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# Labelled Object Velocimetry: Simultaneous Measurements of Bubble Size and Velocity

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## Abstract

This paper presents labelled-object velocimetry (LOV) - a technique to determine the velocities of labelled objects in multiphase flow. LOV is based on spatial correlations similar to those used in particle-image velocimetry (PIV) but employs grey-level shadowgraph images to determine object velocities. Object detection and labelling are performed using a classical image-processing algorithm. In contrast to PIV, interrogation areas in LOV are not uniformly distributed. Instead, these areas surround objects, and therefore, depend on object positions and sizes. Additionally, the proposed technique recalls a previously developed algorithm [1] to distinguish between single bubbles and complex situations, such as overlays, breakups and coalescences. This algorithm-based object selection (ABOS) provides a statistically reliable sample of the entire bubble swarm in terms of size and shape. Although both techniques are completely independent, they can be combined to link object velocities to their geometrical characteristics. Thus, the LOV technique can be used to ascertain velocity-object-diameter histograms.

*Keywords:* Object Labeling ; Sum of Absolute Differences (SAD) ; Bubble Dynamics ;

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\*Fully documented templates are available in the elsarticle package on CTAN.

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## 1. Introduction

The information regarding bubble velocities associated with bubble size constitutes a crucial aspect of investigations, especially those concerning bubble columns widely used in chemical and biochemical industries. Bubble-induced hydrodynamics, which significantly influences the mass transfer and mixing abilities of multiphase flows, depends on bubble characteristics. However, acquisition of reliable experimental data requires precise measurements to be performed under practical operating conditions, wherein the bubble size may show large distribution. To this end, the use of non-intrusive techniques is being actively investigated, and several articles dedicated to their development can be found in literature. One of the simplest nonintrusive techniques involve following a demarcation line between the bubble and liquid zones upon completion of gas injection to estimate the overall swarm velocity [2]. Unfortunately, this method modifies the flow hydrodynamics drastically. Additionally, it is more applicable to steady flows with homogeneous spread in the bubble-column section. The past few decades have witnessed development of more sophisticated laser-based methods. In the 1970s, researchers [3] used laser Doppler anemometry (LDA), which is based on light scattering, or the Doppler Effect [4] to investigate bubble dynamics. More recently, an LDA-based technique was applied to rising microbubbles with dimensions up to  $100\ \mu m$  [5]. The LDA technique has also been extended to develop phase Doppler anemometry (PDA) based on refraction of light through one or more additional photo detectors. A major advantage of the PDA technique is its high data-acquisition rate, especially for turbulence statistical analysis. Nevertheless, applications of both LDA and PDA are limited to single-point measurements and spherical seeding particles. This implies that in cases involving gas-liquid flows in water without surfactants, use of these techniques is limited to bubble sizes (as tracer) of up to  $1\ mm$  [6]. Thus, in applications involving large, non-spherical, and deformable objects, particle tracking velocimetry (PTV) via high-speed CCD cameras is generally employed. Such optical methods facilitate investigation of two-phase

flows in cross-sectional planes illuminated by a sheet of laser light or volumetric projection if backlighting is used. Several PTV techniques have been developed to perform bubble identification between two consecutive images by determining geometric similitudes [7]. In this case, velocity calculations can be performed  
35 based on either the geometric centre [8], centre of a projected ellipse [9]; [10], contour [11] or use of the front-tracking method also applicable to numerical data [12]. All tracking techniques are limited by comparable disadvantages. When using the front-tracking approach, errors may be incurred in cases involving large deformable bubbles or overlays of multiple bubbles rising at different  
40 velocities. Likewise, the geometric centre technique is limited to flows involving small bubbles owing to errors induced in the calculation of the geometric centre location caused by the viewing angle and bubble deformation. Another technique-bubble image velocimetry (BIV)-inspired by particle image velocimetry (PIV) has been proposed [13] [14]. BIV estimates velocity fields with uni-  
45 formly distributed vectors using bubbles, or more precisely, the flow texture of a dense bubble swarm, instead of seeding particles, inside interrogation areas. In addition, it employs backlight instead of laser light for illumination. In a recent study [15], this method was applied to investigate bubble trajectories inside jet bubbling reactors. However, a major limitation of this method can be observed  
50 when analysing heterogeneous flows. If the interrogation area contains several bubbles with different velocities, the vector obtained represents the mean displacement or the centroid of the displacement probability density function rather than individual velocities of each object. In cases involving high field-of-view depth and large velocity variance between different flow planes, significant errors  
55 may be induced. In statistical approaches wherein object velocities are linked to their geometrical parameters, this problem can be addressed by performing algorithm-based object selection (ABOS). The labelled-object velocimetry (LOV) technique presented in this study is based on one such algorithm reported in an extant study [1]. The said algorithm uses bubble properties, such  
60 as size, eccentricity, and solidity. Another weakness of the BIV approach is that generation of large dark regions can be observed if the bubble size is very large

compared to the interrogation area. It is well acknowledged that presence of an insufficient number of grey levels causes correlation functions to become noisy, which in turn, leads to attainment of inaccurate results. To the best of the authors' knowledge, the proposed method is the first of its kind to facilitate precise velocity measurements for all kinds of detected objects irrespective of their size or shape. The proposed digital image-processing technique can be adapted for the analysis of highly polydispersed flows. In addition, the proposed method can be combined with any algorithm capable of characterizing object geometries, such as machine-learning algorithm reported in [16] [17], thereby enabling simultaneous measurement of object size and geometry. Because the proposed technique does not involve particle tracking, no comparison of geometrical characteristics is required between frames. The velocity is directly calculated on the correlation function and no object identification is performed for the second frame. This has the advantage that the velocity-calculation remains unaffected if additional objects appear in the correlation field. One major advantage of this method is that underlying velocity calculations are based on the absolute difference function squared ( $ADF^2$ ) approach developed by the observational astronomy community.  $ADF^2$  is clearly superior to the Fast Fourier Transform (FFT)-based correlations concerning noise [18]. Thus, velocities of all particles - deformed, asymmetric, or distorted - can be estimated using the proposed approach owing to no comparison of their shapes between consecutive images. For example, the proposed LOV method was applied to a case involving bubbly flows with low void fractions ( $< 1\%$ ) and heterogeneous distributions (in terms of both size and velocity). High-speed as well as classical PIV cameras in the double-frame mode can be used with backlight to enhance contrast between captured phases. Additionally, the proposed technique can be employed at any acquisition frequency provided the time interval between image pairs is short.

## 2. Data Treatment Development of Labeling, LOV & ABOS for simultaneous Velocity and Size Measurements

This section describes details concerning the data-processing strategy followed in this study. This strategy was divided into three independent parts. The first part involves performing basic image processing, wherein only the first frame of each image pair is treated and binarised for object detection and labelling. The second frame is subjected to a correlation-based blind research. The image-processing step serves for two purposes - (i) extracting interrogation-area positions and sizes for performing LOV and (ii) calculating values of geometrical parameters for ABOS. The second part of the data-processing strategy provides details regarding operating principles of the LOV technique. It includes the process for obtaining velocity vectors for each object type, thereby generating a shadow on the camera and independently of its nature. Plus, the precision realized via the use of the proposed technique is discussed. In the third part, the ABOS developed and reported in a previous study [1] is recalled. ABOS is capable of distinguishing between single or well-identified bubbles (WIBs) and so-called complex situations (CS). In the context of this study, instances of bubble overlay, coalescence and breakup are considered as complex situations. It is noteworthy that LOV and ABOS are independent of each other. However, combining both techniques (as described in section 3) can link object parameters, such as size and eccentricity, to corresponding object velocities. Thus, a large number of individual bubbles can be characterized as representative samples, and the swarm dynamics problem can be statistically analysed.

*Image Treatment for Labeling.* To label and distinguish each object that generates a continuous shadow (convex object), it is necessary to extract its position coordinates from the first frame of captured shadowgraph image pairs. To this, a classical image-processing technique was applied in this study. Per this technique, raw grey-level images (Fig. 1a) were transformed into binarised ones (Fig. 1d). Figure 1a depicts a magnified ( $700 * 860 px$ ) view of a raw shadowgraph image of bubbly flow. Non-homogeneities due to LED background lighting were

removed by capturing a flat image (i.e. an image of the acquisition-window  
 120 background sans any bubbles). Each captured shadowgraph image was divided  
 by the flat image. Consequently, the grey-level intensity of the resulting image  
 was multiplied by the average value of the flat image. Subsequently, a grey-level  
 filter was used to enhance the contrast further, thereby generating the final bi-  
 125 narisised image (Fig. 1b). The grey-level filter weights the relationship between  
 input and output values to yield a darker output via application of the following  
 equation instead of a linear function:

$$GL_{Out} = \frac{\max(GL_{In}) * GL_{In}^{1/\sigma}}{\max(GL_{Out})} \quad (1)$$

where  $GL$  denotes grey level. In this study, the value of  $\sigma$  was set as 2; how-  
 ever, this value can be increased further to weight darker pixels. The parameter  
 $\max(GL_{Out})$  depends on the colour depth of captured images and equals 256  
 130 for 8-bit images.

To determine the gas-liquid interface location, a grey-level-gradient thresh-  
 old of 0.6 was applied. Pixels with grey levels below this value were considered  
 corresponding to the gas phase, whereas those with higher grey levels were  
 considered to correspond to liquids. Thus, as already stated, frame 1 of each  
 135 image pair was binarised, as depicted in Fig. 1c, wherein black and white pixels  
 correspond to liquid and gas phases, respectively. The last image-processing  
 step comprised hole filling, wherein each white pixel was dilated isotropically  
 by one pixel to close possible interface gaps. Subsequently, objects were filled  
 with white pixels before being eroded isotropically by one pixel to attain their  
 140 initial dimensions. The final binarised image of frame 1 (Fig. 1d) was then  
 used for extracting labelled-object characteristics, such as position coordinates  
 (those corresponding to the smallest possible rectangle surrounding the object)  
 for LOV. In addition, solidity ratios were calculated, and ellipse projection was  
 performed to obtain further information, such as eccentricity or orientation an-  
 145 gle, for ABOS [1]. No labelling was performed on frame 2 of the captured  
 image pairs, because object velocities were determined using correlation func-

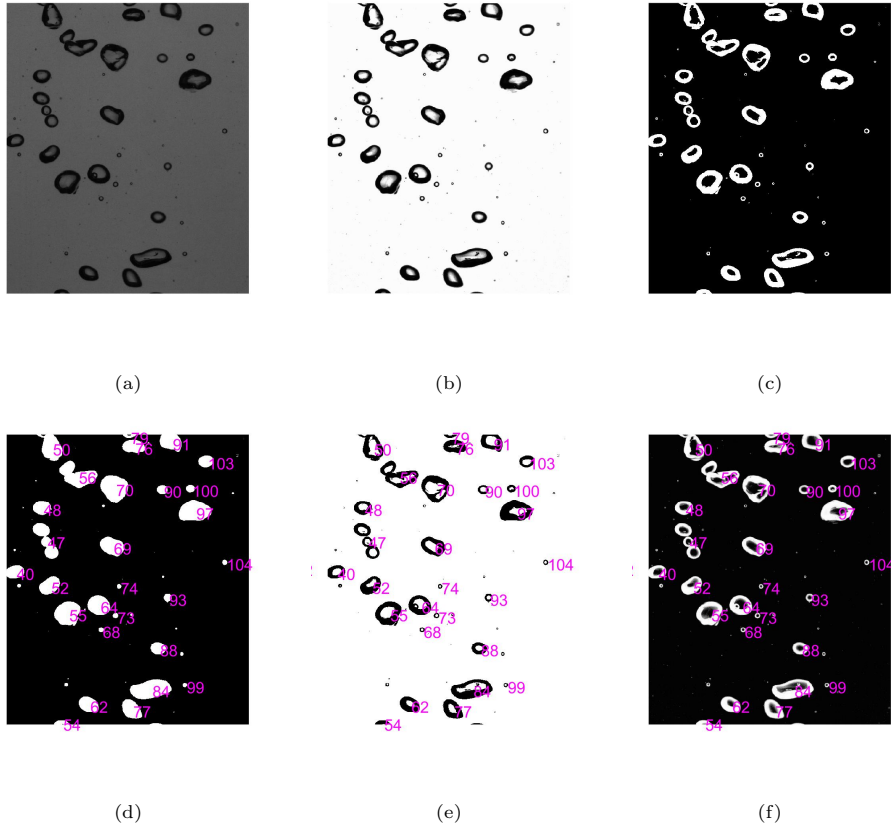


Figure 1: Water - Membrane Sparger -  $100\frac{1}{h}$ : Zoom on a) Raw Image b) Light Filtered Image c) Binarized Image d) Final Binarized Image e) Grey Level Image with Labeling f) Inverted Grey Level Image with Labeling



tions and not via geometrical similarity parameters. However, the said velocity calculations (section 2.2) require use of grey-level images. Therefore, all labels depicted in Fig. 1d were projected onto frame 1 from Fig. 1b, thereby providing  
150 a grey-level image with required labelling (Fig. 1e). As a final step, black and white gradients on grey-level images must be inverted to obtain Fig. 1f, thereby saving computational time in cases where the camera captures more liquid than gas.

*Velocity Calculation on Grey Level Images.* Double-frame acquisition performed  
155 in LOV is similar to that in PIV. Likewise, the application of spatial correlation to image pairs separated by short time intervals is also similar in both techniques. The main difference between LOV and PIV concerns interrogation areas, the assigning of a velocity vector to each of them, and corresponding correlation functions. PIV or BIV [13] images are usually divided into uniformly  
160 distributed interrogation areas based on seeding-particle density, whereas the number and size of interrogation areas in LOV images depend directly on the number and size of labelled objects. In this regard, the LOV technique can be considered equivalent to a Lagrangian approach with interrogation areas surrounding each object.

165 As aforementioned, coordinates of the smallest possible rectangles surrounding each labelled object were extracted from frame 1 of binarised image pairs and projected onto frame 1 of inverted grey-level ones, as described in Fig. 2 (left). Notably, spatial correlations must be applied exclusively to raw or grey-level images and not binarised ones. Grey-level gradients observed at bubble interfaces  
170 facilitate seamless inter-correlation. The observed large spread of grey levels makes the correlation more efficient compared to PIV images, wherein most pixels are dark. However, correlation fields in LOV are obtained by scanning (extending) interrogation areas comprising a large yet identical number pixels in all directions around the initial object position (centre of the rectangle around  
175 an object). Thus, the scan size represents a compromise. This is because on one hand, the scan must be sufficiently large to capture the object in the second

frame, and hence, it must be defined by the maximum object velocity in the dispersed phase. On the other hand, the scan must be small enough to prevent appearance of other objects within the correlation field. In this way, potential  
 180 object mix-ups, and consequently, erroneous velocity-vector calculations can be avoided. In the present study, a scan length of 11 *px* along each direction was considered sufficient to obtain valid velocity vectors. In accordance with the scale (0.1 *mm* with  $\Delta t = 2ms$ ) used in this study, an 11-pixel scan length represents a maximum velocity of 0.55*m/s*. Nevertheless, a safety measure was  
 185 included in the correlation process. For displacement equal to or exceeding 10 *px*, the interrogation area was moved by the same number of pixels along a velocity-vector component before performing a second spatial correlation. In this case, the final vector would correspond to the resultant of the first and second vectors.

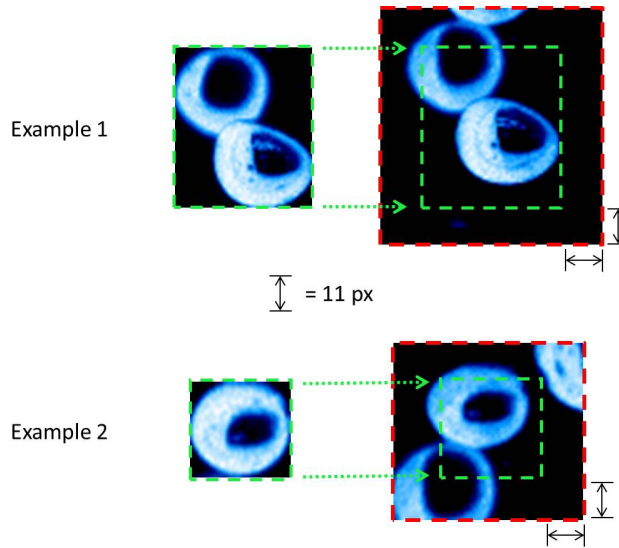


Figure 2: 2 Examples of Double Frame Image Pairs - Left: Frame 1 with the smallest possible Rectangle surrounding the Object ; Right: Frame 2 with the Projection of the Rectangle from Frame 1 + Scan of 11 *pixels*

190 The velocity-calculation process can be divided into two parts. The first part involves use of a spatial correlation. In this study, the absolute difference

function squared ( $ADF^2$ ) approach based on the sum of absolute differences ( $SAD$ ) was preferred owing to its adequate accuracy and fast calculation [18]. The correlation function can be expressed as:

$$ADF^2 = \left( \sum_{x,y} |g(x,y) - g_{ref}(x+i, y+j)| \right)^2 \quad (2)$$

195 where  $g$  denotes the interrogation area in frame 1;  $g_{ref}$  denotes correlation field in frame 2;  $x$  &  $y$  denote the horizontal and vertical grid positions, respectively; and  $i$  &  $j$  denote the horizontal and vertical pixel shifts, respectively. The interrogation area  $g$  from frame 1 is moved one pixel at a time inside  $g_{ref}$  in frame 2 ( $(i, j) \in [-scan, scan]$ ). At every position equation 2 was applied  
 200 to all pixels within  $g$  and  $g_{ref}$  for all pixel shift values  $i$  and  $j$  to obtain the final correlation function for each individual pixel. The said final function has constant size of  $23 * 23 px$  ( $(2 * scan + 1) * (2 * scan + 1)$ ). This constitutes the main difference between the LOV and PIV approaches. Whereas FFT-based correlations are applied to fixed interrogation areas in PIV,  $ADF^2$  correlations  
 205 applied to larger interrogation areas are used in LOV to minimize noise, as reported in [18]. The authors investigated the intensity mismatch (bias), image noise, shift, and root mean square (RMS) errors for five correlation methods and four interpolation algorithms applied to synthetic images with known shifts and noise levels. Based on the findings from this investigation, the authors  
 210 recommended using square difference function ( $SDF$ ) or  $ADF^2$  approaches to calculate correlation functions. The precision of the displacement calculated in this first step of velocity calculation was 1  $px$ .

The second part of the velocity calculation process comprises subpixel interpolation around the global maximum of the correlation function ( $ADF^2$ ). In  
 215 this way, the accuracy of velocity-vector calculations can be improved to subpixel levels. Author et al. [18] recommend use of the 2D least squares or 2D quadratic interpolation methods. Accordingly, the biparabolic fit corresponding to 2D quadratic interpolation was considered in this study. The said fit yields the best results when applied to  $3 * 3$ -elements of the correlation function, as

220 suggested in [19], wherein the authors explain how use of lower- and higher-  
order polynomials tend to over- and underestimate the shift, respectively. In  
addition, it must be remembered that correlation functions might not necessar-  
ily be symmetric, and one must determine the position of the maximum (and  
not median) value of the correlation function. This is another reason for con-  
225 sidering  $3 * 3$ -elements around the maximum value of the correlation function.  
Correlation functions corresponding to objects depicted in Fig. 2 are presented  
in Fig. 3. As can be observed, in the first example, the labelled object consid-  
ered does not change between frames. Hence, the obtained correlation function  
only shows a global maximum (Fig. 3), and therefore, the object velocity can  
230 be easily determined. In the second example considering the object in frame 2  
from Fig. 2 (left), another object of similar size can be observed to lie almost  
entirely within the correlation field. Accordingly, the corresponding correlation  
function (Fig. 3) is characterised by two maxima—global and local. This exam-  
ple helps one appreciate the superiority of the use of LOV technique compared  
235 to tracking methods that require both image frames captured to be geometri-  
cally similar. When using LOV, the appearance of additional bubbles in the  
correlation field causes additional peaks to appear in the correlation function.  
However, the velocity-calculation remains unaffected because the correlation  
function obtained is characterized by a clear global maximum corresponding to  
240 the labelled object obtained from frame 1. Thus, objects in frame 2 need not  
be identified as overlays of multiple bubbles, and no object separation needs  
to be performed. It is noteworthy to mention that the greater the similarity  
between objects the higher is the resulting correlation function. Therefore, the  
time interval considered ( $\Delta t = 2ms$ , as considered in this study) must be short  
245 enough to avoid distortions. The final displacement between the centre of the  
interrogation area and correlation maximum is indicated by an arrow, as de-  
picted in Fig. 3. Thus, knowing the time interval between captured frames, an  
object’s velocity can be easily deduced.

The proposed method can be applied to all connected objects in an image  
250 pair, thereby yielding a velocity map similar to that shown in Fig. 4. Inde-

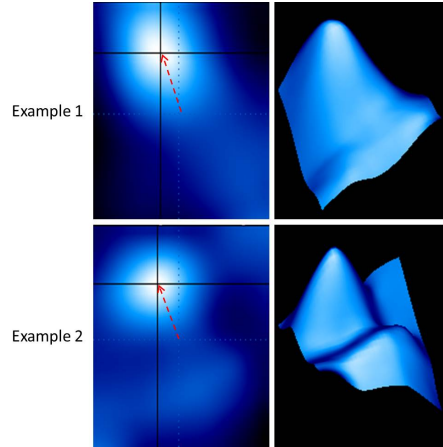


Figure 3: Left: 2D Correlation Function ; Right: 3D Correlation Surface (all Scans show a Size of  $23 * 23$  pixels)

pendent of its nature—single, coalescing, breaking, or overlapping—each object (bubble) detected and labelled in frame 1 of a captured image pair can be represented by an arrow indicating the direction and magnitude of its velocity.

The uncertainty of velocity measurement depends on the estimation of the  
 255 subpixel position of the correlation function’s maximum. As reported in [19],  
 subpixel precision corresponds to the inverse of scan width. In this study, this  
 width equalled  $23 \text{ px}$  ( $11 \text{ px}$  along all directions around the labelled object),  
 thereby yielding a shift accuracy of  $\frac{1}{23}$  times a pixel. It is important to note here  
 (as well as when using PIV) that velocity uncertainty is absolute irrespective of  
 260 the magnitude of the velocity vector. In the present case, one pixel corresponds  
 to  $0.1 \text{ mm}$ , and given the time interval of  $2 \text{ ms}$  between capturing of successive  
 image pairs, a shift accuracy of  $\frac{1}{23}$  times a pixel yields an absolute uncertainty  
 of  $0.22 \text{ mm/s}$ . Thus, the precision as well as the entire velocity-calculation  
 process is independent of object size and shape. In addition, it must be realized  
 265 that when the correlation function becomes too wide, another limitation on its  
 accuracy appears owing to flatness around the observed maximum. However,  
 the correlation function usually maintains a good height-to-width (aspect) ratio

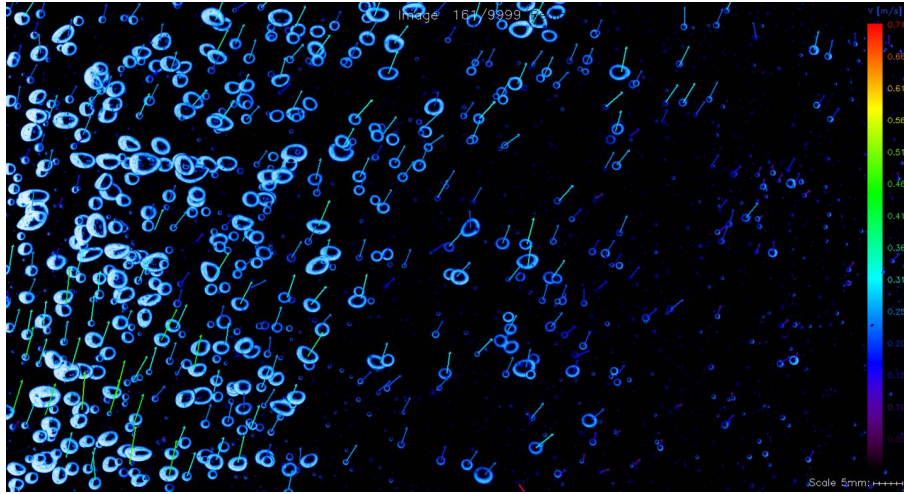


Figure 4: Example of a Velocity Field obtained via LOV without object selection (without ABOS)

because  $ADF^2$  performs a summation of grey levels of all pixels inside the interrogation area (equation 2). This property is further enhanced by the large spread of grey levels induced by the gas-liquid interface. Assuming a  $5 * 5 \text{ mm}$  ( $50 * 50 \text{ px}$ ) interrogation area, each point on the  $ADF^2$  correlation function is the result of  $50 * 50$  times the absolute difference and  $50 * 50$  times the sum, corresponding to  $N_{sum} = (50 * 50)^2$ . Considering camera-induced noise being random, correlation function's noise can be subsequently reduced by a factor of  $\sqrt{N_{sum}} = 50 * 50$ . Thus, the correlation function becomes extremely smooth by a factor equal to the number of pixels in the initial interrogation area. Hence, the height of the correlation function corresponding to a  $5\text{-mm}$  ellipsoidal bubble (refer example 2 in Fig. 2) significantly exceeds its width, as shown in Fig. 3. Moreover, none of the objects considered in this study were even close to being large enough (up to  $40 \text{ mm}$ ) to match this upper limit of the correlation function induced by the maximum's flatness.

*Bubble Identification on Binarized Images.* As already mentioned in preceding sections, a velocity vector corresponding to each labelled object in frame 1 of

an image pair was obtained in this study independent of the object’s nature.

285 This section describes how ABOS can be performed to separate single or well-identified bubbles (WIBs) from complex situations (CS) involving overlaying, coalescing, and/or breaking bubbles. Thus, it is possible to consider data only from individual bubbles to link their characteristics to corresponding velocity vectors for statistical analysis. To this end, object parameters, such as their

290 size (defined as diameter  $DE$  of an equivalent sphere), eccentricity, orientation (angle between the horizontal and major axis of a projected ellipse), and solidity were used. Values of these parameters can be extracted from corresponding binarised images (Fig. 1d) after performing ellipse projection for each labelled object. ABOS aims to obtain a statistically reliable sample representative of

295 the entire bubble swarm. The filter strategy presented in Fig. 5 was used for this purpose. The first step in this regard involved ensuring the object is not intersected by image borders. Subsequently, solidity was considered as the first filtering parameter, the threshold value of which varies with object size—from 0.97 (for small bubbles) to 0.9 (for large bubbles). Likewise, eccentricity was

300 considered the second filtering parameter for objects with equivalent diameters measuring less than  $7.5\text{ mm}$ . For larger objects, their orientation was considered the second filter. In this manner, all objects were categorized as either WIB (ellipsoidal bubbles and spherical caps) or CS. For further details, readers may please refer [1]. With the certainty to consider objects as WIBs exclusively, one

305 linked object velocities to their geometric parameter, in particular, their size. Thus, by combining the techniques presented in sections 2.2 and 2.3 with a large number of WIBs, statistical data analyses of complete bubble-flow dynamic could be performed.

### 3. Examples of Application

310 Two bubbly-flow scenarios were considered in this study to demonstrate the performance of the proposed LOV technique. Both cases were investigated in a pseudo two-dimensional bubble column described in section 3.1. The first case

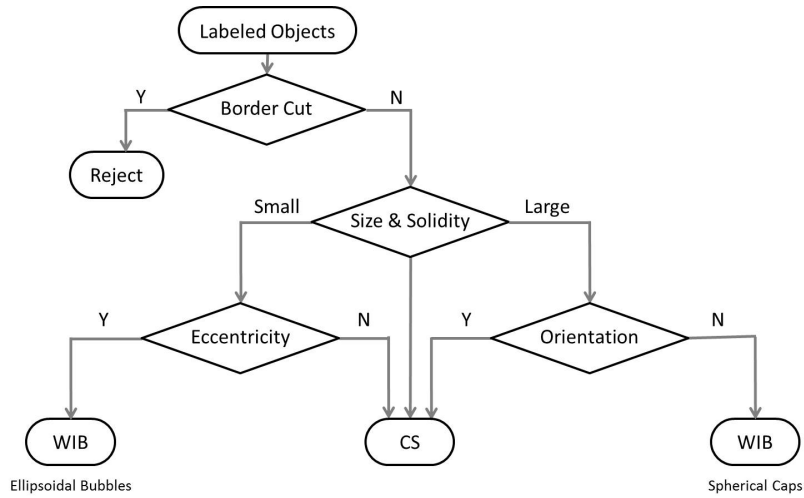
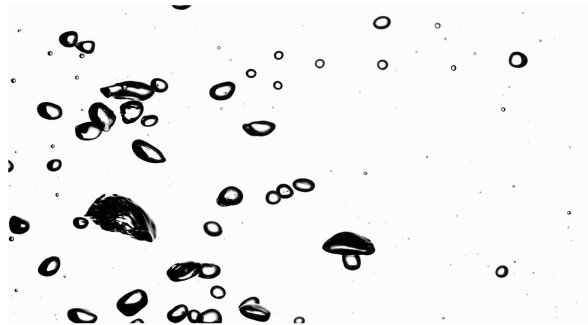


Figure 5: ABOS Filter Strategy for Bubble Identification out of Labeled Objects ; Y = Yes ; N = No ; WIB = Well Identified Bubble ; CS = Complex Situation

involves an oscillating bubble plume with ellipsoidal  $100\text{ l/h}$  bubble injection in water using a membrane sparger. The oscillating plume can also be categorized as vortical flow [20], and it is characterised by a heterogeneous velocity distribution. A shadowgraph image of the acquisition window captured under said flow conditions is depicted in Fig. 6a. The second example corresponds to a bubble jet with spherical-cap injection at  $50\text{ l/h}$  in liquid B5 (with 100 times the viscosity of water) using a slugflow sparger. Bubbles were observed to rise along the centre of the column. The said bubbles remained isolated and did not form a bubble swarm (refer Fig. 6b). The observed flow structure can be considered to correspond to double-cell transition flow [20], and no low-frequency oscillations were observed. This case was considered owing to its bimodal size distribution.

*Experimental Setup.* As stated above, experiments in this study were performed using a pseudo two-dimensional bubble column measuring  $0.06\text{ m}$  deep,  $0.35\text{ m}$  wide and  $2\text{ m}$  high, thereby allowing the capture of shadowgraph images. Details regarding the experimental setup and measurement method are presented





(a)



(b)

Figure 6: Examples of Applications: a) Water - Membrane Sparger -  $100 \frac{l}{h}$  ; Vortical Flow b) Breox (24%) - Slugflow Sparger -  $50 \frac{l}{h}$  ; Double Cell Transition Flow

in a previous study [1]. Figure 7 depicts a sketch of the experimental setup,  
330 which clearly shows the acquisition window. The  $X$ -axis represents the hori-  
zontal component. The width dimension was normalised with respect to half  
the column width, thereby causing column-wall positions to correspond to val-  
ues of  $-1$  and  $1$  on the horizontal axis with the column centreline located at  
zero. Bubble injection was performed using two different spargers located at the  
335 centre of the column bottom. Ellipsoidal bubbles or spherical caps were injected  
into the bubble column using a membrane or slugflow sparger, respectively [1].  
Water (example 1) and Breox (example 2)-a Newtonian fluid with viscosity 100  
times that of water-were considered in this study. The properties of Breox are  
listed in Table 1.

340 Images were captured using the Dantec 2M camera in the double-frame  
(PIV) mode. The image resolution was set to  $1600 * 840 px$ , which corresponds  
to  $167 * 87 mm^2$  image area. As observed in Fig. 7, the acquisition window  
was located at the centre of the liquid column measuring  $1.3 m$ , and it nearly  
covers the entire right half of the column width. To facilitate data analysis,  
345 the acquisition-window width was discretized into 70 spatial intervals of  $23 px$   
each. In both cases, the analysis was restricted to objects located inside two  
intervals around a certain point ( $X = 0.25$  or  $X = 0.07$ ). Thus, the area  
of interest measured  $46 px$  or  $4.7-mm$  wide. The field of view accounted for  
the entire column depth ( $60 mm$ ). The acquisition frequency and time interval  
350 between captured image pairs were set to  $15 Hz$  and  $2 ms$ , respectively. Because  
of low-frequency bubble-plume oscillations of period  $22 s$ , measurements were  
required to be performed over an 11-min duration to capture a sufficient large  
number of periods (30 periods corresponding to 10,000 image pairs). In this  
manner, statistically reliable data were obtained for both experiments, despite  
355 performing the initial WIB discrimination.

*Example 1: Oscillating Bubble Plume.* The first practical example considered  
in this study involved an ellipsoidal bubble plume oscillating with a period of  
 $22 s$  [21]. The plume was observed to move from one side of the liquid column

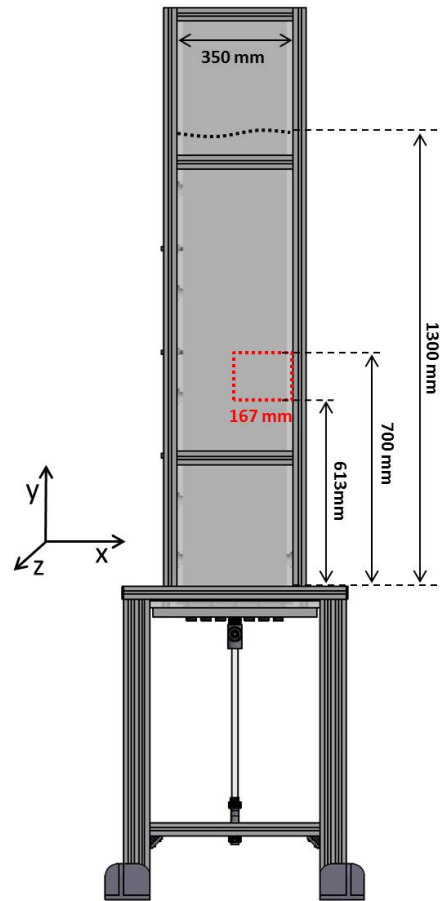


Figure 7: Experimental Setup

Fluid	Ref.	Surface Tension (mN/m)	Viscosity (mPa.s)
Water	W	75.1	1
Breox (24%)	B	55.0	100

Table 1: Fluid Properties

to another, thereby covering almost the entire column section whilst generating  
360 bimodal velocity distributions. Under the experimental conditions considered  
in this study, a low rate of coalescence was observed, and the mean bubble di-  
ameter ( $D_E$ ) equalled  $5.6\text{ mm}$  [1]. From the 10,000 image pairs captured in  
this experiment, 134,229 and 53,578 objects were identified as WIBs and CS,  
respectively, thereby corresponding to a WIB concentration of 71.5%. Thus,  
365 the WIB sample was considered statistically representative of the entire bubble  
swarm. The following analysis focuses on objects captured in two spatial inter-  
vals around  $X = 0.25$  (corresponding to a distance of  $44\text{ mm}$  from the column  
centre). This above value of  $X$  was considered because it corresponds to the  
location of the maximum value of the horizontal time-averaged void-fraction  
370 profile [22].

Moreover, the proposed LOV technique assigned a velocity vector linked to  
the equivalent diameter of each object. Use of the LOV technique facilitated  
the generation of two-dimensional histograms depicted in Fig. 8. Figures 8a  
and 8c depict observed trends in the vertical and horizontal velocity compo-  
375 nents, respectively, with respect to equivalent diameters of identified WIBs.  
As can be confirmed, the vertical velocity component demonstrates a peak at  
 $U_{vertical} \approx 0.35\text{ m/s}$  and  $D_E \approx 5\text{ mm}$ . This velocity represents the summa-  
tion of the free velocity ( $U_{vertical} \approx 0.25\text{ m/s}$ ) of an ellipsoid bubble rising in  
a quiescent liquid and mean liquid velocity ( $U_{LMEAN} \approx 0.05\text{ m/s}$  [22]) of the  
380 bubble plume. The large velocity distribution observed can be explained based  
on the oscillating-plume behaviour. Under the experimental conditions consid-  
ered in this study, liquid-velocity fluctuations at point  $X = 0.25$  (of the order of  
 $U_{LRMS} \approx 0.15\text{ m/s}$  [22]) influence the rising velocity of bubbles, thereby result-

ing in a large velocity spread. Along the horizontal direction, Fig. 8c reveals  
 385 the presence of a nearly symmetric bimodal velocity distribution created by the  
 lateral bubble-plume movement inside the liquid column. Figures 8(b) and 8(d)  
 demonstrate similar trends for CS objects. As can be observed in Figs. 8b and  
 8d, fewer CS objects were identified compared to WIBs. Moreover, the observed  
 range of CS-object size also exceeds that of corresponding with WIBs. In ac-  
 390 cordance with the hydrodynamic structure of objects considered in this case,  
 similar velocity ranges were observed for both CS objects and WIBs. Addition-  
 ally, in this case, CS objects demonstrated only overlays with no instances of  
 coalescence or breakup. These overlays comprised multiple bubbles in different  
 planes moving at nearly identical velocities, which were also similar to those of  
 395 WIBs.

This trend can be confirmed with reference to Fig. 9 that depicts size-  
 independent velocity histograms plotted along both directions. Distributions of  
 both WIBs and CS objects were normalized based on their number, and both  
 distributions are depicted in the figure. As expected, in view of the aforemen-  
 400 tioned results, both WIBs and CS objects demonstrate similar velocity trends.  
 As observed, the vertical-velocity distribution demonstrates the same rising ve-  
 locity  $U_{vertical} \approx 0.35m/s$ , whereas the horizontal component demonstrates a  
 bimodal shape with two clear peaks. The slightly higher peak observed in the  
 positive range in Fig. 9b is caused by decentralization of the measurement po-  
 405 sition towards the right. At this point, bubbles tend to move slightly further  
 away from the centre.

Clear differences between WIB and CS-object size distributions can be ob-  
 served. Figure 10 depicts equivalent-diameter histograms for WIBs and CS  
 objects normalized based on their total count. In the case of WIBs, a large  
 410 peak can be observed close to  $5\text{ mm}$ , whereas for CS objects, the correspond-  
 ing peak appears around  $7.5\text{ mm}$ . Once again, because no coalescence was  
 observed in this case, bubble overlays lead to formation of large objects. The  
 observed size difference illustrates the importance of bubble selection to avoid  
 overestimations.

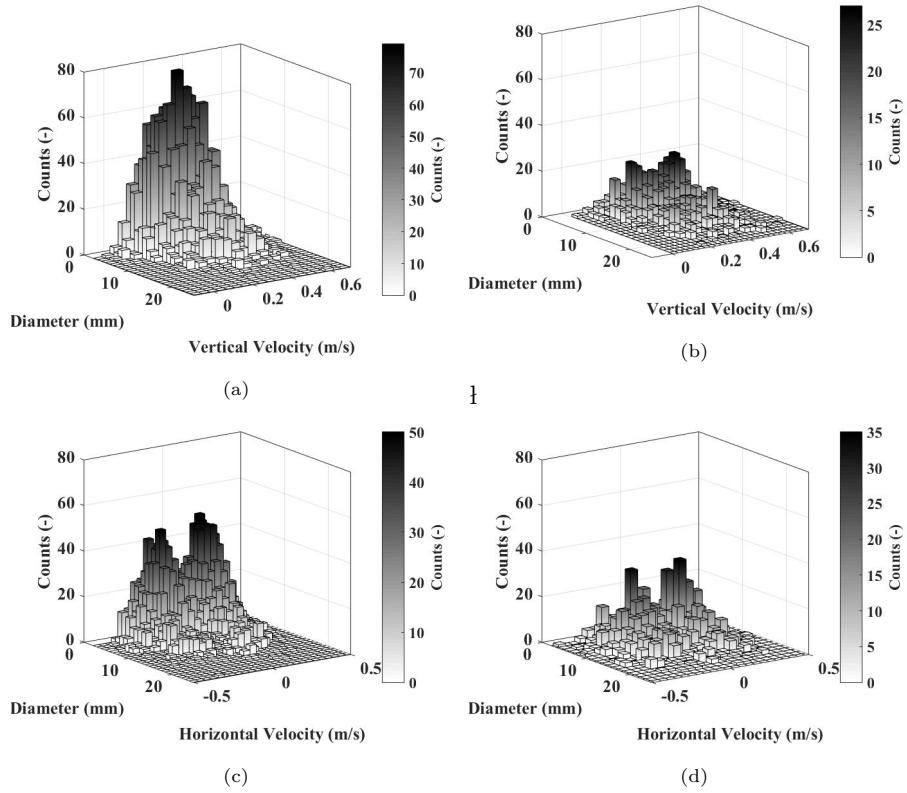


Figure 8: Water - Membrane Sparger -  $100\frac{l}{h}$ : Velocity-Diameter Histograms from measurements in point  $X = 0.25$  for the Vertical Component in the case of a) WIB and b) CS ; and the Horizontal Component and in the case of c) WIB and d) CS

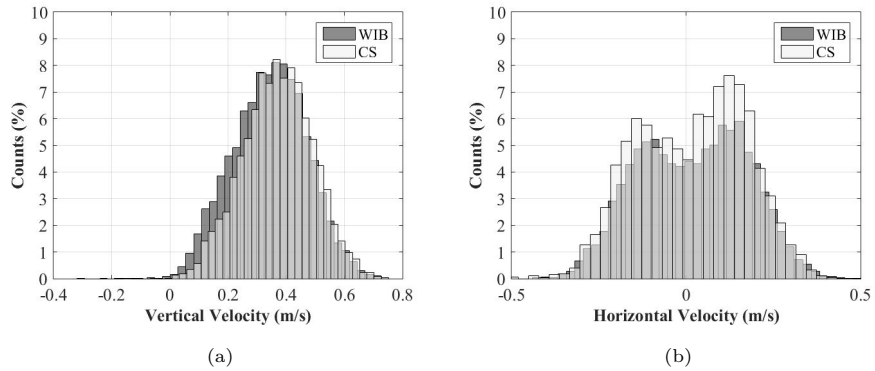


Figure 9: Water - Membrane Sparger -  $100\frac{l}{h}$ : Velocity Distributions in Point  $X = 0.25$  a) Vertical and b) Horizontal Component

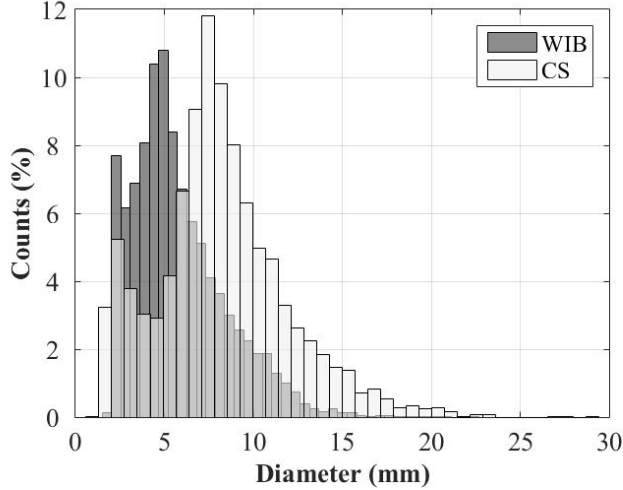


Figure 10: Water - Membrane Sparger -  $100 \frac{l}{h}$ : Bubble Size Distributions in Point  $X = 0.25$

415 *Example 2: Double Cell Transition Flow.* To demonstrate the effectiveness of  
the proposed LOV method further, its application to a second practical case  
involving WIBs exclusively (for the sake of simplicity) is presented herein. In  
this case, large bubbles were injected into a highly viscous fluid (Fluid B) using  
a slugflow sparger, thereby resulting in a non-oscillating "Double-cell Transi-  
420 tion Flow" (DCTF) [20]. Because horizontal-velocity fluctuations assume less  
importance in this case, the analysis mainly focussed on the vertical-velocity  
component. This case was primarily selected in view of its bimodal bubble-size  
distribution. Bubbles may have aspired into the wake of a large one rising in  
front of it, thereby resulting in their coalescence, which in turn, creates large  
425 spherical caps (Fig. 6b) along with a large size spread. In this case, 8,703 WIBs  
were identified out of 13,414 objects, thereby corresponding to 65% WIB con-  
centration. Bubbles were observed to rise along the centre of the liquid column,  
similar to a bubble train. Hence, the maximum value of the time-averaged hori-  
zontal void-fraction profile was observed to be located along the column centre.  
430 Accordingly, the point located at  $X = 0.07$  [22] was considered for data analysis.

Figure 11 depicts a two-dimensional histogram of the vertical velocity com-

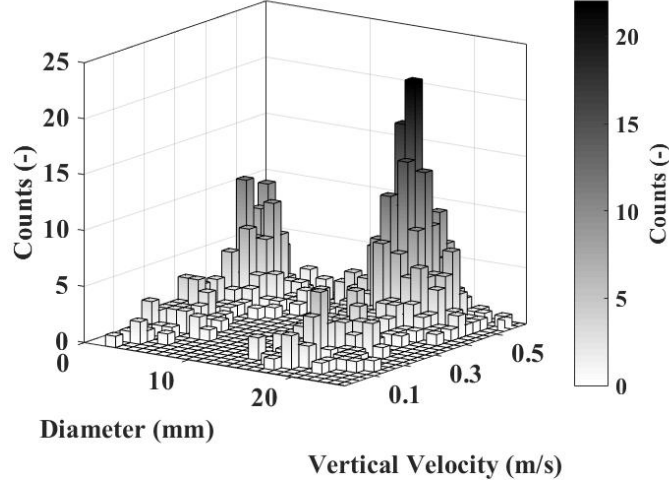


Figure 11: Liquid B - Slugflow Sparger -  $50 \frac{l}{h}$ : Velocity Size Distributions in point  $X = 0.07$  in Vertical Component

ponent with respect to the equivalent WIB diameter, and occurrence of two clear peaks—around 2 mm and around 15 mm—can be observed. These observed peaks correspond to a similar velocity value  $U_{vertical} \approx 0.45 m/s$ . This result can be confirmed with reference to Fig. 12a, wherein the global peak corresponds to the same velocity. This velocity value can be explained based on the flow structure that results in generation of the mean liquid velocity  $U_{LMEAN} \approx 0.2 m/s$  [22]. By adding the value of the free vertical velocity ( $U_{vertical} \approx 0.25 m/s$ ) of rising spherical caps in a quiescent liquid to  $U_{LMEAN}$ , the resulting value of  $U_{vertical} \approx 0.45 m/s$  can be obtained. It is noteworthy that bubbles of all considered sizes (ellipsoidal and caps) attain such high velocities (refer Fig. 12). Figure 12b illustrates the large range of bubble sizes. As can be confirmed, the first peak corresponds to ellipsoidal bubbles, whereas the second peak represents large spherical caps.



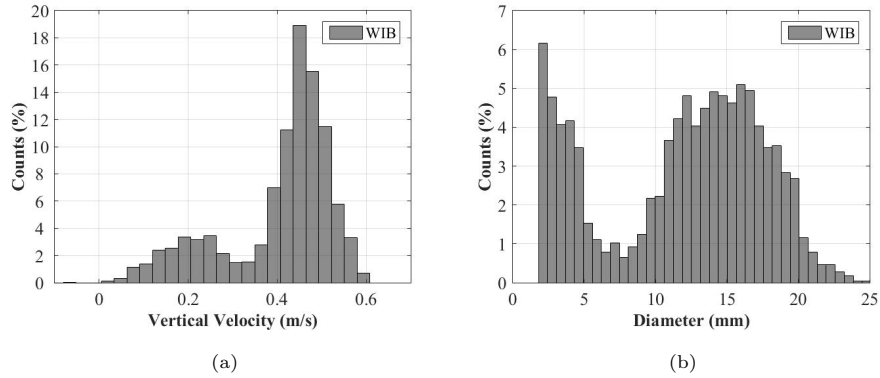


Figure 12: Liquid B - Slugflow Sparger -  $50 \frac{l}{h}$ : a) Velocity Distributions (Vertical Component) and b) Size Distribution in point  $X = 0.07$

445 **4. Conclusion**

This paper presents a Lagrangian approach, referred to as the "labelled-object velocimetry (LOV)" technique, to assign individual velocity vectors to labelled objects identified in multiphase fluid-flow scenarios. The proposed LOV technique is based on the processing of grey-level shadowgraph images with  
 450 subpixel precision. The underlying intercorrelation technique has been extensively discussed, and its realizable level of precision has been adequately demonstrated. In addition, application of an independent image-analysis method, called "algorithm-based object selection (ABOS)" has also been explained. It has been demonstrated how combining both above-mentioned approaches facilitates simultaneous measurement of bubble characteristics and individual object  
 455 velocities. In this way, the proposed study establishes a link between sizes and velocities of statistically representative samples of entire bubble swarms. The effectiveness of the proposed method has been illustrated via consideration of its application in two practical scenarios involving flow of ellipsoidal bubbles  
 460 and spherical caps.

## References

## References

- [1] D. Laupsien, C. Le Men, A. Cockx, A. Liné, Image processing for bubble morphology characteristics in diluted bubble swarms, *Physics of Fluids* 31 (5) (2019) 053306. doi:10.1063/1.5088945.  
465 URL <https://aip.scitation.org/doi/10.1063/1.5088945>
- [2] D. J. Nicklin, Two-phase bubble flow, *Chemical Engineering Science* 17 (9) (1962) 693–702. doi:10.1016/0009-2509(62)85027-1.  
470 URL <http://www.sciencedirect.com/science/article/pii/0009250962850271>
- [3] R. Mahalingam, R. S. Limaye, J. A. Brink, Velocity measurements in two-phase bubble-flow regime with laser-doppler anemometry, *AIChE Journal* 22 (6) (1976) 1152–1155. doi:10.1002/aic.690220631.  
475 URL <https://aiche.onlinelibrary.wiley.com/doi/abs/10.1002/aic.690220631>
- [4] C. P. Wang, A unified analysis on laser Doppler velocimeters, *Journal of Physics E: Scientific Instruments* 5 (8) (1972) 763–766. doi:10.1088/0022-3735/5/8/016.
- [5] G. H. Kelsall, S. Tang, A. L. Smith, S. Yurdakul, Measurement of rise and electrophoretic velocities of gas bubbles, *Journal of the Chemical Society, Faraday Transactions* 92 (20) (1996) 3879–3885. doi:10.1039/FT9969203879.  
480 URL <https://pubs.rsc.org/en/content/articlelanding/1996/ft/ft9969203879>
- [6] Z. W. Gan, S. C. M. Yu, A. W. K. Law, Hydrodynamic stability of a bubble column with a bottom-mounted point air source, *Chemical Engineering Science* 66 (21) (2011) 5338–5356. doi:10.1016/j.ces.2011.07.032.  
485

URL <http://www.sciencedirect.com/science/article/pii/S0009250911004945>

490 [7] C. A. Acuna, J. A. Finch, Tracking velocity of multiple bubbles in a swarm, International Journal of Mineral Processing 94 (3-4) (2010) 147–158. doi:10.1016/j.minpro.2010.02.001.

[8] D. Colombet, D. Legendre, A. Cockx, P. Guiraud, F. Risso, C. Daniel, S. Galinat, Experimental study of mass transfer in a dense bubble swarm, Chemical Engineering Science 66 (14) (2011) 3432–3440. doi:10.1016/j.ces.2011.01.020.

495 URL <http://www.sciencedirect.com/science/article/pii/S0009250911000303>

[9] K. Ellingsen, F. Risso, On the rise of an ellipsoidal bubble in water: oscillatory paths and liquid-induced velocity, Journal of Fluid Mechanics 440 (2001) 235–268. doi:10.1017/S0022112001004761.

500 URL <https://www.cambridge.org/core/journals/journal-of-fluid-mechanics/article/on-the-rise-of-an-ellipsoidal-bubble-in-water-oscillatory-paths-and-liquid-induced-velocity/C4D609D39DD664C8FE5903AD66805B63>

505 [10] M. Maldonado, J. J. Quinn, C. O. Gomez, J. A. Finch, An experimental study examining the relationship between bubble shape and rise velocity, Chemical Engineering Science 98 (2013) 7–11. doi:10.1016/j.ces.2013.04.050.

510 URL <http://www.sciencedirect.com/science/article/pii/S0009250913003187>

[11] R. F. L. Cerqueira, E. E. Paladino, B. K. Ynumaru, C. R. Maliska, Image processing techniques for the measurement of two-phase bubbly pipe flows using particle image and tracking velocimetry (PIV/PTV), Chemical Engineering Science 189 (2018) 1–23. doi:10.1016/j.ces.2018.05.029.

URL <http://www.sciencedirect.com/science/article/pii/S0009250918303269>

[12] J. Xue, M. Al-Dahhan, M. P. Dudukovic, R. F. Mudde, Bubble velocity, size, and interfacial area measurements in a bubble column by four-point optical probe, *AICHE Journal* 54 (2) (2008) 350–363. doi:10.1002/aic.11386.

URL <http://onlinelibrary.wiley.com/doi/10.1002/aic.11386/abstract>

[13] Y. Ryu, K.-A. Chang, H.-J. Lim, Use of bubble image velocimetry for measurement of plunging wave impinging on structure and associated greenwater, *Measurement Science and Technology* 16 (10) (2005) 1945–1953. doi:10.1088/0957-0233/16/10/009.

[14] D. Broder, M. Sommerfeld, Combined PIV/PTV-Measurements for the Analysis of Bubble Interactions and Coalescence in a Turbulent Flow, *The Canadian Journal of Chemical Engineering* 81 (3-4) (2003) 756–763. doi:10.1002/cjce.5450810356.

URL <https://onlinelibrary.wiley.com/doi/abs/10.1002/cjce.5450810356>

[15] Y. Shuai, X. Guo, H. Wang, Z. Huang, Y. Yang, J. Sun, J. Wang, Y. Yang, Characterization of the bubble swarm trajectory in a jet bubbling reactor, *AICHE Journal* 65 (5) (2019) e16565. doi:10.1002/aic.16565.

URL <https://aiche.onlinelibrary.wiley.com/doi/abs/10.1002/aic.16565>

[16] T. Haas, C. Schubert, M. Eickhoff, H. Pfeifer, BubCNN: Bubble detection using Faster RCNN and shape regression network, *Chemical Engineering Science* 216 (2020) 115467. doi:10.1016/j.ces.2019.115467.

URL <http://www.sciencedirect.com/science/article/pii/S0009250919309571>

- [17] I. Poletaev, M. P. Tokarev, K. S. Pervunin, Bubble patterns recognition using neural networks: Application to the analysis of a two-phase bubbly jet, *International Journal of Multiphase Flow* 126 (2020) 103194. doi:10.1016/j.ijmultiphaseflow.2019.103194.  
URL <http://www.sciencedirect.com/science/article/pii/S0301932219305701>
- [18] M. G. Lofdahl, Evaluation of image-shift measurement algorithms for solar Shack-Hartmann wavefront sensors, *Astronomy & Astrophysics* 524 (2010) A90. doi:10.1051/0004-6361/201015331.  
URL <http://arxiv.org/abs/1009.3401>
- [19] L. J. November, G. W. Simon, Precise proper-motion measurement of solar granulation, *The Astrophysical Journal* 333 (1988) 427–442. doi:10.1086/166758.  
URL <http://adsabs.harvard.edu/abs/1988ApJ...333..427N>
- [20] M. E. Diaz, F. J. Montes, M. A. Galán, Influence of Aspect Ratio and Superficial Gas Velocity on the Evolution of Unsteady Flow Structures and Flow Transitions in a Rectangular Two-Dimensional Bubble Column, *Industrial & Engineering Chemistry Research* 45 (21) (2006) 7301–7312. doi:10.1021/ie060466b.  
URL <http://dx.doi.org/10.1021/ie060466b>
- [21] D. Laupsien, A. Cockx, A. Line, Bubble Plume Oscillations in Viscous Fluids, *Chemical Engineering & Technology* 40 (8) (2017) 1484–1493. doi:10.1002/ceat.201600690.  
URL <https://onlinelibrary.wiley.com/doi/abs/10.1002/ceat.201600690>
- [22] D. Laupsien, Hydrodynamics, Mass Transfer and Mixing induced by Bubble Plumes in Viscous Fluids, thesis, Toulouse, INSA (Dec. 2017).  
URL <http://www.theses.fr/2017ISAT0023>