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1 **Estimation of soil water retention in conservation agriculture using published and new**  
2 **pedotransfer functions**

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10

11 **Abstract**

12 Conservation agriculture has been developed as a means to improve the sustainability of  
13 agricultural systems and reduce drawbacks of conventional agricultural practices. Cropping  
14 practices can have a large influence on soil properties such as water retention. Proper tools are  
15 needed to assess and model effects of conservation agriculture on soil properties. As measuring soil  
16 water retention is expensive and time consuming, pedotransfer functions (PTFs) are now commonly  
17 used to predict them. The objectives of this study were to (i) present a new dataset of conservation  
18 agriculture data, (ii) assess performances of existing PTFs in predicting soil water retention of soils  
19 under conservation agriculture and (iii) develop new specific PTFs to predict water retention in  
20 conservation agriculture more accurately. We used data collected only in fields under conservation  
21 agriculture in France to evaluate several published PTFs with three evaluation criteria (RMSE,  
22 prediction bias (ME) and Nash-Sutcliffe Efficiency (EF)). We then developed new PTFs using three  
23 methods – multiple linear regression, regression tree and random forest – to predict soil water  
24 content at matric heads of -100 ( $\theta_{100}$ , field capacity for sandy soils), -330 ( $\theta_{330}$ , field capacity for  
25 other soils) and -15 000 cm ( $\theta_{15\ 000}$ , wilting point). Soil tillage, presence of a cover crop, rotation  
26 length and previous reduced/no tillage were used as predictors in addition to basic soil properties  
27 for regression trees and random forests. The quality of prediction (RMSE, ME and EF) was  
28 calculated for each new PTF using a cross-validation procedure. Generally, predictions of wilting

29 point had lower absolute error than those of sandy-soil field capacity (RMSE = 0.044 and 0.066  
30  $\text{cm}^3/\text{cm}^3$ , respectively). EF was usually negative for all water contents. The cross-validation  
31 performance of the new PTFs was similar for multiple linear regression (RMSE: 0.028, ME: 0.000,  
32 EF: 0.34 for  $\theta_{100}$ ) and random forest (RMSE: 0.027, ME: 0.000, EF: 0.36 for  $\theta_{100}$ ), and generally  
33 worse for regression tree (especially EF). Multiple linear regression that did not consider cropping  
34 practices performed as well as random forest and thus did not identify any major influence of  
35 agricultural management on predicted water content. Future research on developing PTFs should  
36 focus on identifying more relevant predictors.

37

38 Keywords: soil water content, pedotransfer functions, available water capacity, soil tillage, linear  
39 regressions, regression trees, random forests

40

## 41 1. Introduction

42 Conservation agriculture was developed to enhance the sustainability of agricultural systems  
43 and reduce drawbacks of conventional agriculture, especially soil degradation due to erosion  
44 (Hobbs et al., 2008). Conservation agriculture combines three main interrelated soil conservation  
45 techniques: (i) little or no soil disturbance, (ii) permanent soil cover by crop residues and/or living  
46 cover crops and (iii) diversification of plant species (FAO, 2016). Interactions among these three  
47 techniques lead to complex and interrelated modifications in soil physical, chemical and biological  
48 properties. Considering these changes is crucial to assess performances of such agricultural systems  
49 properly. However, studies of impacts of conservation agriculture on soil properties show many  
50 inconsistencies, especially for soil hydraulic processes (Green et al., 2003; Strudley et al., 2008;  
51 Verhulst et al., 2010).

52 Effects of soil cultivation practices on soil properties has received much research attention in  
53 recent decades, but clear trends have not been established due to differences in location, soils and  
54 agricultural practices (Green et al., 2003; Strudley et al., 2008). Tillage tends to decrease bulk

55 density and increase macroporosity, thus increasing the saturated and near-saturated hydraulic  
56 conductivity of the tilled layer. These effects are, however, strongly time-dependent and usually  
57 disappear rapidly after tillage (Mapa et al., 1986), due to natural soil reconsolidation caused by  
58 wetting and drying cycles (Ahuja et al., 1998). Simultaneously, tillage interrupts macropore  
59 connectivity between the soil surface and the untilled deeper soil, thus decreasing water movement  
60 throughout the entire soil profile (Cameira et al., 2003). Conversely, untilled soils have higher bulk  
61 density and greater pore connectivity (Gozubuyuk et al., 2014). Cover crops may (partially)  
62 counterbalance negative effects of no tillage on bulk density by, for example, creating stable  
63 biopores through their root development during the growing season (Williams and Weil, 2004;  
64 Abdollahi and Munkholm, 2014). Moreover, after cover crop destruction, the dead residues form a  
65 mulch that physically protects the soil surface from crusting (Baumhardt and Lascano, 1999).  
66 Maintaining crop residues on the soil surface also leads to accumulation of soil organic matter in  
67 topsoil layers (Kay and VandenBygaart, 2002) and improves aggregate stability (Devine et al.,  
68 2014). In parallel, increased macrofauna activity (especially of earthworms) in conservation  
69 agriculture systems forms biopores that improve water infiltration (Shipitalo et al., 2000).  
70 Finally, soils under conservation agriculture also tend to have a larger proportion of finer pores  
71 (micropores) (Hill et al., 1985). These changes in pore-size distribution could improve the storage  
72 of plant-available water (Bescansa et al., 2006).

73 The variety and complexity of the counteracting effects of conservation agriculture on soil  
74 properties call for developing new tools to properly assess and model these effects. Development of  
75 water- and solute-transport models has received much research attention in recent decades. The lack  
76 of accurate data on soil hydraulic properties, especially for soils under conservation agriculture,  
77 however, hinders the use of models, as they require water-retention and hydraulic conductivity data  
78 as inputs (Wösten et al., 1999). Despite significant improvements in measuring techniques,  
79 researchers agree that directly measuring water-retention curves remain expensive, time consuming

80 and impossible at a large scale (Wösten et al., 2001; Vereecken et al., 2010; Román Dobarco et al.,  
81 2019).

82 Predicting hydraulic properties may be accurate enough to be used in water- and solute-  
83 transport models (Wösten et al., 2001). One promising solution to managing the scarcity of  
84 hydraulic data is to use pedotransfer functions (PTFs), which relate easily available soil properties  
85 to properties that are more difficult to measure, such as hydraulic ones (Al Majou et al., 2008b).  
86 Many PTFs have been developed, and two main groups of water-retention PTFs can be  
87 distinguished: “point” PTFs, which predict volumetric water content at a given matric head, and  
88 “parametric” PTFs, which predict parameters of the water-retention curve as described by van  
89 Genuchten (1980). In addition, depending on the type of input data used, PTFs can be further  
90 divided into “class-PTFs” and “continuous-PTFs”. Class-PTFs predict mean volumetric water  
91 content at a given matric head or mean water-retention curve parameters using information such as  
92 textural class, type of horizon and bulk density class (Al Majou et al., 2008b; Bruand et al., 2004).  
93 Continuous-PTFs are regression equations that predict volumetric water content at a given matric  
94 head or water-retention curve parameters using continuous input variables such as granulometric  
95 fractions, bulk density and soil organic carbon content (Al Majou et al., 2008a; Rawls et al., 1982).  
96 More recently, novel machine-learning methods have been used to develop PTFs based on  
97 regression trees (i.e. “tree-PTFs”) (Toth et al. 2015).

98 Although PTFs have significantly facilitated widespread application of water- and solute-  
99 transport models at the field scale and larger scales (Vereecken et al., 2010), some of their limits  
100 have been identified. Several authors suggested that using information in addition to the commonly  
101 used sand, silt and clay contents, bulk density and organic matter could improve prediction accuracy  
102 (Vereecken et al., 2010). Water contents at selected matric heads (Rawls et al., 1983; Al Majou et  
103 al., 2008a) or terrain attributes (Obi et al., 2014) have been proposed as additional information.  
104 Land cover (Nemes et al., 2003) or soil management (Tóth et al., 2015) have also been proposed,  
105 but they may create PTFs that are less applicable than those that use only soil properties as

106 parameters. Whether the available PTFs apply equally to soils under conservation or conventional  
107 agriculture has not yet been explored. The type of agriculture under which the soils used to develop  
108 a particular PTF is rarely specified, but most PTFs seem to have been developed from soils under  
109 conventional agriculture. To our knowledge, no one has attempted to develop specific tools to  
110 predict water content in conservation agriculture systems. Chen et al. (1998) did observe that the  
111 relevant properties for describing hydraulic conductivity differed between tilled and untilled soil,  
112 which highlights the importance of soil management and supports the need for additional data and  
113 specific tools to predict water dynamics in soils under conservation agriculture.

114 The aims of this study were to (i) present a dataset of water retention data from soils under  
115 conservation agriculture (ii) assess performances of existing PTFs in predicting soil water retention  
116 of these soils and (iii) develop new PTFs using several statistical techniques to improve  
117 representation of the hydraulic properties of soils under conservation agriculture.

118

## 119 **2. Materials and methods**

### 120 *2.1 Description of the dataset on conservation agriculture*

121 Information on farming operations and soil chemical and physical characteristics were  
122 collected from 2009-2011 in 47 fields under conservation agriculture in the central basin of the  
123 Occitanie region in south-west France. Soil types there are mainly hypereutric cambisols, luvisols  
124 and calcareous cambisols (IUSS Working Group WRB, 2015). All fields had been cultivated using  
125 conservation practices since 1987-2003. Four types of tillage were used: deep tillage (DT), with a  
126 working depth >15 cm (n=7 fields); reduced tillage (RT), with a working depth of 5-15 cm (n=18);  
127 strip-till (ST), with tillage restricted to the future row (n=3); and no tillage (NT) (n=19). In addition  
128 to tillage, cover crops were used on 35 of the fields. Four classes of crop rotation were defined:  
129 rotation length > 4 years (n=24); > 2 years to ≤ 4 years (n=15); ≤ 2 years (n=2); and not fixed (n=6).

130 In each field, soil samples were collected from the topsoil (0-30 cm) and then divided into  
131 three layers: 0-10 cm (47 samples), 10-20 cm (47 samples) and 20-30 cm (46 samples). Several  
132 physicochemical properties were determined using international and French norms (NF) published  
133 by the French national organization for standardization (AFNOR) from one bulk sample per layer.  
134 The granulometric distribution of five decarbonated fractions (clay (<2  $\mu\text{m}$ ), fine silt (2-20  $\mu\text{m}$ ),  
135 coarse silt (20-50  $\mu\text{m}$ ), fine sand (50-200  $\mu\text{m}$ ), coarse sand (200-2000  $\mu\text{m}$ )) was determined using  
136 NF X31-107. Soil samples from the fields were concentrated in the silty and clayey zones of the  
137 texture triangle (Fig. 1). NF ISO 10694 was used to determine carbon content and estimate organic  
138 matter content. NF ISO 10390 was used to determine pH (in water). NF ISO 11263 was used to  
139 determine phosphorus content ( $\text{P}_2\text{O}_5$ ) using the Olsen method. NF ISO 10693 was used to  
140 determine total calcium carbonate content. Cation exchange capacity (CEC) and exchangeable CaO,  
141  $\text{Na}_2\text{O}$ ,  $\text{K}_2\text{O}$  and  $\text{MgO}$  were determined using NF ISO 23470. When CaO content was found to be  
142 saturated (i.e. not quantifiable by this method), it was calculated as CEC minus the sum of  $\text{Na}_2\text{O}$ ,  
143  $\text{K}_2\text{O}$  and  $\text{MgO}$ . The Kjeldahl method was used to determine nitrogen content.

144 In addition, for each topsoil layer, soil bulk density was determined from undisturbed soil  
145 samples collected with 250  $\text{cm}^3$  cylinders (8 cm in diameter, 5 cm high), and the soil water-  
146 retention curve was determined from undisturbed soil samples collected with 50  $\text{cm}^3$  cylinders (5  
147 cm in diameter, 2.5 cm high). Bulk density was measured in triplicate for each layer. Soil water  
148 retention was usually measured in duplicate or triplicate (rarely, only one sample was available) and  
149 recorded in the dataset as a mean value. Volumetric water content ( $\theta$ ,  $\text{cm}^3/\text{cm}^3$ ) was measured  
150 successively at 0 ( $\theta_0$ ), -100 ( $\theta_{100}$ ), -330 ( $\theta_{330}$ ), -3300 ( $\theta_{3300}$ ) and -15 000 ( $\theta_{15\ 000}$ ) cm of matric head.  
151  $\theta_0$  was measured after the cylinders were saturated for two days on a tray filled with glass beads  
152 (diameter  $\approx 0.45 \mu\text{m}$ ). The other water contents were measured using pressure plates. The resulting  
153 data were used to fit water-retention curve parameters using the RETC program (van Genuchten et  
154 al., 1991) based on the van Genuchten (1980) equation (eq. 1):

$$155 \quad \theta_h = \theta_r + \frac{\theta_s - \theta_r}{[1 + (\alpha h)^n]^m} \quad m = 1 - \frac{1}{n} \quad (1)$$

156 where  $\theta_r$  [cm<sup>3</sup>/cm<sup>3</sup>] and  $\theta_s$  [cm<sup>3</sup>/cm<sup>3</sup>] are the residual and saturated volumetric water content ( $\theta$ )  
 157 respectively,  $h$  is matric head [cm], and  $\alpha$  [cm<sup>-1</sup>],  $n$  [-], and  $m$  [-] are shape parameters of the curve.  
 158 The fit of the curves to the data had a mean R<sup>2</sup> ( $\pm$  1 SD) of 0.98  $\pm$  0.02.

159 Finally, plant available water capacity (AWC, in mm) was calculated as follows:

$$160 \quad AWC = (\theta_{FC} - \theta_{WP}) \times H \quad (2)$$

161 where  $\theta_{FC}$  and  $\theta_{WP}$  are volumetric water content at field capacity and permanent wilting point  
 162 (cm<sup>3</sup>/cm<sup>3</sup>), respectively, and  $H$  is the depth of each of the three layers (here, 100 mm).

163 According to the literature,  $\theta_{FC}$  can equal either  $\theta_{100}$  (for sandy soils) or  $\theta_{330}$  (for other soils), and  
 164  $\theta_{WP}$  equals  $\theta_{15\,000}$  (Hillel, 1971). Both AWC<sub>100</sub> and AWC<sub>330</sub> were considered for the two definitions  
 165 of  $\theta_{FC}$ . However, PTFs are usually used to predict volumetric water content at several matric heads  
 166 rather than AWC. The rest of the study thus focused only on the relation between  $\theta_{100}$ ,  $\theta_{330}$ ,  $\theta_{15\,000}$   
 167 and basic soil properties and/or cropping practices.

## 168 *2.2 Analysis of the dataset*

169 Principal component analysis (PCA) was performed to explore relations among the  
 170 explanatory variables, using the “FactoMineR” package of R software (version 3.6.1) (R Core  
 171 Team, 2019) using only soil properties. Soil water contents were used only as supplementary  
 172 variables. Spearman correlations were calculated between explanatory variables and soil water  
 173 content at different matric heads, using the “psych” R package. Unbalanced Type II analysis of  
 174 variance (ANOVA) was performed to investigate effects of soil tillage, cover-crop presence,  
 175 rotation length and soil depth on soil water contents, using the “car” R package.



### 176 2.3 *Published pedotransfer functions*

177 Twenty nine existing PTFs that predict  $\theta_{100}$  or  $\theta_{330}$ , and/or  $\theta_{15\,000}$  (Table 1) and eight PTFs  
178 that predict three parameters ( $n$ ,  $\alpha$ , and  $\theta_s$ ) of the van Genuchten (1980) water-retention curve (Eq.  
179 1, Table 2) were taken from the literature and applied to data for the 140 soils in this study. The  
180 study used class-PTFs (Cl), continuous-PTFs (Co) and tree-PTFs (Tr). PTFs were calibrated using  
181 several published databases (Table 1). Of the 26 PTFs that predict  $\theta_{100}$ , 13 were Cl and 13 were Co.  
182 Of the 28 PTFs that predict  $\theta_{330}$ , 13, 13 and 2 were Cl, Co and Tr, respectively. Of the 27 PTFs that  
183 predict  $\theta_{15\,000}$ , 13, 12 and 2 were Cl, Co and Tr, respectively. These published PTFs use different  
184 variables as predictors, such as texture/granulometric fractions, bulk density and organic carbon  
185 content. Two PTFs (M2\_Co and M3\_Co) also use  $\theta_{FC}$  and/or  $\theta_{WP}$  as predictors. However, as a water  
186 content cannot be used to predict itself, M2\_Co and M3\_Co were not used to predict  $\theta_{330}$  or  $\theta_{15\,000}$ .  
187 Most publications identified in the literature (Table 1) also had PTFs for subsoil horizons (> 30 cm).  
188 We used only the published PTFs developed for the topsoil as the dataset contained only topsoil  
189 data. All PTFs were applied to soil data in our dataset to predict  $\theta_{100}$ ,  $\theta_{330}$ ,  $\theta_{15\,000}$ ,  $n$ ,  $\alpha$  and  $\theta_s$ .

### 190 2.4 *Development of new pedotransfer functions*

191 Three types of PTFs, which predicted  $\theta_{100}$ ,  $\theta_{330}$  or  $\theta_{15\,000}$ , were developed. Redundant properties  
192 (calculated from another property), such as organic matter content and the C:N ratio, were removed  
193 from the input data. Table 3 provides summary statistics of the variables that were used for each of  
194 the following methods.

#### 195 2.4.1 Multiple linear regression

196 We developed multiple linear regressions using stepwise regression with forward selection,  
197 which could include all soil properties as predictors. In this procedure, the Akaike information  
198 criterion (AIC) (Akaike et al., 1998) was used to determine which set of predictors predicted water  
199 content best. AIC is calculated at each step of the stepwise regression to determine the improvement

200 brought by adding the new predictor. The “best” model is the one that helps decrease AIC the most.  
201 The procedure stops when no more improvement can be made by a new predictor or when all  
202 predictors are included.

### 203 2.4.2 Regression tree

204 Regression tree methods consist of recursive binary partitions of a dataset. At each node,  
205 observations are split according to a decision rule based on only one predictor. Splitting continues  
206 until all of the subsets (i.e. “terminal nodes” of the tree) are as homogeneous as possible with  
207 reference to the response variable (Hastie et al., 2009; Prasad et al., 2006). Splitting stops when the  
208 subset reaches a minimum size of 5 data points or when no more improvement can be made. The  
209 criterion used to decide which predictor splits the data best is based on ANOVA. First, a maximum  
210 tree is grown that likely overfits the training data. To reduce the size of the tree and avoid  
211 overfitting, the tree is then pruned using cost-complexity pruning (10 cross validation). Briefly, for  
212 each pair of terminal leaves with a common parent node, the error in classifying the testing dataset  
213 is calculated to see whether the sum of squares would be smaller by turning the parent nodes into a  
214 terminal leaf. The procedure is repeated until the pruning does not decrease the error in the testing  
215 data. The resulting pruned tree is usually smaller than the initial maximum tree, but in theory,  
216 pruned trees can range from the maximum size to minimum size (no partitions, no tree). The size of  
217 the pruned tree can depend on the cross-validation method used. The pruned tree to be used as a  
218 model for each water content was then randomly selected. The response variable was volumetric  
219 water content at a given matric head, and the terminal nodes of the tree represented mean water  
220 content in the partitions. The “rpart” R package (Therneau and Atkinson, 2019) was used to build  
221 the trees.

### 222 2.4.3 Random forest

223 Like for regression tree, random forest is also based on recursive partitions of the data. The  
224 difference is that a forest of multiple decorrelated trees is grown by using a randomly bootstrapped

225 subset of data and a random subset of predictors (Hastie et al., 2009; Ließ et al., 2012). The  
 226 “randomForest” R package (Liaw and Wiener, 2002) was used to build forests. The forest consisted  
 227 of 500 trees, and six of 18 variables were randomly selected to grow each tree. Like for regression  
 228 tree, the minimum size of a terminal node was 5 data points. Unlike for regression tree, however, a  
 229 single tree cannot be extracted from the forest, but the relative importance of the predictors can be  
 230 determined and used to help interpret the results. The relative importance of predictors was  
 231 estimated according to how much worse the prediction would be if the data for that predictor were  
 232 permuted randomly (Prasad et al., 2006).

### 233 2.5 Evaluation of pedotransfer functions

234 PTFs were evaluated by comparing predicted values to observed values in the dataset according  
 235 to three criteria: root mean squared error (RMSE), mean error (ME) (also called “bias”) (Bruand et  
 236 al., 2003) and Nash-Sutcliffe efficiency (EF; Nash and Sutcliffe, 1970). They are calculated as  
 237 follows:

$$238 \quad RMSE = \sqrt{\frac{1}{N} \sum_{k=1}^N [f(x_k) - y_k]^2} \quad (3)$$

$$239 \quad ME = \frac{1}{N} \sum_{k=1}^N [f(x_k) - y_k] \quad (4)$$

$$240 \quad EF = 1 - \frac{\sum_{k=1}^N [f(x_k) - y_k]^2}{\sum_{k=1}^N [y_k - \bar{y}]^2} \quad (5)$$

241 where  $f(x_k)$  are the values predicted by the PTF,  $y_k$  are the observed values in the conservation  
 242 agriculture dataset,  $x_k$  are the input data (basic soil properties) needed by PTF  $f$ ,  $\bar{y}$  is the mean of  
 243 observed values and N is the number of data points.

244 RMSE = 0 indicates perfect prediction of the observed data, while the ME indicates whether the  
 245 PTF overpredicts (positive ME) or underpredicts (negative ME) the observed data. The closer ME  
 246 is to 0, the lower the bias is. EF=1 indicates perfect prediction of the observed data, while EF<0

247 indicates prediction worse than the that using the mean of observed values (for which  $EF=0$ ). These  
248 criteria have no thresholds that can be used to conclude whether a prediction is good or not;  
249 nevertheless, to help interpret the results, we arbitrarily defined ranges to indicate satisfactory  
250 prediction of AWC: less than  $0.020 \text{ cm}^3/\text{cm}^3$  for RMSE and ME, and greater than 0.50 for EF.

251 The three criteria were used to assess the performance of the published and new PTFs. For  
252 published PTFs,  $f(x_k)$  corresponded to predictions using basic soil properties in the conservation  
253 agriculture dataset as input data, assessed with the criteria  $RMSE_P$ ,  $ME_P$  and  $EF_P$ . For the new  
254 PTFs, two groups of criteria were used to evaluate their performance. One group of three criteria  
255 ( $RMSE_A$ ,  $ME_A$ ,  $EF_A$ ) evaluated the quality of adjustment to the data. In this case,  $f(x_k)$   
256 corresponded to predictions by the new PTF using basic soil properties in the same dataset from  
257 which they had been developed. The second group of criteria ( $RMSE_{CV}$ ,  $ME_{CV}$ ,  $EF_{CV}$ ) evaluated the  
258 cross-validation quality of prediction. As the dataset contained too few soils ( $N=140$ ) to split out an  
259 independent validation dataset, leave-one-out cross validation (Hastie et al., 2009) was performed  
260 instead. In it, the dataset was split 140 times into two datasets of 139 and 1 soils, respectively. The  
261 140 datasets of 139 soils were used to calibrate 140 new PTFs. The 140 predictions were then  
262 compared to their corresponding value in the dataset of observed values.

### 263 3. Results

#### 264 3.1 Preliminary analysis of the dataset

265  $AWC_{100}$  and  $AWC_{330}$  (in the 0-10, 10-20 and 20-30 cm soil layers) ranged from 10.4-28.6 mm  
266 and 4.2-22.9 mm, respectively, depending on the soil layer. Both varied little as a function of depth,  
267 tillage or cover-crop presence (Fig. 2). However, differences were larger as a function of rotation  
268 length (Fig. 2d, h). Mean  $AWC_{100}$  was ca. 20, 18 and 16 mm when the rotation length was variable,  
269 medium/long and short, respectively. Despite small differences, statistical analysis demonstrated a  
270 significant effect of the three cropping practices (i.e. tillage, cover-crop presence and rotation

271 length) (except for tillage for  $AWC_{330}$ ) and of depth for both AWCs. Both  $AWC_{100}$  and  $AWC_{330}$   
 272 were highest (by a small degree) in the 0-10 cm layer (Fig. 2a, e).

273 The plane defined by the first two axes of the PCA of basic soil properties explained 57% of the  
 274 variance of the dataset (Fig. 3a). Of the 14 basic soil properties, only 8 contributed significantly (i.e.  
 275 more than if each one had contributed equally (i.e., 7%)) to the first two axes. Strong correlations  
 276 were found between CEC, CaO content and clay content ( $r_{CEC/CaO} = 1$ ,  
 277  $r_{Clay/CaO} = r_{CEC/CaO} = 0.9$ ), which contributed the most to the first two axes due to their large  
 278 contributions to the first axis (17%, 16% and 16%, respectively). Nitrogen, organic carbon and  
 279 phosphorus contents contributed the most to the second axis (22%, 21% and 19%, respectively).  
 280 Strong to very strong correlations were found between organic carbon, nitrogen and  $K_2O$  contents  
 281 ( $r_{OC/N} = 0.94$ ,  $r_{K_2O/OC} = r_{K_2O/N} = 0.7$ ). Thus, soil layers above the second axis of the PCA had  
 282 higher organic carbon, nitrogen and phosphorus contents, which was related to their depth, as most  
 283 soil layers above the second axis were 0-10 cm deep (Fig. 3b). This is consistent with the low  
 284 mechanical disturbance of the soil surface under conservation agriculture, which results in a thin  
 285 horizon 5-10 cm deep that can exhibit different soil properties, especially organic matter. When  
 286 projected as supplementary variables on the plane, water contents were poorly represented (Fig. 3a),  
 287 which suggested that none of the basic soil properties were strongly related to them, as confirmed  
 288 by correlation coefficients. The strongest significant correlations for  $\theta_{100}$  were with clay content  
 289 ( $r = 0.5$ ), bulk density ( $r = -0.4$ ), sand content ( $r = -0.4$ ) and CEC ( $r = 0.4$ ). Correlations for  
 290  $\theta_{330}$  were weaker, not exceeding 0.3 with clay content or -0.3 with bulk density. Correlations for  
 291  $\theta_{15\ 000}$  were the strongest among those for the three water contents: 0.6 with clay content, CEC and  
 292 CaO content.

293 We plotted  $\theta_{100}$ ,  $\theta_{330}$  and  $\theta_{15\ 000}$  vs. cropping practices, rotation length, soil tillage and cover-  
 294 crop presence to identify the influence of conservation agriculture on water contents. We also  
 295 investigated the influence of depth, as the PCA indicated a difference between the 0-10 cm layer

296 and the other two layers. There were no clear differences between  $\theta_{100}$  or  $\theta_{330}$  as a function of  
 297 agricultural practices, except for rotation length, with water content lower with variable rotations  
 298 and higher with short rotations, compared to long or medium rotations (Fig. 4a, b). ANOVA  
 299 confirmed a significant effect of rotation length on  $\theta_{100}$  ( $P < 0.001$ ) and  $\theta_{330}$  ( $P < 0.01$ ). For  $\theta_{15\,000}$ ,  
 300 water content was lower under strip-till than under the other types of tillage and had a trend similar  
 301 to those of  $\theta_{100}$  and  $\theta_{330}$  for rotation length (Fig. 4c, d). All three cropping practices had a significant  
 302 effect on  $\theta_{15\,000}$  ( $P < 0.01$  for soil tillage and  $P < 0.001$  for cover-crop presence and rotation length).  
 303 Unlike for AWC, depth had no significant effect on any of the water contents.

### 304 *3.2 Evaluation of the performance of published pedotransfer functions*

#### 305 3.2.1 Prediction of volumetric water content at selected matric heads

306 For prediction of  $\theta_{100}$ ,  $RMSEP$  varied from  $0.034\text{ cm}^3/\text{cm}^3$  (M3\_Co) to  $0.262\text{ cm}^3/\text{cm}^3$   
 307 (M2\_Co) (Table 4). These extreme values were exceptions, however; mean ( $\pm 1\text{ SD}$ )  $RMSEP$  for  
 308 most of the PTFs (22 of 26) was  $0.055 \pm 0.009\text{ cm}^3/\text{cm}^3$ . Of the 26 PTFs, 24 underpredicted  $\theta_{100}$ ,  
 309 with  $ME_P$  ranging from  $-0.112$  to  $-0.007\text{ cm}^3/\text{cm}^3$ . The same four PTFs that had extreme values of  
 310  $RMSEP$  (M1\_Co, M2\_Co, M3\_Co and M10\_Co) had extremely high or low  $ME_P$ . For  $EF_P$ ,  
 311 negative or near-zero values showed that none of the PTFs tested predicted  $\theta_{100}$  well. According to  
 312 the three criteria, M3\_Co, despite having been developed from samples from many locations in the  
 313 USA, predicted  $\theta_{100}$  the best, but used both  $\theta_{330}$  and  $\theta_{15\,000}$  as predictors. However, the other two  
 314 PTFs developed from the same data (M1\_Co, M2\_Co) predicted  $\theta_{100}$  the worst. Among the  
 315 remaining PTFs, which used only basic soil properties, eight French Cl PTFs (M7\_Cl, M8\_Cl,  
 316 M12\_Cl, M13\_Cl, M14\_Cl, M19\_Cl, M20\_Cl, M21\_Cl) had better  $RMSEP$  ( $0.046 \pm 0.004$   
 317  $\text{cm}^3/\text{cm}^3$ ) and  $ME_P$  ( $-0.028 \pm 0.004\text{ cm}^3/\text{cm}^3$ ) than the others. However,  $ME$  remained  
 318 unsatisfactory. All eight PTFs were Cl that used FAO texture or FAO texture and bulk density as  
 319 classes.

320 For prediction of  $\theta_{330}$ ,  $RMSE_P$  ranged from  $0.037 \text{ cm}^3/\text{cm}^3$  (M4\_Cl) to  $0.080 \text{ cm}^3/\text{cm}^3$   
 321 (M10\_Co) and were thus lower overall than those for  $\theta_{100}$ . Of the 28 PTFs, 16 overpredicted  $\theta_{330}$   
 322 ( $ME_P=0.017 \pm 0.015 \text{ cm}^3/\text{cm}^3$ ). The worst  $ME_P$  ( $-0.069 \text{ cm}^3/\text{cm}^3$ ) was an underprediction by  
 323 M10\_Co (Table 4). Four PTFs (M1\_Co, M2\_Co, M10\_Co and M16\_Tr) performed worse than the  
 324 others for all three criteria, especially M10\_Co, a PTF for topsoil layers developed by Al Majou et  
 325 al. (2007). Although the  $RMSE_P$  and  $ME_P$  of the other 24 PTFs were lower, their  $EF_P$  never reached  
 326 satisfactory values ( $\geq 0.5$ ), so their potential use remains limited.

327 For prediction of  $\theta_{15\ 000}$ ,  $RMSE_P$  varied from  $0.034 \text{ cm}^3/\text{cm}^3$  (M22\_Co) to  $0.057 \text{ cm}^3/\text{cm}^3$   
 328 (M10\_Co) and were thus lower overall than those of the other water contents (Table 4). Of the 27  
 329 PTFs, 18 overpredicted  $\theta_{15\ 000}$  ( $ME_P=0.008 \pm 0.007 \text{ cm}^3/\text{cm}^3$ ), but there was no systematic bias.  
 330 Overall, two groups of performance were identified. The first, with lower  $RMSE_P$ , low  $ME_P$  and  
 331 positive  $EF_P$ , were the eight Co of Román Dobarco et al. (2019) and the Co of Tóth et al. (2015).  
 332 This group of PTFs could probably be used with lower risk of poor prediction. Nevertheless, even  
 333 though their  $EF_P$  were positive and much higher than those of the other two water contents, they  
 334 still had difficulty reaching the satisfactory threshold.

### 335 3.2.2 Prediction of water-retention curve parameters

336 For predicting  $\theta_s$ ,  $RMSE_P$  ranged from  $0.035\text{-}0.439 \text{ cm}^3/\text{cm}^3$ , while  $ME_P$  ranged from  $-0.438$  to  
 337  $0.010 \text{ cm}^3/\text{cm}^3$  (Table 5). P2\_Co and P4\_Co had large errors due to physically impossible values of  
 338  $\theta_s$  (close to 0 or even negative). For the other PTFs that predicted  $\theta_s$ ,  $RMSE_P$  and  $ME_P$  had  
 339 satisfactory performances, with the best performance by P3\_Cl, P7\_Co, P8\_Co and P9\_Co  
 340 ( $RMSE_P= 0.037 \pm 0.001 \text{ cm}^3/\text{cm}^3$ ;  $ME_P= 0.023 \pm 0.010 \text{ cm}^3/\text{cm}^3$ ;  $EF_P= -0.43 \pm 0.12$ ). Negative  $EF_P$   
 341 values, however, indicated that none of the PTFs performed better than the mean of observed  
 342 values.

343 For predicting  $\alpha$ , the French PTF P3\_Cl had particularly poor performance according to all  
 344 criteria, and P4\_Cl predicted physically impossible values. Thus, the best predictions were obtained

345 only with PTFs developed at the European scale, all of which performed similarly. For predicting  $n$ ,  
346  $RMSE_P$  varied from 0.305-0.366. The nine PTFs always underpredicted  $n$  (negative  $ME_P$ ), except  
347 for P8\_Co, which had the only satisfactory  $ME_P$  (0.003) and the best  $RMSE_P$ . The two PTFs  
348 developed from soil samples from France performed slightly worse according to all criteria.

### 349 *3.3 Development of new pedotransfer functions*

#### 350 3.3.1 Multiple linear regression

351 All regressions developed from our dataset (N=140) included clay content and bulk density  
352 as predictors (Table 6). The sign of the coefficients associated with these two variables was similar  
353 in each regression and indicated that water content increased as clay content increased and bulk  
354 density decreased. Regressions for  $\theta_{100}$  and  $\theta_{15\ 000}$  also included silt content as predictor, with a  
355 positive effect. Other predictors were included only once in the regressions. Of the 14 potential  
356 predictors, only five, four and four were kept in the  $\theta_{100}$ ,  $\theta_{330}$  and  $\theta_{15\ 000}$  regressions, respectively.  
357 The qualities of adjustment and cross-validation did not differ greatly, except for slightly better  $EF_A$   
358 than  $EF_{CV}$  (Table 7, Fig. 5a). Predictions of  $\theta_{330}$  had worse  $EF_A$  (and  $EF_{CV}$ ) than the other water  
359 contents did.

#### 360 3.3.2 Regression tree

361 The maximum tree grown for  $\theta_{100}$ ,  $\theta_{330}$  and  $\theta_{15\ 000}$  had 11, 9 and 8 partitions, respectively,  
362 despite the inclusion of 18 potential predictors. After pruning, the  $\theta_{330}$  tree was reduced to the  
363 minimum size (no partitions); thus, the mean of  $\theta_{330}$  was the best compromise between a suitable  
364 tree size and low error in predicting the testing data. Consequently, only the trees that predicted  $\theta_{100}$   
365 and  $\theta_{15\ 000}$  were evaluated (Fig. 6). The pruned  $\theta_{100}$  and  $\theta_{15\ 000}$  trees were split 7 and 4 times,  
366 respectively, and had three predictors in common: rotation length, clay content and bulk density.  
367 Both trees were first split according to rotation length, which split variable length from the other  
368 lengths. No other cropping practices appeared in the pruned trees. According to the criteria, all trees



369 had satisfactory quality of adjustment to observed data, with  $ME_A=0$  and  $EF_A \geq 0.5$  (Table 7). All  
 370 criteria except  $ME_A$  were slightly higher for  $\theta_{15\ 000}$  than for  $\theta_{100}$ . The criteria for cross-validation  
 371 quality of prediction had similar trends, with low  $ME_{CV}$ , but the trees did not predict well according  
 372 to  $EF_{CV}$  ( $<0.21$ ) (Table 7). Prediction performance thus decreased between adjustment and cross  
 373 validation (Fig. 5b).

### 374 3.3.3 Random forest

375 Clay content was one of the two most important predictors in the  $\theta_{100}$ ,  $\theta_{330}$  and  $\theta_{15\ 000}$   
 376 random forests (importance of 11%, 10% and 21%, respectively) (Fig. 7). Bulk density was the  
 377 most important predictor for the  $\theta_{100}$  and  $\theta_{330}$  random forests (importance of 14% and 11%,  
 378 respectively) but not for the  $\theta_{15\ 000}$  random forest (only 5% importance). Sand content also had  
 379 significant importance in each random forest, while organic carbon was significant only in the  $\theta_{100}$   
 380 random forest. Rotation length was one of the most important variables in the  $\theta_{15\ 000}$  random forest  
 381 (importance of 12%), but the other cropping practices had low importance. All random forests fit  
 382 well to the data, with low  $RMSE_A$ ,  $ME_A=0$  and  $EF_A > 0.83$  (Table 7). The cross-validation quality of  
 383 prediction showed satisfactory  $RMSE_{CV}$  and  $ME_{CV}$ , but  $EF_{CV}$  remained less than 0.5, which  
 384 indicated limited performance of the models. Prediction performance thus decreased strongly  
 385 between adjustment and cross validation (Fig. 5c).

## 386 **4. Discussion**

### 387 *4.1 Evaluation of the performance of published pedotransfer functions*

388 Most PTFs (24 of 26) underpredicted soil volumetric water content at -100 cm of matric  
 389 head, while no clear trend (overestimation or underestimation) was observed at -330 and -15 000  
 390 cm. The  $RMSE_P$  for predicting volumetric water content were largest for the -100 and -330 cm  
 391 matric heads. Although  $EF_P$  was higher for several PTFs at -15 000 cm, it was never satisfactory ( $\geq$   
 392 0.5). Overall, none of the 29 published PTFs provided satisfactory prediction of the volumetric

393 water content at the selected matric heads (-100, -330 and -15 000 cm) according to any of the  
394 criteria, which limits their use in soil transport models under conservation agriculture.

395 The published PTFs may have had low-quality predictions for several reasons. First, differences  
396 in the sampling or measurement protocol between the databases used to develop the PTFs and the  
397 dataset that we used may be a source of uncertainty (Román Dobarco et al., 2019). For example, Al  
398 Majou et al. (2008b) measured water content using undisturbed aggregates (10-15 cm<sup>3</sup>), whereas we  
399 used undisturbed soil cylinders (50 cm<sup>3</sup>). Several studies have also highlighted the influence of  
400 sample size on soil water retention and the quality of PTFs developed (Ghanbarian et al., 2015;  
401 Silva et al., 2018). Furthermore, some of these PTFs were developed from large databases collated  
402 in the USA or Europe and covered a wide range of sand, silt, clay and organic matter contents and  
403 bulk densities (Rawls et al., 1982; Tóth et al., 2015). Like Cornelis et al. (2001), we calculated the  
404 ranges of the soil properties of our samples and found that all lay within those in the databases from  
405 the USA and Europe; nevertheless, the predictions were unsatisfactory according to the criteria.  
406 Nemes et al. (2003) suggested that using a small set of relevant data rather than a larger, more  
407 general dataset can produce more accurate PTFs. Indeed, for predicting Hungarian soils, they found  
408 that PTFs that had been developed by neural networks from data from throughout the USA and  
409 Europe performed worse than PTFs that had been developed from a smaller dataset that considered  
410 the pedoclimatic context (e.g. the subset of Hungarian soils). Testing published PTFs developed  
411 from large and general datasets with our dataset may explain the poor prediction in our study.  
412 However, most of the PTFs tested were developed from French databases (Bruand et al., 2004; Al  
413 Majou et al., 2007, 2008a, 2008b; Román Dobarco et al., 2019) and should have been more  
414 appropriate for predicting water content of the soils in our dataset. These French PTFs, however,  
415 did not necessarily perform better than those developed by Tóth et al. (2015) at the European scale.  
416 They did, however, perform better than those of Rawls et al. (1982), which were developed from  
417 soil samples from the USA, which appeared to be unsuitable (criteria among the worst for each PTF  
418 evaluated), except when using other water contents as predictors. The poor performance of the

419 French PTFs was not related to the ranges of soil properties in our dataset, because all of them fell  
420 within the domain of applicability of the PTFs tested. Moreover, a metric distance representing a  
421 PTF's domain of applicability, developed by Tranter et al. (2009), was calculated for two of the  
422 published PTFs whose training dataset was available (M9\_Co and M10\_Co). Overall, 97% of the  
423 data in our dataset belonged to the domain of applicability these PTFs, which confirmed that they  
424 could be applied to our dataset.

425 The poor prediction of water-retention curve parameters by parametric PTFs agrees with results  
426 of Ghorbani Dashtaki et al. (2010), who reported that parametric PTFs generally perform worse  
427 than point PTFs, as relations between water-retention curve parameters and basic soil properties are  
428 complex. The same basic soil properties do not necessarily describe the variability in water content  
429 in the wet range and the dry range of the curve, which makes it difficult to capture the relation with  
430 them (Tomasella et al., 2003; Ghorbani Dashtaki et al., 2010).

431 To predict water content better, some authors suggested including other water contents at given  
432 matric heads in the PTFs (Al Majou et al., 2008a; Rawls et al., 1982; Vereecken et al., 2010). In our  
433 study, predictions of such PTFs were slightly better than those of PTFs that included only soil  
434 properties, but with differences depending on the specific water content included in the PTF. As  
435 observed by Al Majou et al. (2008a), water content prediction improved when the other water  
436 content included was that at field capacity (in this case,  $\theta_{330}$ ), but not that at the wilting point  
437 ( $\theta_{15\ 000}$ ), as observed by Borgesen and Schaap (2005). The improvement in prediction when using  
438 the field capacity water content was related to the shape of soil water-retention curves, which  
439 inflected strongly near field capacity. However, determining water content at field capacity in order  
440 to include it in PTFs remains unsatisfactory, as doing so, mainly in laboratories, is time-consuming  
441 and costly. Other authors suggest that information on soil structure, which is often considered  
442 through bulk density, should be included to improve PTF performance. In the study of Al Majou et  
443 al. (2008b), including bulk density kept bias low and improved prediction of water content. In our

444 study, predictions of  $\theta_{330}$  had errors similar to or larger than those of Al Majou et al. (2008b), but  
445 unlike their results, including bulk density did not improve predictions. Soil bulk density in  
446 conservation tillage systems is generally higher than that in conventional systems, which results in  
447 lower total porosity than that in tilled soils but, conversely, generally higher saturated and near-  
448 saturated hydraulic conductivity (Green et al., 2003). While, bulk density is a good proxy of  
449 hydraulic dynamics (Blanco-Canqui et al., 2004; Alletto et al., 2010) and AWC in conventionally  
450 tilled soils, it is less effective in conservation agriculture (Alletto et al., 2010; Chen et al., 1998),  
451 probably due to greater pore connectivity and proportion of macro- and mesopores in the latter. This  
452 disconnection between hydraulic properties and bulk density in conservation agriculture can indeed  
453 be attributed to major changes in pore-size distribution and connectivity when tillage intensity is  
454 reduced (Strudley et al., 2008; Alletto et al., 2010), thus leading to changes in AWC. Furthermore,  
455 as mentioned by several authors (e.g., Nakano and Miyazaki, 2005; Lilly and Nemes, 2008), the  
456 cylindrical core method used to measure bulk density does not predict pore connectivity well, so  
457 complementary methods must be used to assess it.

#### 458 *4.2 Development of new pedotransfer functions*

459 Multiple linear regression is commonly used to develop PTFs (Wösten et al., 2001; Al  
460 Majou et al., 2008a; Tóth et al., 2015; Román Dobarco et al., 2019), unlike regression trees or  
461 random forests. Regression trees have been used to predict water content, but without considering  
462 cropping practices: Tóth et al. (2015) predicted  $\theta_{330}$  and  $\theta_{15\,000}$  using textural and taxonomic  
463 information (Table 1), while Rawls and Pachepsky (2002) did the same using textural and structural  
464 classes. To our knowledge, our study is the first to use random forests to predict water content. Vos  
465 et al. (2019) used random forests to highlight the influence of land use or land-use history classes,  
466 clay content and electrical conductivity on predicting topsoil carbon stock. In our study, random  
467 forests highlighted that some predictors not usually used in PTFs, such as CEC and rotation length,  
468 could help predict water content at a given matric head. Some properties have been suggested as

469 important for predicting water content due to an indirect influence, such as organic carbon, which  
470 plays both an indirect role, by improving soil structure, and a direct role, through its adsorption  
471 properties (Tóth et al., 2015). Cropping practices influence soil properties greatly, especially soil  
472 structure (Strudley et al., 2008), and can thus influence water content indirectly. Román Dobarco et  
473 al. (2019) suggest that land use should be considered in future PTFs, even though PTFs are  
474 generally suitable for most agricultural soils.

475         However, given the similar cross-validation performances of PTFs developed from random  
476 forests and multiple linear regression (which were even better than regression trees), our results do  
477 not support the hypothesis that cropping practices are essential for predicting water content in the  
478 topsoil (0-30 cm). We also set new parameters for two multiple linear regressions (M22\_Co and  
479 M28\_Co), developed by Román Dobarco et al. (2019), that were among the published PTFs that  
480 predicted best; thus, recalibrating existing PTFs rather than developing new ones may be sufficient.  
481 Finally, when we developed PTFs from regression trees and random forests without including  
482 cropping practices, we obtained nearly identical results.

483         In terms of quality of adjustment, random forests performed the best, with almost perfect  
484 fits. This was likely due to the nature of machine-learning methods, which “learn” from the dataset  
485 provided and thus perform well with it. Consequently, we also expected regression trees to have  
486 high quality of adjustment, but their results were similar to those of multiple linear regressions. This  
487 result was likely related to the pruning, as adjustment to the training data is purposely reduced so  
488 that the model performs better with a test dataset. In our study, however, performance of regression  
489 trees and random forests decreased between adjustment (i.e. the training dataset) and cross-  
490 validation (the test dataset) (Fig. 5). While the poor prediction by the regression trees can be  
491 explained easily by their well-known instability (i.e. a small difference in the training dataset can  
492 result in a different tree) (Gey and Poggi, 2006; Yang et al., 2016), the instability of the random  
493 forests was more surprising. Conversely, multiple linear regression was a stable method whose

494 quality of prediction was as good or better than that of the machine-learning methods. The  
495 similarity between its adjustment and cross-validation performances demonstrates its robustness.  
496 Overall, however, the cross-validation quality of prediction remained unsatisfactory in this study,  
497 mainly for  $EF_{CV}$ , which never reached satisfactory values for any of the PTFs despite having  
498 satisfactory  $ME_{CV}$  (close to 0).

499 In France, few water-retention data are available in conservation agriculture, and the small  
500 size of the dataset may have contributed to unsatisfactory predictions. Indeed, our study was located  
501 in a single French region and contained data for relatively few soils (140 samples from 61  
502 agricultural fields). The dataset thus may not represent the wide range of French soil diversity.  
503 Moreover, the lack of an independent dataset to validate the new PTFs led us to use cross  
504 validation, which estimated only the quality of prediction of the modelling approach. Indeed, as  
505 predicted parameter values of the PTFs changed for each soil, the structure of the model could not  
506 be tested. Cross validation revealed that even the highly performing random forest method was  
507 unstable, which may have resulted from the small sample size. Supplementing the scarce water-  
508 retention data would advance development of reliable tools for conservation agriculture. In  
509 particular, more data could have helped us better assess the quality of prediction of the PTFs  
510 developed. The unsuitability of basic soil properties for predicting water retention remains a major  
511 limitation in the development of PTFs (Vereecken et al., 2010). As demonstrated by the study, more  
512 relevant predictors of water retention still need to be identified, as using three methods to select the  
513 best predictors objectively still yielded unsatisfactory results.

## 514 **Conclusions**

515 We tested the performance of several published PTFs and newly developed PTFs using multiple  
516 linear regressions, regression trees and random forests to predict water content at field capacity ( $h =$   
517  $-100$  or  $-300$  cm) and wilting point ( $h = -15\ 000$  cm). Although some PTFs approached satisfactory  
518 performance according to the three criteria, none of them managed to reach it, which limits their use

519 in soil transport models for conservation agriculture. Most of our soil samples belonged to the  
520 domain of applicability of the PTFs, so the poor results obtained are likely related to (i) the use of  
521 unsuitable predictors, (ii) the use of PTFs developed at an inappropriate scale or (iii) differences in  
522 soil management between databases.

523 This study, the first to develop PTFs specifically calibrated for conservation agriculture,  
524 demonstrated that cropping practices were not necessary to predict water contents. The small size of  
525 our dataset was a major obstacle and probably partly explains the unsatisfactory performance of our  
526 PTFs, despite using methods designed to yield high performance. Future studies should use larger  
527 datasets of soils under conservation agriculture, at more locations, to verify the preliminary results  
528 of this study.

529 The machine-learning methods often selected CEC, which had not been used to develop the  
530 PTFs. However, because of low performance, even by random forests, the results suggest that the  
531 development of PTFs still lacks suitable predictors. Including more relevant soil properties when  
532 developing PTFs thus remains a research path for improving PTFs.

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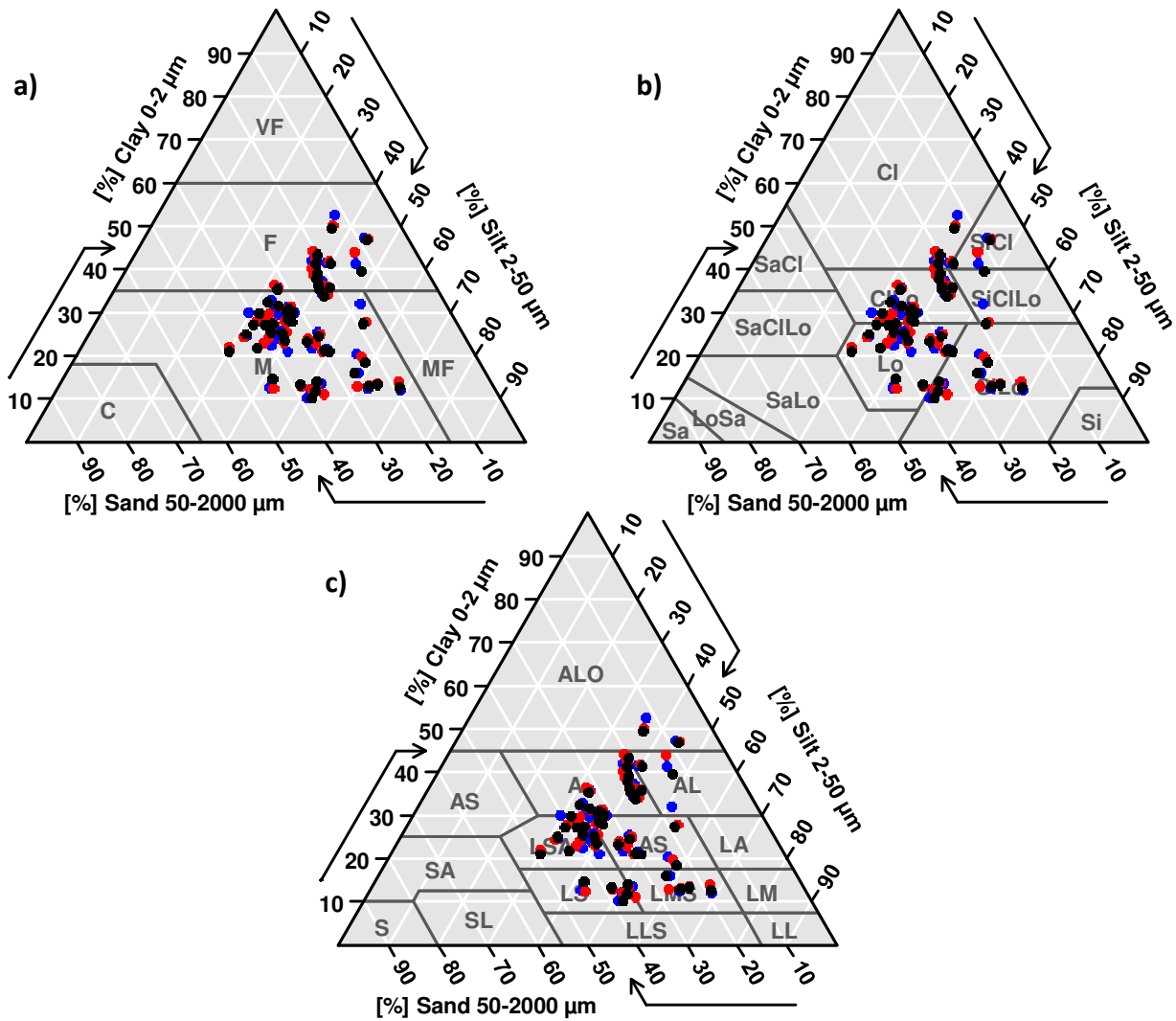
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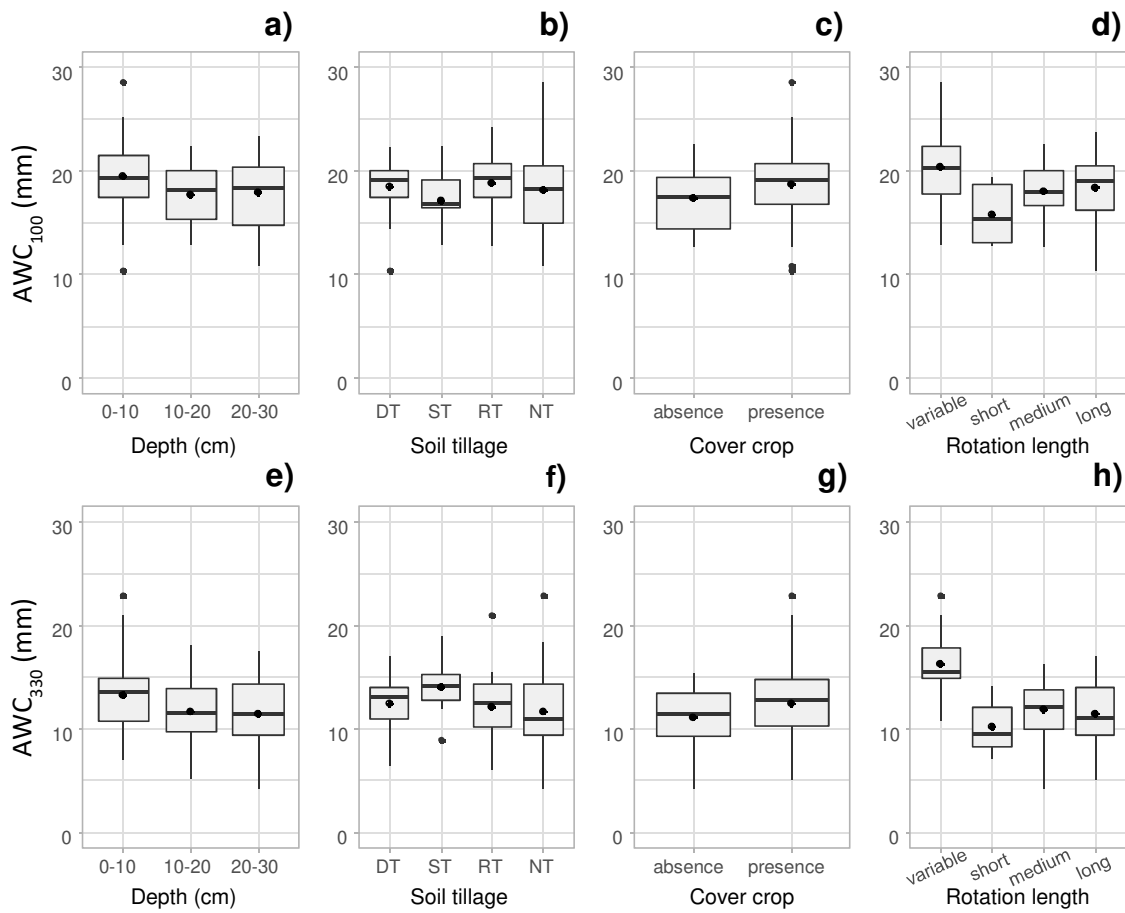
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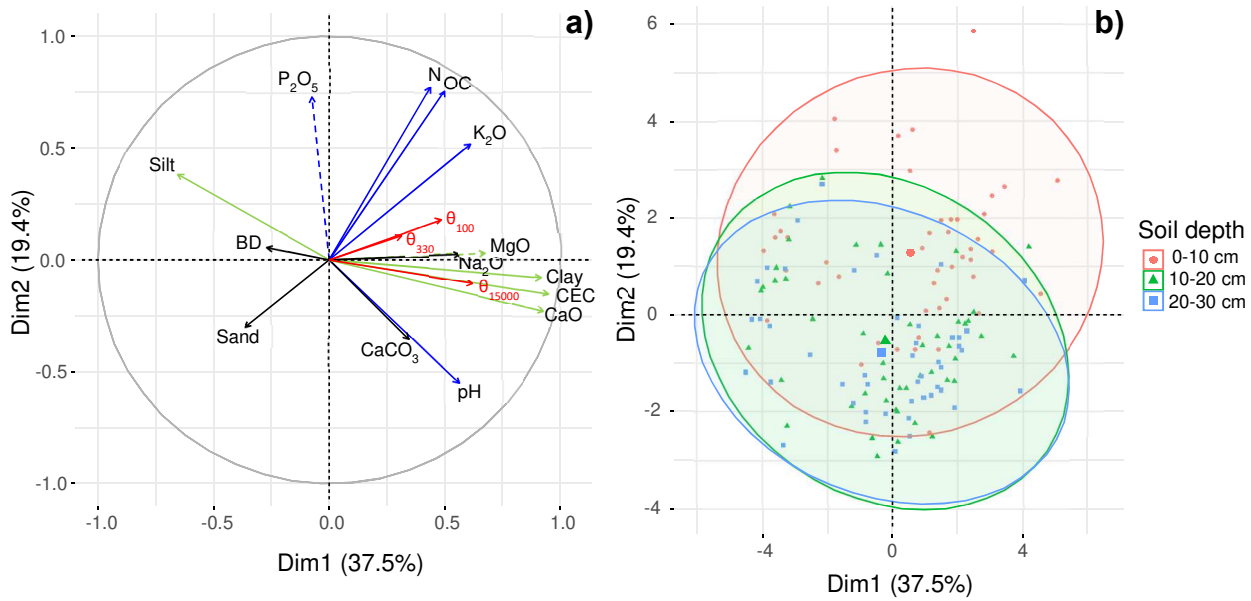


**Fig. 1.** Textures of the soil samples collected in 0-10, 10-20 and 20-30 cm deep soil layers (black, red and blue dots, respectively) in 61 conservation agriculture fields. The three texture triangles are based on the three classifications used to develop the pedotransfer functions found in the literature a) FAO, b) USDA and c) AISNE.

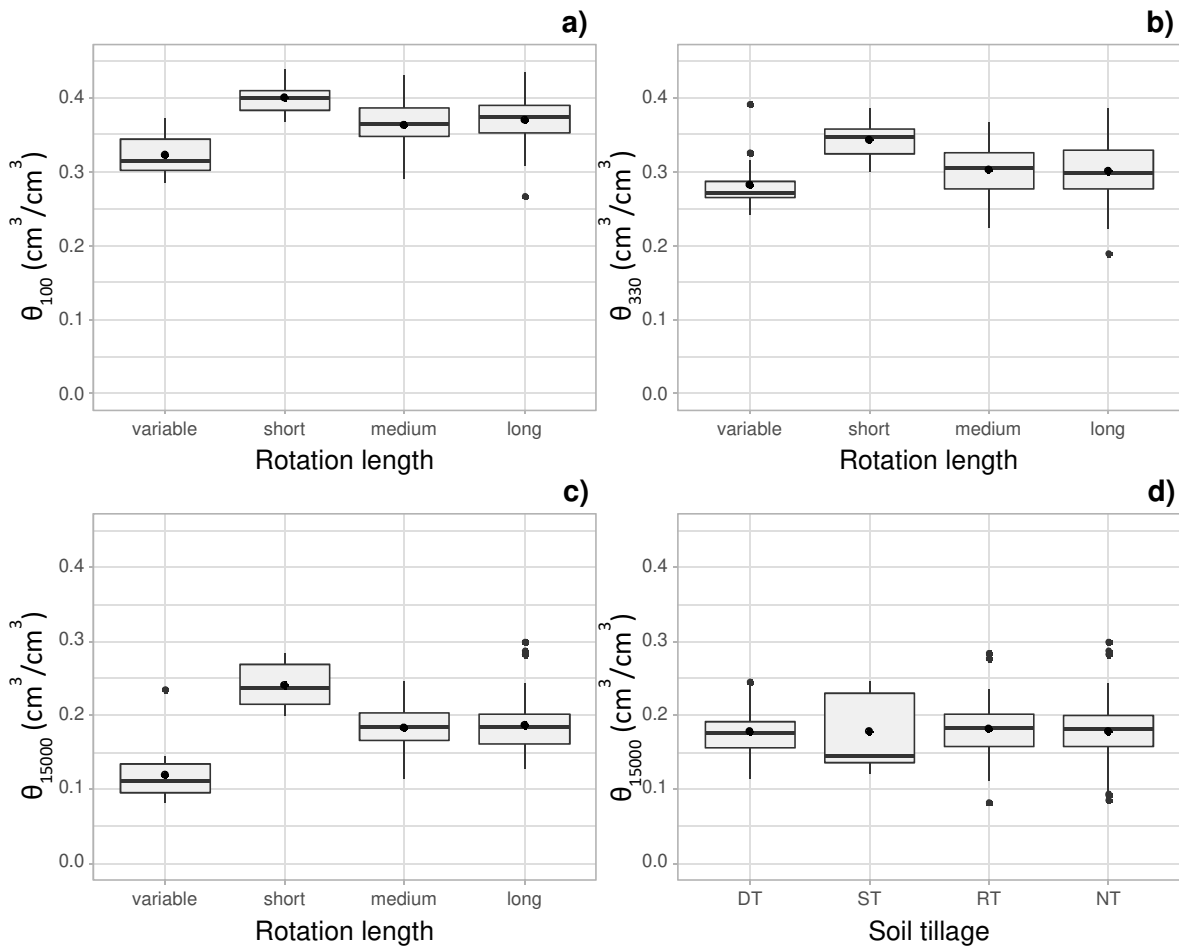


**Fig. 2.** Available water capacity (AWC) predicted assuming field capacity at a volumetric water content of -100 cm ( $AWC_{100}$ ) or -330 cm ( $AWC_{330}$ ) of matric head as a function of soil depth (a, e), soil tillage (b, f), cover-crop presence (c, g) and rotation length (d, h). For soil tillage, DT: deep tillage, RT: reduced tillage, ST: strip-till and NT: no tillage. For rotation length, variable: not fixed, short:  $\leq 2$  years, medium:  $> 2$  years &  $\leq 4$  years, long:  $> 4$  years.

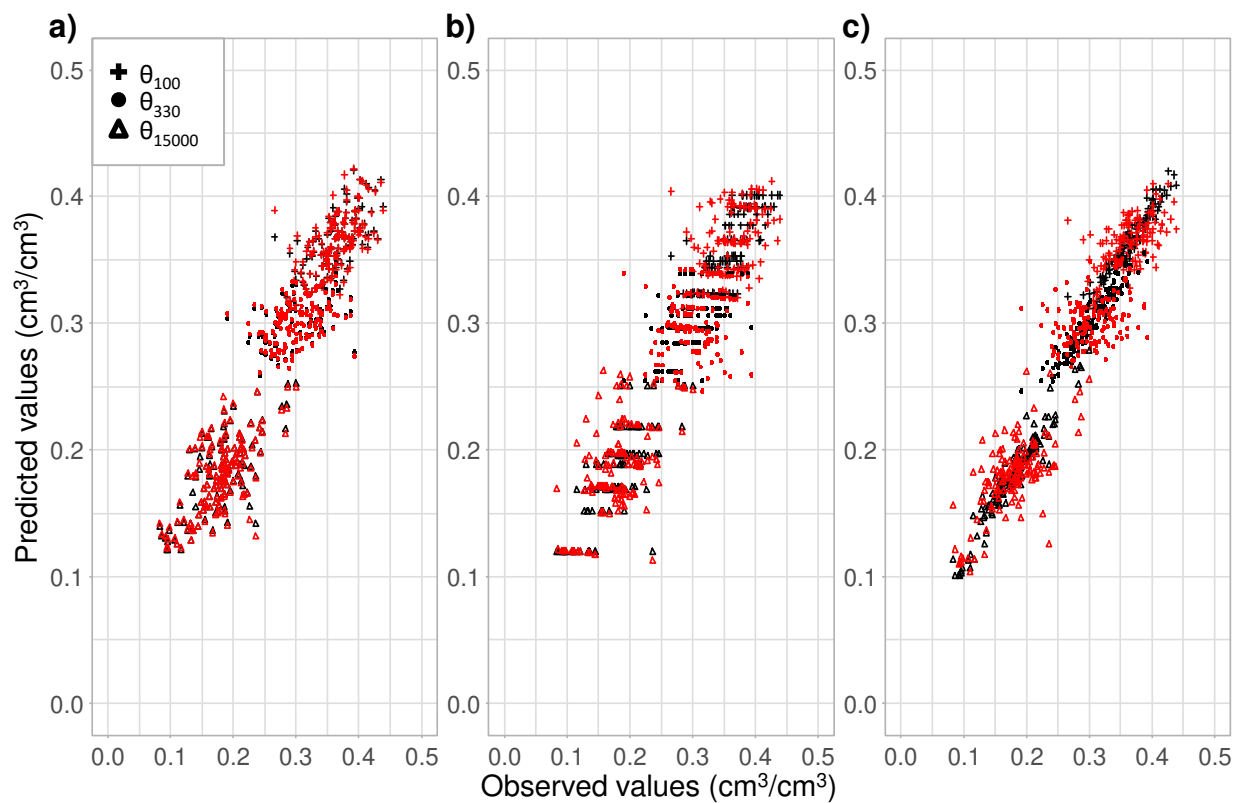




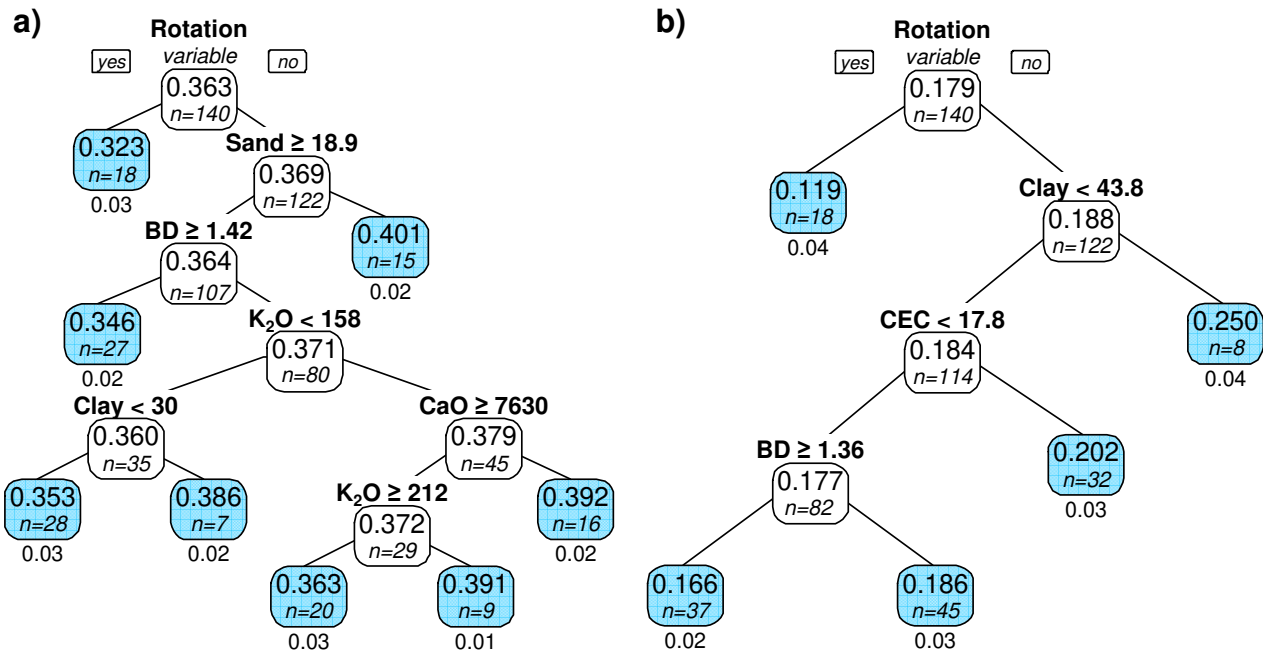
**Fig. 3.** Correlation circle of the (a) variables and (b) soil layers on the first two dimensions of the principal component analysis. (a) The variables that contributed significantly to the first and second axis are green and blue, respectively. Dashed arrows correspond to variables that did not contribute significantly to the first two axes. Black arrows correspond to variables that did not contribute significantly to any of the axes. Red arrows correspond to volumetric water contents at -100 cm ( $\theta_{100}$ ), -330 cm ( $\theta_{330}$ ) and -15 000 cm ( $\theta_{15000}$ ) of matric head, which were not used to construct the axes. (b) Soil layers are coloured by depth, circles represent 95% confidence interval ellipses and larger symbols are centroids.



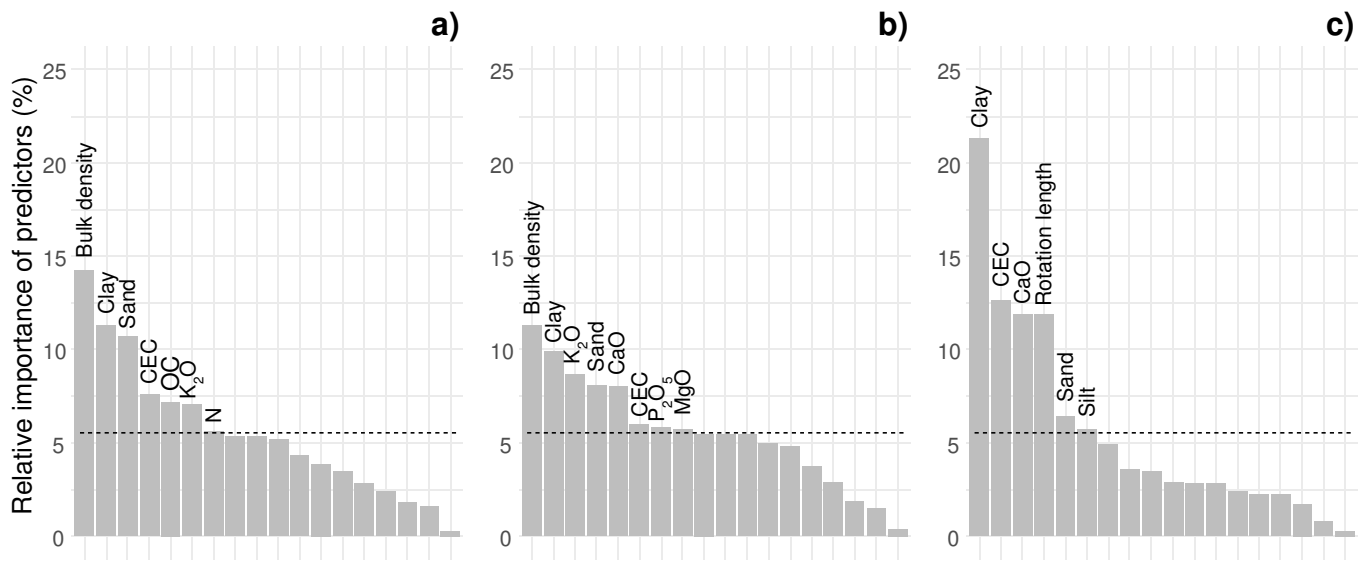
**Fig. 4.** Volumetric water content at (a) -100 cm ( $\theta_{100}$ ), (b) -330 cm ( $\theta_{330}$ ) and (c) -15 000 cm ( $\theta_{15000}$ ) of matric head as a function of rotation length (a, b, c) and (d) at -15 000 cm ( $\theta_{15000}$ ) as a function of soil tillage. For soil tillage, DT: deep tillage, RT: reduced tillage, ST: strip-till and NT: no tillage. For length of rotation, variable: not fixed, short:  $\leq 2$  years, medium:  $> 2$  years &  $\leq 4$  years, long:  $> 4$  years.



**Fig. 5.** Observed vs. predicted soil water content at -100 cm ( $\theta_{100}$ ), -330 cm ( $\theta_{330}$ ) and -15 000 cm ( $\theta_{15000}$ ) of matric head for (a) multiple linear regression, (b) regression tree and (c) random forest. Predicted adjustment values and cross-validation values are black and red, respectively.



**Fig. 6.** Regression trees for the prediction of (a)  $\theta_{100}$  and (b)  $\theta_{15\,000}$ . BD is bulk density ( $\text{g}/\text{cm}^3$ ), CEC is cation exchange capacity ( $\text{cmol}/\text{kg}$ ) and CaO and  $\text{K}_2\text{O}$  are exchangeable calcium and potassium ( $\text{mg}/\text{kg}$ ), respectively. Values in boxes are mean water contents ( $\text{cm}^3/\text{cm}^3$ ) of the  $n$  samples in the partition. The values below terminal leaves (blue boxes) are standard deviations.



**Fig. 7.** Relative importance (%) of predictors in random forests of (a)  $\theta_{100}$ , (b)  $\theta_{330}$  and (c)  $\theta_{15000}$ . Dashed lines represent the mean relative importance; only predictors above the mean are labelled. CEC is cation exchange capacity; CaO,  $K_2O$  and MgO are exchangeable calcium, potassium and magnesium, respectively;  $P_2O_5$ , OC and N are phosphorus, organic carbon and nitrogen content, respectively.

**Table 1.** Published pedotransfer functions (PTFs) used to predict soil volumetric water content ( $\text{cm}^3/\text{cm}^3$ ) at a given matric head  $h=-100$  cm,  $\theta_{100}$ ,  $h=-330$  cm,  $\theta_{330}$ , and  $h=-15\ 000$  cm,  $\theta_{15\ 000}$ . Cl, Si, OC and OM are contents (%) of clay, silt, organic carbon and organic matter, respectively.  $\text{OC}^*=\text{OC}+1$ . BD is bulk density ( $\text{g}/\text{cm}^3$ ). Co: continuous-PTFs, Cl: class-PTFs, Tr: tree-PTFs. When two PTFs are indicated in the PTF ID column, the first does not consider topsoil/subsoil separation, and the second considers only the topsoil.

Reference	Sampling location	N	Predictive variables / Equation	Variables predicted	PTF ID
Rawls et al. (1982)	USA, 32 states	5350	$\theta_h = a + (b \times \text{Sa}) + (c \times \text{Si}) + (d \times \text{Cl}) + (e \times \text{OM}) + (f \times \text{BD})$	$\theta_{40}, \theta_{70}, \theta_{100}, \theta_{200},$	M1_Co
			$\theta_h = a + (b \times \text{Sa}) + (c \times \text{Si}) + (d \times \text{Cl}) + (e \times \text{OM}) + (f \times \text{BD}) + (h \times \theta_{15\ 000})$	$(\theta_{330}), \theta_{600}, \theta_{4000},$ $\theta_{7000}, \theta_{10000},$	M2_Co
			$\theta_h = a + (b \times \text{Sa}) + (c \times \text{Si}) + (d \times \text{Cl}) + (e \times \text{OM}) + (f \times \text{BD}) + (g \times \theta_{330}) + (h \times \theta_{15\ 000})$	$(\theta_{15\ 000})$	M3_Co
Bruand et al. (2004)	France, Paris basin	340	- texture AISNE (topsoil function)	$\theta_{10}, \theta_{33}, \theta_{100}, \theta_{330},$ $\theta_{1000}, \theta_{3300}, \theta_{15\ 000}$	M4_Cl
Al Majou et al. (2007)	France, Paris basin	320	- texture FAO (topsoil function)		M5_Cl   M6_Cl
			- texture FAO (topsoil function)	$\theta_{10}, \theta_{33}, \theta_{100}, \theta_{330},$ $\theta_{1000}, \theta_{3300}, \theta_{15\ 000}$	M7_Cl   M8_Cl
			- bulk density $-\theta_h = a + (b \times \text{Cl}) + (c \times \text{Si}) + (d \times \text{OC}) + (e \times \text{BD})$ (topsoil function)		M9_Co   M10_Co
Al Majou et al. (2008b)	France, Paris basin, Brittany, the western coastal marshlands and the Pyrenean piedmont plain	456	- texture FAO (topsoil function)		M11_Cl   M12_Cl
			- texture FAO (topsoil function)	$\theta_{10}, \theta_{33}, \theta_{100}, \theta_{330},$ $\theta_{1000}, \theta_{3300}, \theta_{15\ 000}$	M13_Cl   M14_Cl
			- bulk density		
Tóth et al. (2015)	18 European countries	18 537	- texture FAO & topsoil/subsoil		M15_Tr
			- texture USDA & topsoil/subsoil		M16_Tr
			$\theta_{330} = a_1 - (b_1 \times \text{OC}^{*-1}) + (c_1 \times \text{Cl}) + (d_1 \times \text{Si}) + (e_1 \times \text{Si} \times \text{OC}^{*-1}) - (f_1 \times \text{Si} \times \text{Cl}) + (g_1 \times \text{Cl} \times \text{OC}^{*-1})$ $\theta_{15\ 000} = a_2 + (b_2 \times \text{Cl}) - (c_2 \times \text{Si}) - (d_2 \times \text{OC}^{*-1}) + (e_2 \times \text{Si} \times \text{Cl}) + (f_2 \times \text{Cl} \times \text{OC}^{*-1}) + (g_2 \times \text{Si} \times \text{OC}^{*-1})$	$\theta_{330}, \theta_{15\ 000}$	M17_Co
Roman Dobarco et al. (2019)	France, northern half of the country, with little representation of more mountainous southern and eastern regions	689	- texture FAO (topsoil function)		M18_Cl   M19_Cl
			- texture FAO (topsoil function)		M20_Cl   M21_Cl
			- bulk density $\theta_h = a + (b \times \text{Cl}) + (c \times \text{Sa})$ (topsoil function)	$\theta_{100}, \theta_{330}, \theta_{15\ 000}$	M22_Co   M26_Co
			$\theta_h = a + (b \times \text{Cl}) + (c \times \text{Sa}) + (d \times \text{OC})$ (topsoil function)		M23_Co   M27_Co
			$\theta_h = a + (b \times \text{Cl}) + (c \times \text{Sa}) + (e \times \text{BD})$ (topsoil function)		M24_Co   M28_Co
			$\theta_h = a + (b \times \text{Cl}) + (c \times \text{Sa}) + (d \times \text{OC}) + (e \times \text{BD})$ (topsoil function)		M25_Co   M29_Co

**Table 2.** Published pedotransfer functions (PTFs) used to evaluate the quality of prediction of the van Genuchten's water-retention curve parameters  $\theta_s$ ,  $\alpha$  and  $n$ . Cl, Si, OC and OM are contents (%) of clay, silt, organic carbon and organic matter, respectively.  $OC^*=OC+1$ . BD is bulk density ( $g/cm^3$ ), CEC is cation exchange capacity (cmol/kg), T/S is topsoil/subsoil (T=1, S=0).  $\theta_s$  is volumetric water content at saturation,  $\alpha$  and  $n$  are shape parameters of van Genuchten's water retention curve.

Reference	Sampling location	Number of samples	Predictive variables / Equation	Predicted variables	PTF ID
Wösten et al. (1999)	12 European countries	4030	- texture FAO		P1_Cl
			$\theta_s = a_1 + (b_1 \times Cl) - (c_1 \times BD) - (d_1 \times Si^2) + (e_1 \times OM^2) + (f_1 \times Cl^{-1}) + (g_1 \times Si^{-1}) + (h_1 \times \ln(Si)) - (i_1 \times OM \times Cl) - (j_1 \times BD \times Cl) - (k_1 \times BD \times OM) - (l_1 \times T/S \times Si)$ $\ln(\alpha) = -a_2 + (b_2 \times Cl) + (c_2 \times Si) + (d_2 \times OM) + (e_2 \times BD) - (f_2 \times T/S) - (g_2 \times BD^2) - (h_2 \times Cl^2) - (i_2 \times (OM^2)) + (j_2 \times OM^{-1}) + (k_2 \times \ln(Si)) + (l_2 \times \ln(OM)) - (m_2 \times BD \times Si) - (n_2 \times BD \times OM) + (o_2 \times T/S \times Cl)$ $\ln(n-1) = -a_3 - (b_3 \times Cl) + (c_3 \times Si) - (d_3 \times OM) + (e_3 \times BD) - (f_3 \times (BD^2)) + (g_3 \times (Cl^2)) + (h_3 \times (OM^2)) - (i_3 \times BD^{-1}) - (j_3 \times Si^{-1}) - (k_3 \times OM^{-1}) - (l_3 \times \ln(Si)) - (m_3 \times \ln(OM)) - (n_3 \times \ln(BD)) - (o_3 \times BD \times Cl) + (p_3 \times BD \times OM) + (q_3 \times T/S \times Cl)$	P2_Co	
Al Majou et al. (2008a)	France, Paris basin	320	- texture FAO		P3_Cl
			$\theta_s = a_1 - (b_1 \times Cl) - (c_1 \times BD) + (d_1 \times Si^2) - (e_1 \times OC^2) + (f_1 \times Cl^{-1}) + (g_1 \times Si^{-1}) - (h_1 \times \ln(Si)) + (i_1 \times OC \times Cl) + (j_1 \times BD \times Cl) - (k_1 \times BD \times OC) - (l_1 \times Si)$ $\ln(\alpha) = a_2 + (b_2 \times Cl) + (c_2 \times Si) + (d_2 \times OC) + (e_2 \times BD) - (f_2 \times BD^2) - (g_2 \times Cl^2) - (h_2 \times OC^2) - (i_2 \times OC^{-1}) - (j_2 \times \ln(Si)) - (k_2 \times \ln(OC)) - (l_2 \times BD \times Si) - (m_2 \times BD \times OC)$ $\ln(n-1) = -a_3 - (b_3 \times Cl) + (c_3 \times Si) - (d_3 \times OC) + (e_3 \times BD) - (f_3 \times BD^2) + (g_3 \times Cl^2) + (h_3 \times OC^2) + (i_3 \times BD^{-1}) + (j_3 \times Si^{-1}) + (k_3 \times OC^{-1}) - (l_3 \times \ln(Si)) + (m_3 \times \ln(OC)) - (n_3 \times \ln(BD)) + (o_3 \times BD \times Cl) + (p_3 \times BD \times OC)$	P4_Co	
Tóth et al (2015)	18 European countries	18 537	- texture FAO		$\theta_s, \alpha, n$ P5_Cl
			- texture USDA		P6_Cl
			$\theta_s = 0.5056 - (0.1437 \times 1/(OC+1)) + (0.0004152 \times Si)$ $\log_{10}(\alpha) = -1.3050 - (0.0006123 \times Si) - (0.009810 \times Cl) + (0.07611 \times 1/(OC^*)) - (0.0004508 \times Si \times Cl) + (0.03472 \times Cl \times 1/(OC^*)) - (0.01226 \times Si \times 1/(OC+1))$ $\log_{10}(n-1) = 0.01516 - (0.005775 \times 1/OC^*) - (0.24885 \times \log_{10}(CEC)) - (0.01918 \times Cl) - (0.0005052 \times Si) - (0.007544 \times pH^2) - (0.02159 \times Cl \times 1/OC^*) + (0.01556 \times Cl \times \log_{10}(CEC)) + (0.01477 \times 1/OC^* \times pH^2) + (0.0001121 \times Si \times Cl) - (0.33198 \times 1/OC^* \times \log_{10}(CEC))$	P7_Co	
			$\theta_s = 0.83080 - (0.28217 \times BD) + (0.0002728 \times Cl) + (0.000187 \times Si)$ $\log_{10}(\alpha) = -0.43348 - (0.41729 \times BD) - (0.04762 \times OC) + (0.21810 \times T/S) - (0.01581 \times Cl) - (0.01207 \times Si)$ $\log_{10}(n-1) = 0.22236 - (0.30189 \times BD) - (0.05558 \times T/S) - (0.005306 \times Cl) - (0.003084 \times Si) - (0.01072 \times OC)$	P8_Co	
			$\theta_s = 0.63052 - (0.10262 \times BD^2) + (0.0002904 \times pH^2) + (0.0003335 \times Cl)$ $\log_{10}(\alpha) = -1.16518 + (0.40515 \times 1/OC^*) - (0.16063 \times BD^2) - (0.008372 \times Cl) - (0.01300 \times Si) + (0.002166 \times pH^2) + (0.08233 \times T/S)$ $\log_{10}(n-1) = -0.25929 + (0.25680 \times 1/OC^*) - (0.10590 \times BD^2) - (0.009004 \times Cl) - (0.001223 \times Si)$	P9_Co	

**Table 3.** Summary statistics of particle size fractions (%), organic carbon (OC; %), nitrogen content (g/kg), bulk density (BD; g/cm<sup>3</sup>), cation exchange capacity (CEC; cmol/kg), exchangeable CaO, MgO, K<sub>2</sub>O, Na<sub>2</sub>O (mg/kg), pH, total calcium carbonate CaCO<sub>3</sub> (g/kg), phosphorus content P<sub>2</sub>O<sub>5</sub> (mg/kg) and volumetric water content at field capacity,  $\theta_{100}$  and  $\theta_{330}$ , and at wilting point,  $\theta_{15\ 000}$  (cm<sup>3</sup>/cm<sup>3</sup>) of the dataset used to evaluate published pedotransfer functions (PTFs) and develop new PTFs

N=140	Clay	Silt	Sand	OC	N	BD	CEC	CaO	MgO	K <sub>2</sub> O	Na <sub>2</sub> O	pH	CaCO <sub>3</sub>	P <sub>2</sub> O <sub>5</sub>	$\theta_{100}$	$\theta_{330}$	$\theta_{15\ 000}$
Mean	27.8	42.2	30.0	1.0	1.1	1.4	13.2	6700	236.0	189.3	13.4	7.6	41.0	35.2	0.363	0.301	0.179
Standard deviation	10.1	9.1	9.0	0.3	0.3	0.1	5.6	3274	135.6	103.3	6.1	0.9	54.1	29.1	0.035	0.037	0.042
Min	10.3	29.4	8.0	0.5	0.6	1.2	3.5	540	47.2	27.8	4.3	5.1	0.0	3.0	0.266	0.190	0.083
Median	28.0	39.1	31.9	1.0	1.0	1.4	13.4	6966	211.4	171.2	12.2	8.1	19.0	27.0	0.364	0.298	0.182
Max	52.6	68.7	49.0	2.2	2.2	1.7	24.6	13057	595.4	522.8	35.7	8.7	220.0	147.0	0.439	0.392	0.300



**Table 4.** Statistical criteria for the prediction of  $\theta_{100}$ ,  $\theta_{330}$  and  $\theta_{15\,000}$ . RMSE<sub>P</sub>: root mean squared error of prediction, ME<sub>P</sub>: mean error of prediction, EF<sub>P</sub>: Nash-Sutcliffe Efficiency of prediction. Co: continuous-PTFs, Cl: class-PTFs, Tr: tree-PTFs. 0.000 means  $< 1.10^{-3}$

PTF	$\theta_{100}$ (cm <sup>3</sup> /cm <sup>3</sup> )			$\theta_{330}$ (cm <sup>3</sup> /cm <sup>3</sup> )			$\theta_{15\,000}$ (cm <sup>3</sup> /cm <sup>3</sup> )		
	RMSE <sub>P</sub>	ME <sub>P</sub>	EF <sub>P</sub>	RMSE <sub>P</sub>	ME <sub>P</sub>	EF <sub>P</sub>	RMS E <sub>P</sub>	ME <sub>P</sub>	EF <sub>P</sub>
M1_Co	0.089	0.078	-5.68	0.073	0.049	-2.84	0.047	0.017	-0.29
M2_Co	0.262	0.259	-56.75	0.059	0.047	-1.53	-	-	-
M3_Co	0.034	-0.007	0.03	-	-	-	-	-	-
M4_Cl	0.065	-0.056	-2.24	0.037	-0.014	-0.11	0.040	-0.027	0.17
M5_Cl	0.056	-0.042	-1.60	0.042	-0.007	-0.28	0.044	0.003	-0.14
M6_Cl	0.052	-0.039	-1.26	0.038	0.002	-0.02	0.046	-0.013	-0.24
M7_Cl	0.049	-0.028	-1.01	0.045	0.001	-0.47	0.051	-0.004	-0.50
M8_Cl	0.042	-0.029	-0.48	0.038	0.009	-0.02	0.044	-0.01	-0.13
M9_Co	0.053	-0.044	-1.36	0.047	-0.025	-0.59	0.043	-0.023	-0.08
M10_Co	0.116	-0.112	-10.40	0.080	-0.069	-3.59	0.057	-0.045	-0.87
M11_Cl	0.057	-0.043	-1.73	0.042	-0.007	-0.28	0.045	0.011	-0.20
M12_Cl	0.049	-0.030	-1.04	0.043	0.009	-0.31	0.049	0.011	-0.38
M13_Cl	0.046	-0.028	-0.78	0.043	0.003	-0.31	0.050	0.008	-0.45
M14_Cl	0.039	-0.019	-0.30	0.044	0.017	-0.35	0.052	0.017	-0.56
M15_Tr	-	-	-	0.043	0.022	-0.33	0.045	-0.015	-0.20
M16_Tr	-	-	-	0.054	0.036	-1.07	0.042	0.001	-0.03
M17_Co	-	-	-	0.045	0.025	-0.45	0.036	0.000	0.23
M18_Cl	0.059	-0.045	-1.88	0.047	0.001	-0.57	0.050	0.018	-0.48
M19_Cl	0.051	-0.033	-1.20	0.041	0.014	-0.24	0.047	0.010	-0.29
M20_Cl	0.048	-0.031	-0.95	0.052	0.018	-0.91	0.056	0.020	-0.80
M21_Cl	0.042	-0.025	-0.50	0.041	0.016	-0.23	0.049	0.013	-0.37
M22_Co	0.066	-0.057	-2.63	0.04	0.005	-0.16	0.034	0.003	0.31
M23_Co	0.061	-0.051	-2.08	0.046	-0.011	-0.51	0.035	0.003	0.29
M24_Co	0.055	-0.046	-1.54	0.041	-0.001	-0.22	0.035	0.001	0.30
M25_Co	0.055	-0.045	-1.51	0.042	-0.002	-0.28	0.036	0.001	0.25
M26_Co	0.059	-0.048	-1.89	0.043	-0.007	-0.33	0.036	0.002	0.23
M27_Co	0.065	-0.056	-2.52	0.044	-0.016	-0.37	0.036	-0.002	0.25
M28_Co	0.060	-0.049	-2.02	0.042	-0.005	-0.25	0.036	0.002	0.24
M29_Co	0.074	-0.064	-3.55	0.048	-0.022	-0.65	0.038	-0.007	0.16

**Table 5.** Statistical criteria for the prediction of  $\theta_s$ ,  $\alpha$  and  $n$  parameters.  $RMSE_P$ : root mean squared error of prediction,  $ME_P$ : mean error of prediction,  $EF_P$ : Nash-Sutcliffe efficiency of prediction. Co: continuous-PTFs, Cl: class-PTFs

PTF	$\theta_s$ (cm <sup>3</sup> /cm <sup>3</sup> )			$\alpha$ (cm <sup>-1</sup> )			$n$ (-)		
	$RMSE_P$	$ME_P$	$EF_P$	$RMSE_P$	$ME_P$	$EF_P$	$RMSE_P$	$ME_P$	$EF_P$
P1_Cl	0.054	0.029	-2.05	0.232	-0.018	-0.01	0.331	-0.132	-0.23
P2_Co	0.439	-0.438	-198.53	0.232	-0.019	0.00	0.333	-0.110	-0.25
P3_Cl	0.038	0.010	-0.49	0.506	0.441	-3.78	0.361	-0.201	-0.47
P4_Co	0.376	-0.373	-144.92	-	-	-	0.366	-0.197	-0.51
P5_Cl	0.046	0.033	-1.14	0.232	-0.017	-0.01	0.326	-0.119	-0.19
P6_Cl	0.05	0.036	-1.59	0.232	0.012	0.00	0.339	-0.125	-0.29
P7_Co	0.037	0.019	-0.41	0.234	-0.036	-0.02	0.325	-0.068	-0.19
P8_Co	0.035	0.029	-0.27	0.233	-0.033	-0.02	0.305	0.003	-0.04
P9_Co	0.038	0.033	-0.56	0.234	-0.035	-0.02	0.316	-0.051	-0.12

**Table 6.** Multiple linear regression coefficients for estimating  $\theta_{100}$ ,  $\theta_{330}$  and  $\theta_{15\ 000}$  from the non-stratified dataset and the dataset for the top and bottom soil layers.  $\theta$  is the soil volumetric water content ( $\text{cm}^3/\text{cm}^3$ ) at a given matric head. Clay: clay content (%), Silt: silt content (%), Sand: sand content (%), BD: bulk density ( $\text{g}/\text{cm}^3$ ), N: nitrogen content ( $\text{g}/\text{kg}$ ), CEC: cation exchange capacity ( $\text{cmol}/\text{kg}$ ) and  $\text{P}_2\text{O}_5$ : phosphorus content ( $\text{mg}/\text{kg}$ )

<b><math>\theta_{100} = a + b \times \text{Clay} + c \times \text{BD} + d \times \text{Silt} + e \times \text{N} + f \times \text{Sand}</math></b>						
	Intercept	Clay	BD	Silt	N	Sand
Coefficients	-9.809	$1.04 \times 10^{-1}$	$-1.24 \times 10^{-1}$	$1.03 \times 10^{-1}$	$2.37 \times 10^{-2}$	$1.02 \times 10^{-1}$
<b><math>\theta_{330} = a + b \times \text{Clay} + c \times \text{BD} + d \times \text{CEC} + e \times \text{P}_2\text{O}_5</math></b>						
	Intercept	Clay	BD	CEC	$\text{P}_2\text{O}_5$	
Coefficients	0.386	$2.54 \times 10^{-3}$	$-9.27 \times 10^{-2}$	$-2.71 \times 10^{-3}$	$1.72 \times 10^{-4}$	
<b><math>\theta_{15\ 000} = a + b \times \text{Clay} + c \times \text{BD} + d \times \text{pH} + e \times \text{Silt}</math></b>						
	Intercept	Clay	BD	pH	Silt	
Coefficients	0.145	$2.56 \times 10^{-3}$	$-8.56 \times 10^{-2}$	$7.00 \times 10^{-3}$	$6.24 \times 10^{-4}$	

**Table 7.** Statistical criteria (root mean squared error (RMSE, cm<sup>3</sup>/cm<sup>3</sup>), mean error (ME, cm<sup>3</sup>/cm<sup>3</sup>) and Nash-Sutcliffe efficiency (EF)) of the quality of adjustment (subscript <sub>A</sub>) or cross validation (subscript <sub>CV</sub>) for the prediction of  $\theta_{100}$ ,  $\theta_{330}$  and  $\theta_{15\ 000}$  by new pedotransfer functions developed from the non-stratified dataset and datasets of the top and bottom soil layers. Values less than 0.001 are expressed as 0.

Criterion	Multiple linear regression			Regression tree			Random forest		
	$\theta_{100}$	$\theta_{330}$	$\theta_{15\ 000}$	$\theta_{100}$	$\theta_{330}$	$\theta_{15\ 000}$	$\theta_{100}$	$\theta_{330}$	$\theta_{15\ 000}$
RMSE <sub>A</sub>	0.026	0.033	0.029	0.024	0.037	0.028	0.012	0.016	0.013
ME <sub>A</sub>	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
EF <sub>A</sub>	0.44	0.21	0.49	0.52	0.00	0.55	0.88	0.83	0.90
RMSE <sub>CV</sub>	0.028	0.035	0.032	0.034	0.038	0.037	0.027	0.036	0.031
ME <sub>CV</sub>	0.000	0.000	0.000	0.000	0.000	0.003	0.000	0.000	0.000
EF <sub>CV</sub>	0.34	0.14	0.41	0.01	-0.03	0.21	0.36	0.05	0.45