calibrations more than often include a pre-processing step to
10 reduce the effect of unwanted (not Y-related) sources of variability. Because there are many
11 types of background noise, there are many pre-treatment methods. It is therefore tedious to
12 select and/or combine the best pre-treatments. This article proposes to combine several pre-
13 treatments through the use of sequential and orthogonalized partial least squares (SO-PLS),
14 thus leading to a boosting method. The performances and properties of this new method,
15 called Sequential Preprocessing through ORThogonalization (SPORT), are compared to those of
16 a previously published stacking method. SPORT demonstrates very good calibration
17 performances, but also the ability to make significant pretreatment selections.

18 Keywords

19 Spectroscopy, analytical techniques, pretreatments, ensemble, boosting, multi-block analysis,
20 sequential and orthogonalized partial least squares (SO-PLS), sequential preprocessing through
21 orthogonalization (SPORT)

22 Introduction

23 Spectroscopy and, more generally, analytical chemistry techniques provide multivariate
24 outcomes. These instrumental signals are often collected in order to evaluate one or more
25 properties of a product. This evaluation is generally based on calibrating a chemometric
26 model, e.g., by principal component regression (PCA) or partial least square regression (PLSR).
27 However, in these techniques, model building is based on extracting components which
28 account for a relevant share of the variance in the predictor space. Accordingly, whatever
29 phenomenon (wanted or unwanted) has an impact on the data variance can be included in the
30 predictive model, quite often, in the case of spurious variance, with a detrimental effect. For
31 this reason, the calibration of chemometric models generally includes a pre-treatment step, to
32 reduce the effect of these interfering phenomena. Such interferences are generally due to the
33 variation of physical (e.g. temperature) or chemical (e.g., humidity) influence factors.
34 Variations of these factors induce different effects on the measured spectra: the particle size
35 affects the baselines, the temperature affects the position and relative amplitude of the peaks,
36 the geometric configuration of the measurement induces additive and multiplicative effects,
37 etc. The wide variety of effects has led to the development of a large number of pre-treatment
38 methods [1]. The removal of a baseline, whatever its shape, is generally done by calculating
39 suitable approximations, either by a polynomial (Detrend [2]), a low-frequency filter (ALS,
40 Asymmetric Least Squares [3]), and then subtracting it from the measured data. The reduction
41 of multiplicative effects is achieved either by logarithmic transformation or by normalization
42 (SNV, Standard Normal Variate [2]), possibly weighted (VSN, Variable Sorting for Normalization
43 [4]) or in comparison with a reference spectrum (MSC, Multiplicative Scatter Correction [5]).
44 High frequency noise reduction is achieved by low-pass filtering (SG, Savitsky and Golay [6]).
45 The highlighting of spectral details is done by differentiation, usually through the SG algorithm,
46 which allows the computation of derivatives, without noise magnification. The correction of

47 harmful spaces, which can be observed, for example, when transferring a calibration between
48 two spectrometers, can be done by an orthogonal projection method (EPO, External
49 Parameter Orthogonalization [7]; TOP, Transfer by Orthogonal Projection [8]).

50 This raises the problem of choosing a suitable pre-treatment. In [9], different methodologies
51 are examined to select the appropriate pre-treatment. This article concludes that "... *how*
52 *extremely difficult it can be to determine which method - of the vast number of available pre-*
53 *processing methods - can successfully help...*". In addition, these pre-treatments are often
54 combined. In many articles, it can be read that baseline reductions are associated with
55 normalizations or even derivatives. These choices are often based on a trial and error
56 procedure, where the combination of different pre-treatments is done sequentially, e.g. SNV
57 followed by a derivative. In this regard, it should be noted that the order according to which
58 pre-treatments are applied may be important [9].

59 Another way to manage the choice and association of pre-processing is to use the so-called
60 "ensemble learning" methods [10]. Ensemble learning is similar to that of "data
61 augmentation", very common in deep learning [11]. Ensemble methods use several learning
62 algorithms to achieve better performance than each algorithm used alone. Several approaches
63 exist, as boosting, model averaging, model combination, buckets of models, stacking. All these
64 methods differ roughly in the way the algorithms are aggregated. For instance, in boosting
65 approaches weak learners are trained sequentially on different subset of samples (or, more
66 generally, on different weighting scheme over the training individuals) and, in order for each
67 successive model to be better than the predecessors, along the iterations higher weight (or
68 higher probability of being selected) is given to the most difficult samples. Instead, model
69 stacking, which is the form in which ensemble learning has mostly been used in chemometrics,
70 consists in training a meta-model to output a prediction based on the outcomes of the various
71 individual models, which, differently than in boosting can also be heterogeneous in nature; in

72 its simplest form, predictions from the weak learners can be gathered in a new data matrix,
73 which is used to build a final model. In [12], it is proposed to divide the NIR spectra into
74 intervals, then to stack the PLSR models performed on each interval by combining them by
75 linear regression. In [13], it is proposed to stack different PLSR models using different
76 pretreatments on the same data. Twenty different pre-processing operations, based on first
77 and second derivatives, smoothing, SNV, MSC and their combinations were performed on NIR
78 spectrum sets. A similar procedure, i.e., the exploitation of six PLS models (calculated on data
79 preprocessed by diverse preprocessing approaches) as learners in an ensemble learning
80 modelling algorithm was discussed in [14]. The output of this approach is computed by
81 averaging the predicted values computed by its constituent learners.

82 In the present article, the concept that different preprocessing strategies applied to the same
83 set of spectra could result in a multi-block data, and that, as such, the latter could be
84 processed as a whole through dedicated multi-block strategies, is exploited in a boosting
85 approach. In particular, due to its characteristics, the choice of the multi-block strategy to be
86 adopted has fallen on sequential and orthogonalized partial least squares regression (SO-PLS,
87 [15-16]), since it allows the possibility of including/excluding blocks, depending on their
88 relevance, of evaluating the incremental contribution of the different matrices and, up to a
89 certain extent, which blocks carry common and distinctive information. The resulting approach
90 has been called Sequential Preprocessing through ORThogonalization (SPORT) and it will be
91 described in detail in the following sections, together with examples of its application to real
92 world NIR data sets.

93 **Material and methods**

94 **Data sets**

95 The proposed method was tested on three sets of real data:

96 Wheat grain data [17]: The NIR transmission spectra of wheat seeds were measured at 100
97 wavelengths and used to calibrate the protein content. The data set contained a calibration set
98 of 415 samples and a test set of 108 samples.

99 Meat data [18]: The NIR transmission spectra of fine meat slices were measured at 100
100 wavelengths and used to calibrate the fat content. The data set contained a calibration set of
101 172 samples and a test set of 43 samples.

102 Tablet Data [19]: Near infrared spectra were collected on 310 tablets (spectral range between
103 7400 and 10507 cm⁻¹) whose relative active substance contents (% w/w) were available. Data
104 were divided by the Duplex algorithm [20] into a training and a test set of 210 and 100
105 samples, respectively.

106 Wheat and tablet data sets are freely available for download on the website of the
107 Chemometrics and Analytical Technology group of the Copenhagen University (KU):
108 www.models.life.ku.dk/datasets. The meat dataset is freely available for download on the
109 website of the Carnegie Mellon University, at: <http://lib.stat.cmu.edu/datasets/tecator>.

110

111 **The SPORT method**

112 As anticipated in the Introduction, the proposed method is based on processing the different
113 data matrices which result by preprocessing a spectral data set by different techniques
114 through a multi-block approach called sequential and orthogonalized partial least squares
115 regression (SO-PLS). As the name suggests, Sequential and Orthogonalized-Partial Least
116 Squares (SO-PLS) is a multi-block regression method where the information is sequentially

117 extracted from the different predictor blocks. Very concisely, considering the simplest multi-
 118 block scenario, i.e., the case of two predictor blocks (\mathbf{X}_1 and \mathbf{X}_2) used to estimate a \mathbf{y} response,
 119 the algorithm can be summarized by the following steps:

120 1. The \mathbf{y} response is fitted to \mathbf{X}_1 by PLS.

$$121 \quad \mathbf{y} = \mathbf{X}_1 \mathbf{b}_{X_1} + e_1 = T_{X_1} Q_{X_1}^T + e_1 \quad (1)$$

122 2. \mathbf{X}_2 is orthogonalized with respect to the scores extracted from the first PLS regression.

$$123 \quad X_2^{Orth} = \left[I - T_{X_1} (T_{X_1}^T T_{X_1})^{-1} T_{X_1}^T \right] X_2 \quad (2)$$

124 3. The orthogonalized \mathbf{X}_2 is used to predict the \mathbf{y} -residuals obtained from step 1.

$$125 \quad e_1 = X_2^{Orth} \mathbf{b}_{X_2^{Orth}} + e_2 = T_{X_2^{Orth}} Q_{X_2^{Orth}}^T + e_2 \quad (3)$$

126 4. The full predictive model is calculated summing up results from step 1. and step 3.

$$127 \quad \hat{\mathbf{y}} = \mathbf{X}_1 \mathbf{b}_{X_1} + X_2^{Orth} \mathbf{b}_{X_2^{Orth}} = T_{X_1} Q_{X_1}^T + T_{X_2^{Orth}} Q_{X_2^{Orth}}^T \quad (4).$$

128 In equations (1)-(4), b indicate regression coefficients, while T and Q the \mathbf{X} -scores and \mathbf{Y} -
 129 loadings, respectively.

130 If more data blocks are involved, they are orthogonalized with respect to all the previous
 131 modelled predictors and then used to estimate the \mathbf{y} -residuals. A wider discussion over the
 132 algorithm and the advantages/disadvantages of the method can be found in [15,21]. In SPORT,
 133 several pretreatments of the same data block are associated in an SO-PLS.

134 For each dataset, SPORT was applied with different pretreatments. A repeated cross-validation
 135 (2 random blocks by 10 repetitions) was performed for a number of latent variables varying
 136 from 0 to 15 for each pretreatment. The results of this cross-validation allowed us to choose

137 the **appropriate** number of latent variables to keep for each pretreatment, using the *global*
 138 *approach* described in [22]. **Briefly, this consist in building cross-validated SO-PLS models with**
 139 **all the possible combinations of latent variables (within a fixed maximum). The optimal**
 140 **complexity is then defined inspecting the RMSECVs.** Then, a SO-PLS model using these
 141 numbers was calibrated on the calibration set and applied on the test set. The root mean
 142 squared errors of calibration (RMSEC), cross-validation (RMSECV) and prediction (RMSEP) were
 143 calculated at each step of the process.

144 In order to compare the results of SPORT with the ones provided by the stacking approach, the
 145 same pre-treatments as in [13] were performed on the wheat and meat datasets, as reported
 146 in table 1.

147

148 *Table 1: list of the pretreatments applied on the datasets wheat and meat. *: SG-W-O-D means*
 149 *savitsky and Golay using a W points wide window, an O^{th} order polynomial and a D^{th} derivative*

Pretreatment
SG-9-3-0*
SG-9-4-0
SG-9-3-1
SG-9-4-1
SG-9-3-2
SG-9-4-2
SNV

150

151 **The order of the blocks may affect the results of SO-PLS, especially as far as the selection of**
 152 **the blocks is concerned.** The tablet dataset was used to test the order in which the blocks are

153 introduced in SPORT. Five pre-treatments, including “raw data” (i.e., just mean centering), first
 154 and second derivatives, SNV and VSN [21] were selected and combined as reported in Table 2.
 155 **Not all the possible orders were tested, but only the ones that reversed the orders of raw,**
 156 **differentiating and normalization processes.**

157 *Table 2: List of boostings of pretreatments applied on the tablet dataset, with different orders.*

Boosting 1	Boosting 2	Boosting 3
raw data	SNV	SG-15-3-2
SG-15-2-1	raw data	SNV
SG-15-3-2	SG-15-3-2	raw data
SNV	VSN, tol 0.0067, Npar 2	VSN, tol 0.0067, Npar 2
VSN, tol 0.0067, Npar 2	SG-15-2-1	SG-15-2-1

158

159 All the calculations discussed in the present paper were run under Matlab (The Mathworks
 160 Inc., MA). All the functions can be freely downloaded from:

161 <https://www.chem.uniroma1.it/romechemometrics/research/algorithms/>

162 **Results and discussion**

163 *Table 3: Results of the single and ensemble models on wheat and meat datasets. ^a: results*
 164 *taken from [13].*

Pre-treatment	Wheat			Meat		
	LVs	RMSEC	RMSEP	LVs	RMSEC	RMSEP
SG-9-3-0	11	0.53	0.71	6	2.97	2.80
SG-9-4-0	10	0.55	0.78	6	2.97	2.80
SG-9-3-1	8	0.55	0.66	11	2.11	2.09

SG-9-4-1	9	0.53	0.72	14	1.89	2.00
SG-9-3-2	6	0.54	0.52	10	1.97	2.08
SG-9-4-2	8	0.52	0.55	8	1.88	2.13
SNV	10	0.54	0.68	4	2.09	2.01
<i>stacked</i> ^o	-	0.50	0.57	-	1.55	1.82
boosted	0,0,4,0,0,0,11	0.47	0.47	0,0,0,0,0,7,7	1.50	1.65

165

166 Table 3 reports the results of the single block models, of the stacked approach and of the
167 SPORT approach, for both wheat and meat datasets. It can be noted that the models built on
168 raw data (after smoothing and mean centering) have poor performances and, in the case of
169 wheat, also require a large number of latent variables. For the wheat dataset, the best pre-
170 treatment is second derivative. It allows us to decrease the RMSEP from 0.70 to 0.51, i.e., a
171 gain of 50% in the error variance (from 0.49 to 0.25). Moreover, the number of latent variables
172 decreases from 11 to 6. When looking at the application of individual preprocessing strategies,
173 for the meat dataset, the gain is less spectacular. Indeed, the best first-derivative and SNV
174 approximately give the same RMSEP of about 2.00, in comparison to 2.01 for the model built
175 on raw data (after smoothing and mean centering). However, SNV allows us to decrease
176 dramatically the number of latent variables (from 14 to 4). As reported in [13], the stacked
177 model is slightly outperformed by the best single block pretreatments for the wheat dataset,
178 whilst it gives better performances for the meat dataset (RMSEP decreases from 2.01 to 1.82,
179 i.e. the error variance decreases by 20%). The SPORT models give the best performances on
180 both datasets. On the wheat data set, the resulting RMSEP is 0.47, representing a 55% gain in
181 the error variance compared to the raw model. On the meat data set, the RMSEP is 1.65,
182 representing 32% less error variance than the raw model. Compared to the stacked models,
183 the RMSEP decreases from 0.57 to 0.47 and from 1.82 to 1.65 for the wheat and meat
184 datasets, respectively, resulting in a corresponding improvement in error variance of 32 and

185 18%.

186 For both datasets, it can be noted that SPORT led to a very parsimonious selection of blocks,
187 since only two out of 7 blocks were used in the multi-block process. In both cases, a linear
188 pretreatment (SG) was associated with a non-linear pretreatment (SNV). For the wheat
189 dataset, SO-PLS has associated a first derivative (block 3) with SNV (block 7). This may seem
190 surprising at first sight, as the second derivative blocks (5 and 6) give much better performance
191 than the first derivative blocks (3 and 4). This illustrates well the ability of SO-PLS to identify
192 the blocks for additional (non-redundant) information, thanks to the orthogonalization steps
193 that take place between the addition of each new block. For meat data, the same
194 phenomenon can be observed. SO-PLS has associated a second derivative (block 6) with the
195 SNV (block 7), while the first derivative blocks (3 and 4) were the ones giving better
196 performances, when taken individually. In [16], Fig. 4 shows that stacking has also selected a
197 second derivative with SNV. This shows a good agreement between the two methods, with
198 regard to the selection of pre-treatments. Therefore, the reason of the difference in
199 performances observed should be ascribed to something else. It can be hypothesized that
200 stacking aggregation, which consists of a linear combination of the predictions of single block
201 PLS, is less effective than the iterative extraction of complementary information by SO-PLS. In
202 addition to the results obtained on our examples, this hypothesis is based on the fact that in
203 the case where the blocks are made up of different pretreatments of the same initial data set,
204 they contain a large redundancy of information, which is a situation that has to be handled
205 with precaution in a linear regression.

206 *Table 4: Results of different boosting orders on the tablet dataset.*

block number	Boosting 1	Boosting 2	Boosting 3
1	raw data	SNV	SG-15-3-2

2	SG-15-2-1	raw data	SNV
3	SG-15-3-2	SG-15-3-2	raw data
4	SNV	VSN, tol 0.0067, Npar 2	VSN, tol 0.0067, Npar 2
5	VSN, tol 0.0067, Npar 2	SG-15-2-1	SG-15-2-1
#LV	0,3,0,0,4	0,5,0,2,0	0,0,5,2,0
RMSEC	0.27	0.28	0.28
RMSEP	0.33	0.34	0.34

207

208 Table 4 shows the influence of the order in which the blocks are introduced into SPORT on the
209 tablet data. First of all, it can be noted that the performances obtained, both in RMSEC and
210 RMSEP, **are not very much influenced by** the order of the blocks. The total number of latent
211 variables used is the same in any order (7), but is distributed differently over the selected
212 blocks. SO-PLS systematically selected pairs of pre-treatments. It can be noted that the second
213 derivative is never selected. The SNV is not selected either, to the benefit of VSN, which is on
214 the contrary, always selected. This is in line with the fact that, on the one hand, VSN is a
215 generalization of SNV and is therefore supposed to give better results [21] and that, on the
216 other hand, at least one standardization method is selected because the tablet spectra contain
217 a very strong multiplicative effect [1,18]. The "raw data" + VSN pair is selected twice out of
218 three (boostings 2 and 3). In both cases, the block of the first derivative (SG1) was arranged
219 after these two blocks. On the other hand, if block SG1 is interposed between the raw data
220 block and the VSN block, it is selected instead of the raw data block.

221 Conclusion

222 This paper explores a new way to associate and select pre-treatments of spectra before their
223 use in a calibration model. This involves applying the different pre-treatments to the same set
224 of spectra, then combining the resulting blocks of data through a multi-block approach (SO-

225 PLS). As it proceeds by a sequential inclusion of the blocks that carry non-redundant
226 information, the proposed method, called sequential preprocessing through orthogonalization
227 (SPORT), belongs to boosting family of ensemble methods. The application of SPORT to
228 different datasets shows the advantage of associating pre-treatments in an ensemble method.
229 It also shows that our boosting approach, on the data sets used, is more efficient than the
230 stacking approach, already published. On the other hand, the influence of the order according
231 to which the individual blocks are processed was also studied. It appears that this order may,
232 as expected, influence which blocks are combined in order to build the final model, but it has a
233 rather small impact on the predictive performances. The use of SPORT in other, more complex
234 data sets and applications, such as discrimination, will allow for a more in-depth study of its
235 properties.

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