A new reflectivity index for the retrieval of surface soil moisture from radar data

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Abstract — A new approach based on the change detection technique is proposed for the estimation of surface soil moisture (SSM) from a time series of radar measurements. A new index of reflectivity (IR) is defined that uses radar signals and Fresnel coefficients. This index is equal to 0 in the case of the smallest value of the Fresnel coefficient, corresponding to the driest conditions and the weakest radar signal, and is equal to 1 for the highest value of the Fresnel coefficient, corresponding to the wettest soil conditions and the strongest radar signal. The Integrated Equation Model (IEM) is used to simulate the behavior of radar signals as a function of soil moisture and roughness. This approach validates the greater usefulness of the IR compared with that of the commonly used index of SSM (I_SSM), which assumes that the SSM varies linearly as a function of radar signal strength. The IR-based approach was tested using Sentinel-1 radar data recorded over three regions: Banizombou (Niger), Merguellil (Tunisia), and Occitania (France). The IR approach was found to perform better for the estimation of SSM than the I_SSM approach based on comparisons with ground measurements over bare soils.

Index Terms — change detection, index of reflectivity, index of surface soil moisture, surface soil moisture, Sentinel-1, radar

I. INTRODUCTION

Soil moisture is an essential parameter for analyzing interactions between the Earth’s surface and the atmosphere as well as the manner in which precipitation is ultimately allocated among the three main processes of runoff, infiltration and evapotranspiration [1-3]. In this context, remote sensing has demonstrated its considerable potential for monitoring the water content of soil surfaces [4-5]. Several different approaches have been used for this purpose, based primarily on the interpretation of passive and active microwave observations [6-15].

The first methods to be proposed were based on the use of data from the Soil Moisture and Ocean Salinity (SMOS) [7] and Soil Moisture Active and Passive (SMAP) [9] missions and produced SSM estimations at relatively low spatial resolutions of approximately 10-50 kilometers. So-called active radar missions involve the use of synthetic aperture radar (SAR) data and low-resolution scatterometers. Methods based on the use of SAR data are generally applied at the scale of agricultural fields [16-26] or at scales close to 1 km resolution [27-29]; in recent years, they have become more consistent and operational thanks to the arrival of the Sentinel-1 Copernicus constellation [28-29]. In this context, there are three main approaches to the inversion of radar signals: one is based on direct inversion of physical models [30-32], a second is based on statistical techniques such as neural networks [33-36], and the other is based on the use of change detection algorithms [37-40].

The change detection approach was first applied at a low spatial resolution with data provided by the European Remote sensing Satellite (ERS) and the Advanced SCATterometer (ASCAT) instrument on the METoerological OPerational satellite (METOP) platform of the European Space Agency (ESA) [37]. This approach was used to develop an operational product at resolutions of 12.5 and 25 km for water content monitoring at global scales and for operational applications. A moisture index between 0 and 1 was proposed, with 0 corresponding to the weakest radar signal and thus to the driest soil conditions and 1 corresponding to the strongest radar signal and thus to the wettest soil conditions, with the model assuming a linear relationship between radar signal strength and soil moisture. This approach has been generalized to other applications at medium and high spatial resolutions. Reference [28] thus developed soil moisture products at a 1 km spatial resolution using Sentinel-1 data, and these products are now used operationally for the European continent. The results illustrate the strong potential of this method, despite limitations in certain areas resulting from inaccurate modeling of the influence of vegetation on the backscattered radar signals [41]. Reference [39] also proposed an application based on the change detection technique for the study of soil moisture at a scale equivalent to the size of agricultural plots. These authors took the influence of vegetation cover into account and used optical images from the Sentinel-2 satellite to assess temporal variations in surface-scattered Sentinel-1

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radar signals. Reference [40] proposed an approach based on cumulative density function (CDF) matching, which is more sophisticated than the simple hypothesis of linearity between soil moisture and RADARSAT-2 radar signal strength. For all applications at high spatial resolutions, an accuracy generally better than 0.06 m$^3$/m$^3$ is achieved when this moisture index is converted to volumetric moisture. In conclusion, the main advantage of change detection approach is the simplicity of the proposed algorithms, the limitation of the number of input parameters, with high precision of the estimates. On this basis, it is suitable for an operational application.

In parallel with the aforementioned methods used for the inversion of radar signals, theoretical simulations and various experimental studies [42-46] have long shown that the relationship between radar signal strength and SSM is nonlinear, as clearly illustrated by the radar signal saturation at high soil moisture levels. Thus, despite the generally accurate estimations achieved with the change detection approach, the assumption of linearity between radar signals and SSM can lead to inaccurate soil water content estimations under extreme conditions, as has already been observed in areas affected by high moisture levels [47].

The purpose of this article is to propose an improved approach that is based on the change detection technique but takes into account the observed nonlinearity of variations in radar signal strength as a function of soil moisture.

Section II presents the study sites and data described in this paper. Section III describes the proposed methodology and introduces our new index of reflectivity (IR). Section IV presents the results and discusses the application of the proposed approach to three study sites based on Sentinel-1 time series data. Our conclusions are presented in section V.

II. STUDY SITES AND DATABASES

A. Study sites

In the present study, three sites were investigated. These sites, located in West Africa (Niger), North Africa (Tunisia) and Occitania (France) (Fig. 1), were equipped with ground stations.

1) Niger site

The ground measurements were carried out in southwestern Niger, near Banizombou, between the Niger River and the fossil valley of Dallo Bosso. This is a portion of a one square degree area (12°-13°N, 2°-3°E), defined in 1992 for the purposes of the international Hapex-Sahel survey and the African Monsoon Multidisciplinary Analysis–Coupling the Tropical Atmosphere and the Hydrological Cycle (AMMA-CATCH) observatory [48-49]. The Sahelian climate in this region is semiarid, with an average annual rainfall ranging between 300 and 750 mm, and is characterized by a rainy season from June to September. The landscape is mainly flat and is dominated by dissected plateaus with slopes of less than 6%. The plateaus have lateritic soils and are partly covered with tiger bushes. These plateaus are surrounded mostly by terrain with strong transitional features and steep inclines that can have slopes of up to 35%. Vegetation in the valleys is dominated by cultivated (mainly millet) and fallow fields. Over the studied site, a network of two continuous Thetaprobe stations (Delta T Devices) installed in locations with bare soil provided moisture measurements every 1 h, near Banizombou (~12°43’N; 2°30’E). At each station, all in situ measurements were made at depths of 5 cm and were calibrated using gravimetric measurements. The data for this site can be obtained from the International Soil Moisture Network (https://ismm.geo.tuwien.ac.at/en/).

2) Merguellil site

The Merguellil site is located in central Tunisia (9°54’E; 35°35’N). It is characterized by a semiarid climate with highly variable rainfall patterns, very dry summer seasons and wet winters. The average annual rainfall is approximately 300 mm/year [17]. The studied site is in an agricultural region where the dominant croplands are mainly olive groves and cereal fields; the croplands have large irrigated perimeters that mobilize large quantities of water for agricultural production. Over the studied site, a network of seven continuous Thetaprobe stations installed in locations with bare soil provided moisture measurements every 3 h. At each station, the measurements were made at depths of 5 cm. All soil moisture measurements were calibrated using gravimetric measurements. Four stations covering the period of Sentinel-1 measurements are considered in this study (Barrage (~35°35’N; 9°45’E), Barrouta (~35°36’N; 10°04’E), Bouhajla (~35°21’N; 10°12’E) and INGC (~35°37’N; 9°56’E)). The data for this site can be obtained from http://osr-cesbio.upssltlse.fr/.

3) Occitania sites (France)

The Occitania region was studied at several different sites close to the cities of Toulouse and Montpellier. The in situ SSM measurements were provided by the soil moisture observing system–meteorological automatic network integrated application (SMOSMANIA) observation system. SMOSMANIA is a long-term project that has been organized in an effort to acquire SSM profiles from automated weather stations in southwestern and southeastern France [50]. The stations were chosen in order to form a Mediterranean–Atlantic transect for studying the marked climatic gradient between the two coastlines. The SSM probes (ThetaProbes) were calibrated at all depths (5, 10, 20, 30 cm) by measuring the SSM from gravimetric soil samples collected during the installation. In this study, only the measurements at 5 cm depth were used. While this region mainly consists of croplands, the stations are generally located in grasslands. Two stations (at Mouthoumet (~43°N; 2°31’E) and Narbonne (~43°11’N; 3°E) that are representative of climate and land cover types in the Occitania region were analyzed in this study. Their mean temperatures ranged between 12.3 and 15.2°C, and their mean annual precipitation ranged between 649 and 845 mm. Data for these stations can be obtained from...
the International Soil Moisture Network (https://ismn.geo.tuwien.ac.at/en/).

B. Sentinel-1 data

Sentinel-1A and Sentinel-1B images were acquired between December 2015 and the end of 2019. These two satellites circle the Earth in the same orbital plane, 180° from each other. Their SAR instruments operate in the C-band (5.4 GHz) and the interferometric wide-swath (IW) mode and have a spatial resolution of 10 m. Each satellite has a revisit time of 12 days, which implies an overall revisit time in Europe equal to six days. The sensors provide dual-polarization imagery (copolization (VV) and cross-polarization (VH)) at an incidence angle ranging between 31° and 43°. We used Level-1 ground range detection (GRD) products that are derived from focused SAR signals that have been detected, multi-looked and projected to ground range using an Earth ellipsoid model [51].

The image processing was executed using the Sentinel Application Platform (SNAP) toolbox. The first step in this process converts the signal to obtain the backscattering coefficient. A terrain correction is then applied to correct for geometric distortions using a digital elevation model (DEM), specifically, the DEM derived from the Shuttle Radar Topography Mission (SRTM) at 30 m spatial resolution. Finally, thermal noise removal and a Lee filter are applied to reduce speckle effects. In the present study, only VV polarization data were considered.

III. METHODOLOGY

A. Behavior of IEM backscattering simulations over bare soil

To analyze the behavior of radar signals backscattered by soil surfaces, we used the IEM, which is considered to be the model that is best suited to a wide range of soil roughness values. In this study, all simulations were considered in the VV polarization, which corresponds to the data provided by the Sentinel-1 mission. The IEM is expressed as [43]:

\[
\sigma_{VV} = \frac{k^2}{2} e^{-2k_s^2} \sum_{n=1}^{\infty} \frac{s^{2n} |l_{VVn}|^2 W^{(n)}(-2k_s^2,0)}{n!}
\]  

(1)

where \( \sigma_{VV} \) is the backscattering coefficient, \( \theta \) is the radar incidence angle, \( k \) is the wavenumber, \( k_s = k \times \cos(\theta) \), \( s \) is the root mean surface height, \( l_{VVn} \) is a function of the radar incidence angle, the relative dielectric constant of the soil, \( \epsilon_r \), and the Fresnel reflection coefficient. \( W^{(n)}(-2k_s^2,0) \) is the Fourier transform of the \( n \)th power of the surface correlation function.

\( R_{VV} \) is the Fresnel coefficient for the VV polarization:

\[
R_{VV} = \frac{\cos(\theta) - \sqrt{\frac{1}{\epsilon_r}} (1 - \sin^2(\theta))}{\cos(\theta) + \sqrt{\frac{1}{\epsilon_r}} (1 - \sin^2(\theta))}
\]

(2)

Fig. 2 provides a simulated view of IEM backscattering as a function of soil moisture and at different roughness levels. In this study, for the roughness description, we used the statistical parameter \( Z_s \), which combines the effects of \( s \) and correlation length, as proposed by [52]. The effect of the autocorrelation function is very important in the simulation of soil scattering [53]. Only the exponential autocorrelation function, which is generally considered appropriate for natural surfaces, was used in the simulations illustrated in this article. However, we note that simulations using the Gaussian autocorrelation function produced the same conclusions. For these simulations, the SSM was considered to range between 0.03 m³/m³ and 0.4 m³/m³. In the IEM, the relative dielectric constant is computed from soil moisture using the Hallikainen model [54]. An approximately logarithmic relationship was found between the simulated radar signal (in VV polarization) and the two surface parameters, SSM and roughness (\( Z_s \)). The signal became almost saturated at high SSM values. When the soil moisture ranged between 0.3 to 0.4 m³/m³, the resulting increase in radar signal was close to 1 dB, corresponding to a slope of approximately 10 dB/m³/m³. However, when the SSM ranged between 0.1 and 0.3 m³/m³, the slope of this function increased to approximately 25 dB/m³/m³. The roughness effect was approximately the same for the entire moisture range, with an increase in the signal with roughness from \( Z_s = 0.05 \) cm to \( Z_s = 0.25 \) cm and a quasi-saturation of the simulated signal starting at \( Z_s = 0.2 \) cm. The simulation did not exceed \( Z_s = 0.25 \) cm to avoid IEM simulations out of its validity domain.

From these results and using the approximation of the small perturbation model [55], the radar signal \( \sigma_{VV} \) is considered to be the sum of a function that depends on roughness \( g_{VV} \) and another function that depends on the Fresnel coefficient (soil moisture) \( f_{VV} \):

\[
\sigma_{VV} = f_{VV}(\log(R_{VV})) + g_{VV}(Zs)
\]

(3)

Fig. 3 shows the IEM-simulated backscattering in the VV polarization (C-band) for the same range of values of SSM and \( Z_s \) as those used in Fig. 2. In this case, the simulated radar signal strength is plotted as a function of the Fresnel coefficient (\( \log(R_{VV}) \)) and for different \( Z_s \) values (0.05 cm, 0.1 cm, 0.15 cm, 0.2 cm, 0.25 cm). The radar signal is shown to have a nearly linear behavior as a function of (\( \log(R_{VV}) \)) over the full range of roughness values, with a correlation coefficient \( R^2 \) greater than 0.98. The function \( f_{VV} \) can thus be expressed as:

\[
f_{VV}(\log(R_{VV})) = a_{VV} \times \log(R_{VV}) + \beta_{VV}
\]

(4)
where $\alpha_{VV}$ is the slope of $f_{VV}$ as a function of $\log(R_{VV})$ and $\beta_{VV}$ is a constant parameter corresponding to the value of $f_{VV}$ when $R_{VV}$ is equal to 1.

**B. The classical soil moisture index, $I_{SSM}$**

The classical change detection SSM index $I_{SSM}$ [34] is defined as:

$$I_{SSM} = \frac{\sigma_{VV} - \sigma_{VV_{min}}}{\sigma_{VV_{max}} - \sigma_{VV_{min}}} = \frac{SSM_t - SSM_{min}}{SSM_{max} - SSM_{min}}$$

(5)

Where $SSM_t$ is the soil moisture content at time $t$; $SSM_{min}$ and $SSM_{max}$ are the minimum and maximum values of in situ soil moisture, respectively, measured at a depth of 5 cm; $\sigma_{VV}$ is the radar signal at time $t$; and $\sigma_{VV_{min}}$ and $\sigma_{VV_{max}}$ are the minimum and maximum values of the radar signal time series, respectively.

To convert this index to volumetric soil moisture, we introduce:

$$SSM_t = I_{SSM} \times (SSM_{max} - SSM_{min}) + SSM_{min}$$

(6)

**C. The new reflectivity index, $IR$**

Based on the linear behavior described above, for the radar signal simulated as a function of the Fresnel coefficient (on a logarithmic scale), we propose a new reflectivity index. From equations (3) and (4), the index can be expressed as:

$$IR = \frac{\sigma_{VV} - \sigma_{VV_{min}}}{\sigma_{VV_{max}} - \sigma_{VV_{min}}} = \frac{\log(R_{VV}) - \log(R_{VV_{min}})}{\log(R_{VV_{max}}) - \log(R_{VV_{min}})}$$

(7)

where $R_{VV_{min}} = R(SSM_{min})$, the minimum value of the Fresnel coefficient, and $R_{VV_{max}} = R(SSM_{max})$, the maximum value of the Fresnel coefficient.

This $IR$ is equal to zero for the weakest radar signal, corresponding to the lowest value of the Fresnel coefficient and thus to a minimum value of soil moisture. Similarly, this index is equal to 1 for the strongest radar signal, corresponding to the highest value of the Fresnel coefficient and thus to a maximum value of soil moisture.

A given value of the $IR$ can be converted to volumetric soil moisture using the same approach as that proposed for the $I_{SSM}$ using the minimum and maximum values of SSM for a given site:

$$\log(R_{VV} (SSM_t)) = \log(R_{VV_{min}} (SSM_{min})) + IR \times (\log(R_{VV_{max}} (SSM_{max})) - \log(R_{VV_{min}} (SSM_{min})))$$

(8)

From the theoretical relationship between $R_{VV} (SSM_t)$ and the soil moisture, as defined in equation (2), the estimated value of $\log(R_{VV} (SSM_t))$ can be inverted to retrieve the soil moisture, $SSM_t$.

**IV. RESULTS AND DISCUSSION**

**A. Analysis of IR potential using an IEM simulation series with constant roughness**

We produced a simulated series of IEM backscattering coefficients in the VV polarization at 5.3 GHz containing 10,000 samples with a Gaussian distribution that corresponded to a range of soil moisture between 0.03 m$^3$/m$^3$ and 0.4 m$^3$/m$^3$, a root mean square (rms) height equal to 0.8 cm, a correlation length equal to 6 cm, and an incidence angle equal to 40°. A noise signal respecting a Gaussian distribution and a standard deviation equal to 0.5 dB was added to the simulated radar signals to approximate real Sentinel-1 radar measurements [56]. Fig. 4 shows the resulting time series simulation.

Figs. 5-a and 5-b plot the estimated values of soil moisture as a function of the input values of soil moisture used for the simulations, retrieved using the $I_{SSM}$ and the proposed $IR$, respectively. The $IR$ was estimated from equation (7) using backscattering coefficients derived from the IEM simulations with additional Gaussian noise. The soil moisture was then calculated with equation (8). The minimum and maximum values of soil moisture used to compute $R_{VV_{min}}$ and $R_{VV_{max}}$ were derived from the input soil moisture series and applied to the IEM. The $I_{SSM}$ was computed from equation (5) using backscattering coefficients derived from the IEM simulations with additional Gaussian noise. The SSM was then calculated with equation (6).

Figs. 5a and 5b show that the $IR$-based approach leads to an improved estimation of the surface moisture, with a root mean square error (RMSE) equal to 0.023 m$^3$/m$^3$, when compared to the values of soil moisture determined with estimations using $I_{SSM}$, for which the RMSE was equal to 0.055 m$^3$/m$^3$. With the latter index, the strongest bias was observed for average moisture values in the range of 0.1-0.2 m$^3$/m$^3$, since the model was initially calibrated with respect to the extreme values of soil moisture, i.e., values close to 0 m$^3$/m$^3$ and 0.4 m$^3$/m$^3$. In the $IR$-based approach, the errors in estimated soil moisture increased with increasing actual soil moisture. In particular, the accuracy of this method decreased for high moisture values due to the saturation of the radar signal and the resultant stronger effects of radar noise. RMSE values for all moisture ranges (0-0.1 m$^3$/m$^3$, 0.1-0.2 m$^3$/m$^3$, 0.2-0.3 m$^3$/m$^3$, 0.3-0.4 m$^3$/m$^3$) are provided in Table I. As noted above, the greatest difference between the two approaches was obtained at average values of soil moisture.

**B. Analysis of IR potential using an IEM simulation series with variable roughness**

As in section IV-A, a series of IEM simulations of 10,000 samples with the same added noise is analyzed. In addition to the variation in soil moisture, we also include a roughness variation as input to the IEM simulations to evaluate its effect.
on IR potential. A Gaussian variation in the standard deviation of the heights, with a mean of 0.8 cm and a standard deviation of 0.2 cm, was used for the IEM simulations of the 10,000 samples. Figs. 6-a and 6-b plot the estimated values of soil moisture obtained using the $I_{SSM}$ and the proposed IR, respectively, as functions of the soil moisture input values used for the simulations. For the proposed analysis, which used a variable roughness, the estimate based on IR showed higher precision, with an RMSE of 0.038 m$^3$/m$^2$, than the estimate based on $I_{SSM}$ (RMSE of 0.068 m$^3$/m$^2$). Obviously, in both cases, the precision is much lower than that in simulations without variations in roughness. However, for the IR estimation, the RMSE remained below 0.05 m$^3$/m$^2$, which is generally taken as an acceptable threshold for the precision of soil moisture estimates. The maximum difference between the respective accuracies of IR and $I_{SSM}$ remained in the range of 0.1-0.2 m$^3$/m$^2$, as shown in Table I. In the context of real data, roughness is rarely considered in proposed change detection algorithms. Using low-resolution data such as those from scatterometers [37] or working at average scales of approximately 1 km makes it possible to assume that the average roughness remains slightly variable. This assumption could decrease the precision of the estimates if there were important temporal changes in roughness.

C. Evaluation of the IR across three study sites

Following our validation of the proposed approach based on the IR, the method was applied to soil moisture data from eight ground stations located within the three study sites (Occitania, Merguellil, Banizombou) described in section II. Five of the selected ground stations (BZ1, BZ2, Bouhajla, Barrage, Barrouta) are characterized by a landscape with either bare soil or low-density vegetation cover, and three others (INGC, Mouthoumet, Narbonne) are characterized by an agricultural landscape with important temporal dynamics in vegetation cover.

We identified a 1 km$^2$ zone centered around each moisture measurement station and derived an averaged radar signal (in the linear domain) for each Sentinel-1 acquisition for each zone. Only pixels with radar signal values between -20 dB and -5 dB were taken into account to avoid possible extremes from surfaces other than natural surfaces (such as water coverings or buildings) [28]. The choice of the 1 km$^2$ size was intended to limit the effects linked to roughness as much as possible and to enable the assumption of relatively stable average roughness. Indeed, in areas of limited size, the effect of roughness can be much greater and thus affect the proposed algorithm, as illustrated in section IV-B. For each site, we considered data from one orbit with an approximately constant incidence angle. This approach notably reduced the number of images used by the change detection application but prevented errors resulting from empirical incidence angle normalization, which could change from one pixel to another and from one season to the next.

We then analyzed the Sentinel-1 data time series over a four-year period. For each station, the $I_{SSM}$ and IR values were converted to volumetric moisture as described in section III and by using the ground moisture time series data. $SSM_{min}$ and $SSM_{max}$ represent the minimum and maximum values of in situ surface soil moisture at a depth of 5 cm at a given site (m$^3$/m$^2$) as defined by the 90% confidence interval of a Gaussian distribution [57]. By defining $\mu$ and $\sigma$ as the mean and standard deviation of the ground-truth data over the study period used for this analysis, $SSM_{min}$ and $SSM_{max}$ can be computed as follows: $SSM_{min} = \mu - 1.65 \times \sigma$ and $SSM_{max} = \mu + 1.65 \times \sigma$, where 1.65 represents the 95% quantile of the standard normal distribution. It was preferred to use these quantities rather than the strict minimum and maximum values in order to eliminate outliers. In the general case of applications without ground measurements, it is possible to use soil texture maps to directly retrieve these hydrological properties through pedotransfer functions [58].

Figs. 7 and 8 compare the ground measurements with the soil moisture products estimated from Sentinel-1 data using the proposed IR and the classical $I_{SSM}$ at two soil moisture stations. Strong agreement is observed between the ground measurements and the soil moisture estimated from the two considered indices. At the Barrouta site, RMSE and R are equal to 0.034 and 0.73 and to 0.04 and 0.74 for the IR and $I_{SSM}$ approaches, respectively. At the INGC site, RMSE and R are equal to 0.06 m$^3$/m$^2$ and 0.6 and to 0.056 m$^3$/m$^2$ and 0.61 for the IR and $I_{SSM}$ approaches, respectively.

However, differences in the rate at which the soil moisture decreases after rainfall events were noted. This is probably due to the effective penetration depth of the S1 radar, which is theoretically smaller than the value of 5 cm used for the ground-truth measurements [59]. In these cases, limited differences were observed between IR and $I_{SSM}$.

Table II summarizes the results obtained with the Sentinel-1 data products using $I_{SSM}$ and IR. A strong correlation was generally found between the ground measurements and the estimations for both indices, with an RMSE typically less than 0.06 m$^3$/m$^2$ for seven of the sites. At the five stations with bare soil or low vegetation cover, the IR index provided a limited improvement in accuracy for the soil moisture estimations, as indicated by its marginally lower RMSE values. For the other three stations, which had vegetation cover dynamics, IR shows slightly poorer accuracy than with $I_{SSM}$. The proposed index does not include any correction for the influence of vegetation.

Despite the overall results of the comparisons with the actual data, which showed high precision for both indices, the IR demonstrated its potential to provide accurate estimates of soil moisture. The correlation between ground measurements and remotely sensed soil moisture estimations is generally high. Some discrepancies can be attributed to the unpredictable conditions during precipitation events, which make it difficult to detect sporadic rainfall with radar acquisitions due to the 6- or 12-day repeat cycle of the Sentinel-1 constellation.

Compared to that in the analyses proposed in sections IV-A and IV-B based on the IEM, the improvement provided by the
IR seems lower in analyses with real measurements. We retrieved approximately the same results with \( I_{SSM} \) as with \( IR \). This difference may have several explanations. First, the size of the four-year time series was likely too limited to obtain highly reliable statistics. High soil moisture radar data also tend to be noisier due to various effects, such as the temporal variations in soil roughness, which make it more difficult to reproduce the theoretical trends expected in the relationship between soil moisture and radar signal strength. At stations with temporal vegetation cover dynamics, errors may be more important, particularly during the wet season, when a strong vegetation effect that is not corrected for in the proposed algorithm occurs. At stations located in West Africa, the application context in semi-arid areas could generate volume scattering on the driest dates [10] and high vertical soil moisture profile heterogeneity [59], which are also a source of errors in the application of the change detection technique.

The analysis of a relatively restricted database (4 years) does not allow us to observe the trends within each range of soil moisture (0-0.1 m\(^3\)/m\(^3\), 0.1-0.2 m\(^3\)/m\(^3\), 0.2-0.3 m\(^3\)/m\(^3\)) with precision. Table III illustrates the RMSE observed for each site. The differences between the \( I_{SSM} \) and \( IR \) approaches are generally small.

V. CONCLUSION

A new inversion approach based on the change detection algorithm is proposed for the remotely sensed estimation of SSM. This approach is based on the near linearity of the relationship between backscattered radar signals and the logarithm of the Fresnel coefficient, which has been confirmed through the use of backscattering simulations based on the \( IEM \). We thus introduce a new reflectivity index, \( IR \), which ranges in value between 0 and 1. An index value of zero corresponds to the lowest value of the radar signal time series and thus to the driest conditions. An index value of 1 corresponds to the strongest radar signals and thus to the wettest conditions. \( IEM \) simulations of a series of radar signals with added noise, expressed as a function of soil moisture, confirmed the potential improvements that can be achieved with this index compared to the classical \( I_{SSM} \), which assumes that the backscattered radar signals vary linearly as a function of soil moisture. In these simulations with constant roughness condition, the RMSE decreased from 0.055 m\(^3\)/m\(^3\) to 0.023 m\(^3\)/m\(^3\) when this new index was used. With introduction of roughness variation in \( IEM \) simulations, the RMSE decreased from 0.067 m\(^3\)/m\(^3\) to 0.038 m\(^3\)/m\(^3\) when \( IR \) was used.

The proposed algorithm was validated using Sentinel-1 data recorded over three study regions (Banizombou, Merguellil, Occitania). Eight ground moisture stations (five with bare soil or low-density vegetation cover and three with agricultural landscapes showing temporal vegetation change) were used for this validation. For each station, when the \( IR \) was converted to volumetric moisture, it was found to be strongly consistent with ground measurements, with RMSEs of less than 0.06 m\(^3\)/m\(^3\) for seven of the eight stations. When compared to the classical \( I_{SSM} \), which assumes a linear relationship between soil moisture and radar signals, we observed almost the same precision with \( IR \), with a slight improvements at stations with bare soils. This result is very encouraging, and we expect that even more robust results could be obtained with a longer time series. In the future, a more global analysis that considers the effect of vegetation cover will be performed.

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Jerome Demarty received his PhD degree from the Paris Diderot University (France) in 2001. He has been working for 12 years as researcher for the French Institute of Research for the development (IRD, France), at the HydroSciences Montpellier laboratory. He is specialized in ecohydrology, surface modeling and remote sensing, especially on Sahelian and Mediterranean ecosystems.

Sekhar Muddu received the Ph.D. degree from the Indian Institute of Science, Bangalore, India in 1993 in the area of hydrology & water resources. Since 1994, he is with Department of Civil Engineering, Indian Institute of Science and currently he holds the position of Professor. He is also member of the scientific team of the Indo-French Cell for Water Sciences at IRS. His main research interests are on analysis, modeling & process understanding of groundwater systems, satellite hydrology. He is collaborating with interdisciplinary teams on integrated hydrological and geochemical catchment experiments and is a leading member of the Kabini CZO and AMBHAS observatory.
Fig. 1. Studied sites (Banizombou (Niger), Merguellil (Tunisia), Occitania (France))

Fig. 2. Relationship between backscattering IEM simulations and soil moisture for different $Z_s$ (roughness parameter) levels

Fig. 3. Relationship between backscattering IEM simulations and log(R) for different $Z_s$ (roughness parameter) levels

Fig. 4. IEM-simulated series for soil moisture ranging between 0 m$^3$/m$^3$ and 0.4 m$^3$/m$^3$, a rms height equal to 0.8 cm, and a correlation length equal to 6 cm.

Fig. 5. Comparison between the input (actual) soil moisture used for the IEM simulations with constant roughness and the soil moisture estimations computed using two different indices: a) $l_{SEM}$ and b) IR.

Fig. 6. Comparison between the input (actual) soil moisture used for the IEM simulations with variable roughness and the soil moisture estimations computed using two different indices: a) $l_{SEM}$ and b) IR.
Fig. 7. Surface soil moisture estimations derived using the \textit{I}_{\text{SM}} and IR products compared with \textit{in situ} measurements of soil moisture at the Barrouta site.

Fig. 8. Surface soil moisture estimations derived using the \textit{I}_{\text{SM}} and IR products compared with \textit{in situ} measurements of soil moisture at the INGC site.

### Table I
RMSE (m$^3$/m$^3$) BETWEEN ESTIMATIONS BASED ON IEM SIMULATIONS AND SOIL MOISTURE INPUTS FOR THE I$_{\text{SM}}$ AND IR ALGORITHMS FOR DIFFERENT SOIL MOISTURE RANGES AND ROUGHNESS CONDITIONS

<table>
<thead>
<tr>
<th>Soil moisture range (m$^3$/m$^3$)</th>
<th>Constant roughness condition</th>
<th>Variable roughness condition</th>
</tr>
</thead>
<tbody>
<tr>
<td>\textit{I}_{\text{SM}}</td>
<td>\textit{IR}</td>
<td>\textit{I}_{\text{SM}}</td>
</tr>
<tr>
<td>0-0.1</td>
<td>0.043</td>
<td>0.007</td>
</tr>
<tr>
<td>0.1-0.2</td>
<td>0.067</td>
<td>0.012</td>
</tr>
<tr>
<td>0.2-0.3</td>
<td>0.057</td>
<td>0.021</td>
</tr>
<tr>
<td>0.3-0.4</td>
<td>0.025</td>
<td>0.035</td>
</tr>
</tbody>
</table>

### Table II
RMSE AND R FOR SURFACE SOIL MOISTURE (M$^3$/M$^3$) COMPUTED USING \textit{I}_{\text{SM}} AND IR FOR ALL SITES

<table>
<thead>
<tr>
<th>Site</th>
<th>RMSE (m$^3$/m$^3$)</th>
<th>R</th>
<th>RMSE (m$^3$/m$^3$)</th>
<th>R</th>
</tr>
</thead>
<tbody>
<tr>
<td>BZ1 (Niger)</td>
<td>0.019</td>
<td>0.81</td>
<td>0.018</td>
<td>0.82</td>
</tr>
<tr>
<td>BZ2 (Niger)</td>
<td>0.025</td>
<td>0.81</td>
<td>0.022</td>
<td>0.81</td>
</tr>
<tr>
<td>Bouhajla (Merguellil)</td>
<td>0.031</td>
<td>0.66</td>
<td>0.03</td>
<td>0.67</td>
</tr>
<tr>
<td>Barrage (Merguellil)</td>
<td>0.061</td>
<td>0.5</td>
<td>0.054</td>
<td>0.52</td>
</tr>
<tr>
<td>Barrouta (Merguellil)</td>
<td>0.04</td>
<td>0.74</td>
<td>0.034</td>
<td>0.73</td>
</tr>
<tr>
<td>INGC (Merguellil)</td>
<td>0.056</td>
<td>0.61</td>
<td>0.06</td>
<td>0.6</td>
</tr>
<tr>
<td>Mouthoumet (France)</td>
<td>0.048</td>
<td>0.42</td>
<td>0.05</td>
<td>0.41</td>
</tr>
<tr>
<td>Narbonne (France)</td>
<td>0.069</td>
<td>0.06</td>
<td>0.07</td>
<td>0.05</td>
</tr>
</tbody>
</table>

### Table III
RMSE FOR SURFACE SOIL MOISTURE (M$^3$/M$^3$) COMPUTED USING \textit{I}_{\text{SM}} AND IR FOR EACH SITE AND FOR EACH RANGE (0-0.1, 0.1-0.2, 0.2-0.3)

<table>
<thead>
<tr>
<th>Site</th>
<th>0-0.1</th>
<th>0.1-0.2</th>
<th>0.2-0.3</th>
</tr>
</thead>
<tbody>
<tr>
<td>BZ1</td>
<td>0.019/0.018</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>BZ2</td>
<td>0.025/0.022</td>
<td>0.017/0.019</td>
<td>-</td>
</tr>
<tr>
<td>Bouhajla</td>
<td>0.030/0.028</td>
<td>0.057/0.05</td>
<td>-</td>
</tr>
<tr>
<td>Barrage</td>
<td>0.056/0.04</td>
<td>0.067/0.038</td>
<td>-</td>
</tr>
<tr>
<td>Barrouta</td>
<td>0.045/0.052</td>
<td>0.040/0.047</td>
<td>-</td>
</tr>
<tr>
<td>INGC</td>
<td>0.038/0.026</td>
<td>0.044/0.05</td>
<td>0.10/0.1</td>
</tr>
<tr>
<td>Mouthoumet</td>
<td>-</td>
<td>0.042/0.06</td>
<td>0.051/0.036</td>
</tr>
<tr>
<td>Narbonne</td>
<td>-</td>
<td>0.069/0.049</td>
<td>0.066/0.08</td>
</tr>
</tbody>
</table>