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To cite this version:

Douadia Bougherara, Lana Friesen, Céline Nauges. Risk Taking with Left- and Right-Skewed Lotteries. Journal of Risk and Uncertainty, 2021, 62 (1), pp.89-112. $10.1007 \text{/} s11166-021-09345-w$. hal-03219533

HAL Id: hal-03219533 <https://hal.inrae.fr/hal-03219533v1>

Submitted on 10 Aug 2024

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Risk Taking with Left- and Right-Skewed Lotteries*

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April 2020

Abstract: While much literature has focused on preferences regarding risk, preferences over skewness also have significant economic implications. An important and understudied aspect of skewness preferences is how they affect risk taking. In this paper, we design a novel laboratory experiment that elicits certainty equivalents over lotteries where the variance and skewness of the outcomes are orthogonal to each other. This design enables us to cleanly measure both skewness seeking/avoiding and risk taking behavior, and their interaction, without needing to make parametric assumptions. Our experiment includes both left- and right-skewed lotteries. The results reveal that the majority of subjects are skewness avoiding risk takers who correspondingly also take more risk when facing less skewed lotteries. Our second contribution is to link these choices to individual rank-dependent utility preference parameters estimated using a separate lottery choice protocol. Using a latent-class model, we are able to identify two classes of subjects: skewness avoiders with the classic inverse s-shaped probability weighting function and skewness neutral subjects that do not distort probabilities. Our results thus demonstrate the link between probability distortion and skewness seeking/avoidance choices. They also highlight the importance of accounting for individual heterogeneity.

Keywords: Risk; Skewness; Laboratory Experiment; Probability Weighting

JEL classification: C91; D81

* We thank Jean-Marc Rousselle for assistance in programming and running the experiment, and Olivier L'Haridon for sharing his experimental instructions (in French) on certainty equivalent elicitation. We are also grateful for helpful comments provided by conference and seminar audiences at the Toulouse School of Economics, the BEST Conference on Human Behavior and Decision Making, and the UQ BESC social sciences workshop. Finally Céline Nauges acknowledges funding from the French National Research Agency (ANR) under the Investments for the Future (Investissements d'Avenir) program, grant ANR-17- EURE-0010.

1. Introduction

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While much literature has focused on preferences regarding risk, preferences over skewness also have important economic implications. Skewness seeking, for example, can explain the overpricing and less than average returns of (right-) skewed securities (Barberis, 2013), overinvestment in winner-take-all careers and the high rates of small business failures, the attraction of lotteries (Garrett and Sobel, 1999), and even the well-known "favorite – long shot bias" where people overprice long shots and underprice favorites (Golec and Tamarkin, 1998).

An important and understudied aspect of skewness preferences is how they affect risk taking. That is, are people more or less willing to take risk when facing more skewed outcomes? Answering this question is important for many economic decisions. For example, people may purchase less insurance as skewness increases if they are more willing to take risks, and new crop varieties that reduce downside risk (i.e. technologies that reduce the probability of crop failure) may affect farmers' willingness to adopt new technologies and seeds, or to buy insurance.¹

To study how the skewness of outcomes affects risk taking we design a novel laboratory experiment that elicits certainty equivalents over lotteries where the variance and skewness of the outcomes are orthogonal to each other. Our design enables us to cleanly measure both skewness seeking/avoiding and risk taking behavior, and their interaction, without needing to make parametric assumptions. An important part of our design is the inclusion of both right- and left-skewed lotteries, with the latter less commonly studied. However, left skewness is a feature in many important economic decisions such as financial markets, agricultural production, insurance risks, health outcomes, employment income, and so on. In these situations, there is a

¹ New agricultural technologies will generally change both the skewness and variance of crop yields (e.g., Chavas and Shi, 2015, or Emerick et al., 2016).

small likelihood of very unfavorable outcomes such as negative profits, unemployment, serious illness, etc. As Barberis (2013, p.182) describes, while some individual securities are rightskewed, "the aggregate stock market is negatively skewed: it is subject to occasional large crashes". Increasing global connectivity magnifies these potential financial risks as exemplified by the recent global stock market crash associated with the coronavirus (COVID-19) pandemic. Similarly, the threat of climate changes brings an increased likelihood of extremely bad (catastrophic even) outcomes (e.g. Hanemann et al., 2016).

The most common pattern we observe in our experiment is skewness avoidance and risk taking, which is particularly prevalent when considering lotteries with the same direction of skewness (i.e. all left- or all right-skewed). Correspondingly, subjects also take more risk when facing less skewed lotteries. Nevertheless, we observe considerable heterogeneity in behavior. Our second novel contribution is to link these behaviors to individual structural risk preference parameters estimated using a separate lottery choice task. This allows us to investigate the role of individual heterogeneity, particularly utility curvature and probability weighting, in a manner that previous studies have only hinted at. For this purpose, we use the Harrison and Rutström (2009) protocol, which is specifically designed to measure individual risk preference parameters. For each subject, we estimate their utility curvature and probability weighting parameters in the rank-dependent utility (RDU) model (Quiggin, 1982). We find two classes of subjects: skewness avoiders who have an inverse s-shaped probability weighting function, and skewness neutral subjects that do not distort probabilities.² Our results are the first to demonstrate the relationship

 2 Subjects characterized by an inverse s-shaped probability weighting function overweight small probabilities and underweight large probabilities.

between skewness seeking/avoiding and probability distortion at the individual level.³

We are only aware of three other studies that investigate how skewness affects risk taking behavior. Grossman and Eckel (2015) use a variation of their Eckel and Grossman (2002, 2008) risk elicitation task and find that when choosing among options with greater skewness, subjects tend to choose riskier options than they did when facing options with lower skewness. In their experiment, subjects choose from six lotteries with the same skewness (and kurtosis) but different expected values or variances. Subjects make (up to) three lottery choices with skewness increasing from zero to two positive levels. However, when controlling for the largest gain in the lottery, their results reverse with subjects taking less risky choices as skewness increases. While Grossman and Eckel (2015) note this is consistent with overweighting the long shot, their experiment is not designed to provide evidence of probability weighting. Astebro, Mata and Santos-Pinto (2015) use a variation of the Holt and Laury (2002) risk elicitation task, modified for different levels of (right) skewness. They find that greater skewness leads to greater risk taking among both students and executives, and with low and high incentives. Using the same choices to estimate average preference parameters for their samples, they rule out risk loving as an explanation but provide support for optimism and likelihood insensitivity. In a different experimental setting using binary lotteries, Ebert (2015) finds that with a symmetric risk, subjects are mostly risk averse but with a right-skewed risk they are mostly risk loving. Thus, similar to these other studies, he finds that risk taking increases with greater skewness.

In contrast to these studies, we structurally estimate individual level risk preference

 3 There are two reasons why we do not estimate a model such as cumulative prospect theory (CPT) that allows for subject loss aversion. First, the existing literature on the interaction between variance and skewness has focussed on the role of probability distortion and not on loss aversion. Since ours is the first study to estimate individual structural parameters and link them to skewness and risk taking behavior, we focus on the key concept in the literature. Second, as noted by Barberis (2013), a weakness of CPT is the need to make assumptions regarding the appropriate reference point.

parameters using a standard protocol and relate these to decisions over skewness and risk observed in a separate experimental task. Our results demonstrate the important relationship between probability distortion and skewness seeking/avoiding, as well as revealing considerable individual heterogeneity. In addition to measuring individual risk preference parameters, our experiment also differs by using mixed lotteries that are both left- and right-skewed, whereas the three studies described above use only right-skewed lotteries over gains.⁴ Finally, our design allows us to study not only how skewness affects risk taking but also how the risk of lotteries affects observed skewness-related behavior.⁵

Our work is also related to the "favorite – long shot bias"; a robust finding in horse betting that long shots (right-skewed lotteries) are overpriced, leading to lower returns on average than favorites. While earlier explanations were that bettors were risk lovers, Golec and Tamarkin (1998) provide evidence consistent with skewness seeking and risk aversion rather than risk loving preferences. In later work, both Jullien and Salanie (2000) and Snowberg and Wolfers (2010) found that models allowing for bettor misperceptions fit the racetrack data better than risk loving preferences do. Importantly, both of these papers rely on a representative agent model and so do not study individual heterogeneity as we do. Further, controlled laboratory experiments can properly isolate factors in a way that is not possible with naturally occurring data where the variance and skewness of bet returns are correlated. Nevertheless, an implication from the long-shot bias is that bettors' preference for skewness is sufficiently strong to overcome aversion to risk and lower expected returns, which reinforces the importance of studying the

⁴ While Ebert (2015) does include left-skewed lotteries in his experiment (as discussed below), he only studies the interaction of risk taking and skewness seeking with right-skewed lotteries (as compared to symmetric, or zero-skew ones).

⁵ We know of only one study that asks this reverse question although this is not isolated in the experimental design but revealed in regression results. Specifically, Brunner et al. (2011) finds that higher variance generates more skewness-seeking choices in their experiment using binary lotteries.

interaction between risk and skewness.

It is important to note that we study skewness seeking/avoiding behavior rather than prudence. Consistent with Ebert and Wiesen (2011), we define skewness seeking as preferring a lottery with a larger skewness over another lottery with a smaller skewness but the same expected value, variance and kurtosis.⁶ In contrast, prudence is a stricter feature of preferences, implying skewness seeking behavior that is robust to different levels of kurtosis. Ebert and Wiesen (2011) find evidence of prudence, with most prudent subjects also being skewness seeking but not necessarily vice versa.⁷ In our experiment, we hold kurtosis constant and use the terminology "skewness seeking" to mean subjects prefer a lottery with larger skewness to one with smaller skewness and exactly the same mean, variance and kurtosis. Similarly, we study "risk taking" rather than risk preference, with the former referring to preferences over changes in standard deviation holding the other moments constant.⁸

As mentioned earlier, most studies include only right-skewed lotteries. Exceptions include Ebert and Wiesen (2011) who study eight pairs of binary lotteries that have the same expected value, variance, (and kurtosis, by definition because they are binary lotteries), and absolute skewness, but one is right-skewed and the other left-skewed. They find significant evidence of skewness seeking (defined here as choosing the right-skewed lottery) with 77% of choices in this direction. Ebert (2015) includes both left- and right-skewed lotteries in his experiment involving binary lottery choices, as well as symmetric (i.e. zero-skew) lotteries. He

Example of Larger skewness can therefore mean either a more right-skewed lottery or a less left-skewed lottery.

Trautmann and van de Kuilen (2018) survey the growing number of avanimental stylies that study.

⁷ Trautmann and van de Kuilen (2018) survey the growing number of experimental studies that study prudence using the risk apportionment task theoretically developed by Eeckhoudt and Schlesinger (2006). The aggregate level findings regarding prudence are considered inconsistent with standard models of expected utility, and while the potential for non-EU models is noted, these are not investigated using individual level data (e.g. Ebert and Wiesen, 2014).
⁸ This is true for the first part of the experiment where we observe behavior towards standard deviation and

skewness. In the second part of the experiment, we use lottery choices to elicit risk preferences, that is, the curvature of the utility function and a parameter of probability distortion. These elicited risk preference parameters are then used to explain behavior in the first part of the experiment.

finds that subjects care about differences in the direction of the skewness but less about the magnitude of skewness, finding no evidence of skewness seeking when comparing two rightskewed lotteries. Ebert (2015, p. 86) finds evidence for skewness preferences, "that individuals both like right-skew and dislike left-skew, and we do not find that one is more important than the other". In a striking contrast, Symmonds et al. (2011), in a neuroeconomics study, consider lotteries with both left and right skewness and finds that *preference for left skewness* is actually more prevalent than skewness seeking. The design is very different in this study, which involves complicated lotteries with between three to nine outcomes.⁹ More generally, these contrasting findings suggest that it is important to study skewness seeking/avoiding behavior across different domains including both left and right skewness.

2. Experimental Design and Methodology

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Our experiment consists of the three following tasks always presented in the same order: eliciting willingness to pay for lotteries varying in standard deviation and skewness, eliciting individual structural risk preference parameters (utility curvature and probability weighting), and a final questionnaire eliciting standard demographic information.¹⁰ The tasks are always presented in the same order so that our primary task always comes first before subjects become bored or fatigued. We discuss the two first tasks in turn. Experimental instructions (translated from French) are provided in Appendix A.

 9 Symmonds et al. (2011) is the closest in design to our experiment in the sense that they use an orthogonal design involving six levels of skewness and ten levels of variance. However, in their design rather than explicitly eliciting the certainty equivalent, the subject chooses between each gamble and a single sure amount. The single sure amount has three levels, and this choice is repeated for each gamble using each level. In total, each subject makes 180 decisions in rapid succession.

 10 The experiment also involved an additional unrelated task, however as the results from this task are not used in this article we do not discuss it further.

2.1 Eliciting Willingness to Pay for Lotteries Varying in Standard Deviation and Skewness

We designed eight lotteries varying in standard deviation and skewness but with a constant mean and kurtosis, for which we seek to elicit certainty equivalents (CEs). As shown in Table 1, the lotteries have two different levels of standard deviation but four different levels of skewness, two negative and two positive, but with the same absolute value. Positively skewed lotteries are right-skewed, while negatively skewed lotteries are left-skewed. We use lotteries with three possible outcomes as this allows us to control the kurtosis, mean, and variance, while changing the skewness. We keep the probabilities fixed but change the outcomes, which always include a mix of gains and losses. Subjects are endowed with ϵ 6 at the beginning of this first task to cover the largest possible loss.¹¹ Each lottery is defined as $\{(X1, 0.5), (X2, 0.4), (X3, 0.1)\}\,$ with X1, X2, X3 representing the outcomes and 0.5, 0.4 and 0.1 their respective probabilities. All amounts are in Euros.

We elicit willingness to pay for each lottery using the CE method commonly used in the risk literature. The subject makes a series of binary choices between the lottery and a sure amount using the multiple price list technique. Following the recent literature (Etchart-Vincent and L'Haridon, 2011; Diecidue et al., 2015; Cubbitt et al., 2015; Ifcher and Zarghamee, 2016), each binary choice involves a sure amount varying from the lowest to the highest payoff of the lottery with a ϵ 0.50 step. To avoid inconsistencies in behavior (switching back and forth), some articles (Etchart-Vincent and L'Haridon, 2011; Cubbitt et al., 2015) report asking subjects to state the row at which they would switch from choosing the lottery to choosing the sure amount. In our setting, we also decide to constrain subjects to switch only once.

¹¹ This is a losses-from-an-initial-endowment payment scheme as widely used by experimentalists both for practical and ethical reasons. As shown by Etchart-Vincent and L'Haridon (2011), in a similar CE elicitation task, such a payment scheme does not suffer from bias towards more risk-seeking or more risk-averse behavior.

Lottery	X1	X2	X3	Expected	Standard	Skewness	Kurtosis
	$(p=0.5)$	$(p=0.4)$	$(p=0.1)$	Value	Deviation		
A	-2.96	7.26	10.74	2.50	5.55	0.105	1.174
B	-1.83	9.28	-2.98	2.50	5.55	0.397	1.174
C	7.96	-2.26	-5.74	2.50	5.55	-0.105	1.174
D	6.83	-4.28	7.98	2.50	5.55	-0.397	1.174
E	-0.23	4.88	6.62	2.50	2.77	0.105	1.174
F	0.34	5.89	-0.24	2.50	2.77	0.397	1.174
G	5.23	0.12	-1.62	2.50	2.77	-0.105	1.174
H	4.66	-0.89	5.24	2.50	2.77	-0.397	1.174

Table 1. Lotteries Employed in the Experiment

Note: Only the information contained in columns 2 to 4 is provided to the subjects.

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To help subject comprehension, the lottery options were presented to subjects using pie charts. Figure 1 shows an example for Lottery F.

We employ a within-subject design and ask each subject to reveal their willingness to pay for each of the eight lotteries. To control for potential order effects, although they seem unlikely as each lottery is quite different, we created eight sequences that were randomized across subjects.¹²

 12 The eight sequences are shown in Appendix C. Each lottery appears once in each sequence; each lottery appears in a given rank (1 to 8) in each sequence; each lottery is always played with the same preceding lottery except when it is played first: for example, D is always played after C (except in sequence 6 where it is played first), so there is more control.

Figure 1. Sample Screen - Lottery F

2.2 Eliciting Individual Structural Risk Preference Parameters

To elicit risk preferences (utility curvature and probability distortion) for each subject in our sample we use the "mixed frame" protocol of Harrison and Rutström (2009) who use a modified Hey and Orme (1994) protocol. In this part of the experiment, subjects are presented with 60 lottery pairs, each represented as a "pie" showing the probability of each prize. Figure 2 shows an example. Subjects could choose the lottery on the left or the right, or explicitly express indifference (then the experimenter flips a coin on the subject's behalf).

Following the protocol of Harrison and Rutström (2009), our design consists of 60 lottery choices per subject. Subjects are given an initial endowment of ϵ 8 (which covers the largest possible loss) and the prizes are $- \epsilon_8$, $- \epsilon_3$, ϵ_3 , and ϵ_8 . The probabilities used in each lottery ranged roughly evenly over the unit interval. The 60 lottery choices are listed in Appendix B.

Figure 2. Sample Screen - One of the 60 Binary Lottery Choices

Time left: 00:00:20

In order to avoid long delays and an unnecessarily long session, after the first three choices we set a 30-second time limit on choices in this part of the experiment. We chose no timer for the first three tasks so that subjects can familiarize themselves with the design. The time limit was based on subjects' decision times in Harrison and Rütström (2009), which went from 3 to 30 seconds per task (figures computed from the dataset). In the case of indifference or the time expiring, subjects were told that the experimenter would flip a coin on the subject's behalf f for payment .

We collected data from 210 subjects making 12,600 binary choices. Of these choices, 95 (0.75%) resulted in the time expiring, which we exclude from our analysis, leaving 12,505 observations.13 About 6% of these choices consisted of indifference between the two lotteries, which is somewhat higher than the 1.7% in Harrison and Rutström (2009) but may reflect subject fatigue as this task comes after the elicitation of CEs.

Our design allows structural estimation of individual risk preference parameters; specifically, utility curvature and probability weighting. We use a RDU model (Quiggin, 1982), which extends Expected Utility Theory (EUT) by considering probability distortion. The utility function over income *x* is as follows:

$$
U(x) = x^{\alpha} \tag{1}
$$

where α is the shape parameter of the utility function and α is the lottery prize plus the endowment. Under RDU, probabilities p are transformed by a probability weighting function, which we specify according to Tversky and Kahneman (1992) :¹⁴

$$
\Gamma(p) = \frac{p^{\gamma}}{\left[p^{\gamma} + (1-p)^{\gamma}\right]^{\frac{1}{\gamma}}}
$$
 (2)

where γ is a parameter describing the shape of the probability weighting function.

We follow the empirical modelling strategy of Harrison and Rutström (2008) to estimate individual structural parameters in our sample. Details are provided in Appendix D. We perform two estimations. We first estimate one concavity parameter and one probability weighting parameter for the whole sample of 210 subjects, clustering at the individual level, using all 12,505 observations. Then we estimate one concavity parameter and one probability weighting parameter for each individual using the 60 lottery choices per subject, except for missing observations due to time expiring as mentioned above.

¹³ From the subject's point of view, choosing indifference or letting the time expire leads to the same incentive structure (i.e. the experimenter flips a coin). Thus, a subject might let time expire to express indifference but we have no way of knowing this.

 14 We also estimated the model using the Prelec (1998) function. Results were qualitatively similar but the statistical significance of parameters in the final latent class model was higher with the Tversky and Kahneman (1992) function.

2.3 Implementation

At the end of the experiment, one of three tasks (the 8-lottery task, the 60-lottery task and a third unrelated task not reported in this paper) was randomly chosen for payment. Then one out of eight choices (if 8-lottery task) or one out of 60 choices (if 60-lottery task) or one out of five choices (if unreported task) was randomly chosen and played out for real. If the 8-lottery task was chosen, then a particular row was also randomly selected for the chosen lottery with the subject paid either the sure amount for that row, if they choose that, or the lottery is played according to the probabilities indicated. Subjects were paid these lottery outcomes plus the initial endowment of either ϵ 6 (8-lottery task) or ϵ 8 (60-lottery task).

The experiment was fully computerized and programmed using the LE2M software developed at the Laboratory for Experimental Economics - Montpellier (France).¹⁵ We conducted 12 sessions at the University of Montpellier in June 2018, with approximately 20 subjects per session. The first session with 20 subjects was a pilot to check our program and is excluded from the analysis. We have complete data from 210 subjects. The subjects, recruited using ORSEE (Greiner, 2015), were mostly students and 55% were male. While most had experience in experiments (89%), none had previously participated in a similar experiment. The experiment typically lasted for one hour and average earnings were ϵ 8, ranging from ϵ 1.50 to €16.50. These earnings were added to the show up fee of E 2 for students of the Economics Department (where the experimental lab is located) and ϵ 6 for those from outside the department.

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¹⁵ https://www.cee-m.fr/leem/

3. Results I: Skewness Seeking and Risk Taking Behavior

Our results are structured as follows. First, we describe the evidence for skewness seeking among our subjects, distinguishing between left- and right-skewed lotteries. Second, we study how risk taking changes as skewness increases. Third, we look at the interaction. These results derive purely from the first (8-lottery) part of the experiment and do not rely on parametric assumptions. In the following section, we explain our findings by examining individual level behavior using structural parameters estimated using the second (60-lottery) part of the experiment. Unless stated otherwise, all reported p-values are from paired two-sided ttests.

3.1 Aggregate Level Behavior

For each of our 210 subjects we elicited the CE for the eight different lotteries in part one of the experiment. Choices were made in ϵ 0.50 steps. We computed the CE for each lottery by taking the midpoint of the range where the subject switched from the lottery to the sure amount. Table 2 summarizes the distribution of elicited CEs for each of the eight lotteries.

Figure 3 shows the mean CE for each lottery where the eight lotteries are arranged according to skewness and variance. On the arrows, we report the results of paired t-tests comparing the CEs of two orthogonal lotteries. Horizontal comparisons involve lotteries that differ only in skewness, while vertical comparisons compare pairs of lotteries that differ only in variance. Diagonal arrows combine the two effects.

Recall that we use the terminology "skewness seeking" when subjects prefer a lottery with a larger skewness to one with a smaller skewness and exactly the same mean, variance, and kurtosis. Note that "larger" skewness also encompasses the case of a smaller negative skewness.

In addition, the terminology of "risk taking" behavior or preferring a "riskier" lottery refers only to an increase in standard deviation of a lottery.

Lottery	X ₁	X ₂	X3	1st	Median	3rd	Mean	Std.	Min	Max
	$(p=0.5)$	$(p=0.4)$	$(p=0.1)$	Quart		Quart		Dev.		
A	-2.96	7.26	10.74	2.25	3.75	6.25	4.03	2.88	-2.75	11.25
B	-1.83	9.28	-2.98	0.75	2.75	4.75	2.95	2.93	-3.25	9.75
\mathcal{C}	7.96	-2.26	-5.74	0.25	2.25	4.25	2.39	3.03	-6.25	8.25
D	6.83	-4.28	7.98	1.25	3.75	5.75	3.28	2.98	-4.75	8.25
E	-0.23	4.88	6.62	2.25	3.25	4.75	3.36	1.92	-0.75	7.25
\boldsymbol{F}	0.34	5.89	-0.24	1.25	2.25	3.25	2.42	1.50	-0.75	6.25
G	5.23	0.12	-1.62	1.75	2.25	3.75	2.48	1.57	-2.25	5.75
H	4.66	-0.89	5.24	1.75	2.75	3.75	2.82	1.52	-1.25	5.75

 Table 2. Summary Statistics on Elicited CEs (€)

Consider first the four right-skewed lotteries, A, B, E, and F. These are shown on the right panel of Figure 3. The two horizontal comparisons show that the more (right) skewed lotteries are valued less than the lower skewed lottery with the same expected value, variance and kurtosis; i.e. $\overline{\text{CE}}_{\text{B}} < \overline{\text{CE}}_{\text{A}}$ and $\overline{\text{CE}}_{\text{F}} < \overline{\text{CE}}_{\text{E}}$, and these differences are highly significant (pvalues < 0.01). These results suggest that rather than being skewness seeking, subjects are skewness avoiding, and this is true for lotteries with both low and high variance. The two vertical comparisons in the right panel show that subjects value riskier lotteries more than a lottery with lower variance but the same expected value, skewness and kurtosis; i.e. $\overline{\text{CE}}_A > \overline{\text{CE}}_E$ and $\overline{\text{CE}}_B >$ $\overline{\text{CE}}_F$, and these differences are significant (p-values<0.05). These results imply that subjects are risk takers, and this is true for lotteries with both low and high positive skewness. The diagonal compares the combined effect of an increase in variance and an increase in skewness. Since CE_B $\rm < CE_E$ this implies that the skewness effect dominates; subjects value less lotteries that are more skewed to the right and riskier, although the difference is only weakly significant (p-value<0.10).

Notes: all values in ϵ ; the arrows show the direction and significance of paired t-tests of CEs; *** p<0.01, ** $p<0.05$, * $p<0.10$.

Next, consider the four left-skewed lotteries, C, D, G, and H, shown in the left panel of Figure 3. Again, the horizontal comparisons show that lotteries with a larger skewness are valued less, with $CE_C < CE_D$ and $CE_G < CE_H$, and these differences are significant (p-values < 0.05). Subjects are again skewness avoiding. The vertical comparisons show that subjects value the riskier lottery more but only when the lottery is highly skewed to the left; i.e. CE_D > CE_H and the difference is significant (p-value 0.05). In contrast, the CE of lotteries C and G is not significantly different. The combined effect of an increase in variance and an increase in skewness (shown on the diagonal) is again negative, with $\overline{CE}_C < \overline{CE}_H$ implying that the skewness effect dominates. The difference is weakly significant (p-value<0.10).

Overall, the two panels show a consistent pattern of skewness avoiding and risk taking behavior, which is true with both right- and left-skewed lotteries. Next, we compare lotteries with the same absolute level of skewness but different directions. On average, subjects continue to be skewness avoiders when we compare lotteries with a large absolute skewness (0.397) as $\overline{\text{CE}}_{\text{F}}$ < $\overline{\text{CE}}_{\text{H}}$ (significant at 0.01) and $\overline{\text{CE}}_{\text{B}}$ < $\overline{\text{CE}}_{\text{D}}$ (although not significant at usual levels).¹⁶ However, the results differ when we compare lotteries with the same small absolute skewness (0.105), as subjects prefer the right-skewed lottery to the left-skewed one. Specifically, $\overline{\text{CE}}_{\text{A}}$ > $\overline{\text{CE}}_{\text{C}}$ and $\overline{\text{CE}}_{\text{E}}$ > $\overline{\text{CE}}_{\text{G}}$, and these differences are highly significant (p-values < 0.01).

While skewness avoidance is the dominant behavior, these different results when considering lotteries A and E suggests that subject decisions are influenced by factors beyond the moments of the lotteries. In particular, consider how X3, the least likely outcome which occurs with p=0.10, varies across the eight lotteries. As reported in Table 1, lotteries A, D, E and H, all have their best lottery outcome as X3, while lotteries F, G, B and C all have their worst outcome (always a loss) as X3. In the four pairwise lottery comparisons where only the magnitude of skewness is changing and not the direction (i.e. CD, BA, FE, GH), the four more right-skewed lotteries (C, B, F, G) all have their worst outcome as X3, and skewness avoiding is the predominant behavior. In contrast, when we compare lotteries that have the same absolute skewness (e.g. AC and EG), the more right-skewed lotteries (A and E) have their best outcome

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 16 ¹⁶ These results are not shown in Figure 3 to avoid cluttering the diagram.

as X3, and then behavior reverses as subjects are predominantly skewness seeking. This might explain the differences we find and could relate to subjects overweighting the least likely (X3) outcome.17 This motivates the second part of our experiment.

3.2 Individual Level Behavior

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Taken at the aggregate level, subjects are predominately skewness avoiding risk takers. In this section, we examine individual behavior. For each horizontal pairwise comparison of lotteries (e.g. lottery B versus A) we count the number of individuals that reported CEs consistent with skewness seeking (i.e. $CE_B > CE_A$), skewness neutrality ($CE_B = CE_A$) or skewness avoidance ($CE_B < CE_A$). For each pairwise comparison, the percentages of skewness seeking and skewness avoiding behaviors are shown in Figure $4¹⁸$ In seven out of the twelve pairwise horizontal comparisons the proportion of skewness avoiders is larger than the proportion of skewness seekers. Consistent with the results discussed above, the highest shares of skewness avoiders are observed where the two lotteries have the same direction of skewness (either right- or left-skewed). This implies that our average findings are reflective of general behavior among our subjects.

Our aggregate level results suggested that risk taking was the predominant decision among our subjects. In a similar manner, we now consider individual risk taking behavior by examining the four vertical comparisons among lotteries that differ only in variance. We classify

 17 Exploring probability weighting is especially relevant. As mentioned earlier, Eckel and Grossman (2015) find that when controlling for the largest gain in the lottery, subjects take less risky choices, instead of riskier choices, as skewness increases. Bordalo, Gennaioli, and Shleifer (2012) offer an alternative theory, salience theory, to explain why subjects might be risk averse in some situations and risk seeking in others. Some payoffs might draw subjects' attention (be salient). Subjects are then risk seeking when a lottery's upside is salient and risk averse when its downside is salient.

 18 For each lottery pair we use a chi-square test (of equality of proportions) to compare the observed proportions of skewness seeking, skewness neutral, and skewness avoiding subjects to random proportions. The latter are obtained by drawing randomly 10,000 CEs for each lottery in uniform distributions and counting the number of draws falling in each of the three categories. The null hypothesis that the choices are random is strongly rejected in each case.

an individual as a risk taker if their CE is higher for the higher variance lottery, risk neutral if the same, and risk avoiding if the other way around. The results are summarized in Figure 5. These results also confirm what was observed at the aggregate level: in three out of the four pairwise comparisons, the majority of subjects are risk taking.¹⁹

Note: the proportion of skewness neutral subjects makes up the balance

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While these results show that our aggregate level findings reflect the predominant individual behavior, the results in Figures 4 and 5 also reveal considerable heterogeneity in behavior, which we seek to account for in the next section. In addition, the risk taking behavior of individuals appears to vary with the skewness of the lotteries. In particular, for each individual

¹⁹ Here to are random for each of these pairwise comparisons. oo the chi-squa are test (of equality of proportions) rejects the null hypothesis that the choices and proportions

we counted the number of risk taking choices out of four. Of the 210 subjects, only 34 exhibit risk taking behavior in all four cases, while 18 subjects are risk avoiders in all four cases. These mixed results suggest that risk taking changes with skewness, reiterating the importance of studying the interaction between skewness and variance.

Figure 5. Risk-related Behaviors (Vertical Pairwise Lottery Comparisons)

3.3 Skewness and Variance

We next ask whether subjects are more or less willing to take on risk as skewness increases. If subjects are more risk taking as skewness increases, then the difference in CEs between lotteries B and F will be larger than the difference between CEs for lotteries A and E. Said differently, is the extra amount that subjects are willing to pay for a riskier lottery larger when the lottery is more right-skewed? In fact, we find the opposite: $\overline{CE}_B - \overline{CE}_F = 0.52$ is less than $\overline{CE}_A - \overline{CE}_E = 0.66$ although the difference is not significant (p-value=0.51). When comparing left-skewed lotteries, however we find a significant difference: $\overline{\text{CE}}_{\text{C}} - \overline{\text{CE}}_{\text{G}} = -0.09$ is less than $\overline{\text{CE}}_{\text{D}} - \overline{\text{CE}}_{\text{H}} = 0.46$ (p-value = 0.0053). Therefore, subjects are willing to pay more for riskier lotteries that are more left-skewed. Alternatively, since they are skewness avoiding they prefer to take on risks they like. When looking at individual behavior we find 89 subjects for whom ($CE_B - CE_F$) is larger than ($CE_A - CE_E$), i.e. 42% of our subjects are more risk taking as right-skewness increases. With left-skewed lotteries we find 126 subjects for which $(CE_C - CE_G)$ is smaller than $(CE_D - CE_H)$, hence 60% of subjects are more risk taking when the lottery is more left-skewed.

We also ask if subjects' attitudes to skewness are different as variance increases. That is, are subjects more skewness avoiding when the lottery has a higher variance? With right-skewed lotteries we find no significant difference, although $\overline{\text{CE}}_A - \overline{\text{CE}}_B = 1.10$ is greater than $\overline{\text{CE}}_E - \overline{\text{CE}}$ $F = 0.94$ (p=0.50). The difference is however significant for left-skewed lotteries, with \overline{CE}_D – $\overline{\text{CE}}_{\text{C}}$ = 0.89 greater than $\overline{\text{CE}}_{\text{H}}$ – $\overline{\text{CE}}_{\text{G}}$ = 0.34 (p=0.0035). When making these comparisons at the individual level, we have 97 subjects (46%) for whom ($CE_A - CE_B$) is greater than ($CE_E - CE_F$) and 126 subjects (60%) for whom (CE_D – CE_C) is greater than (CE_H – CE_G).

In summary, these results on the interaction of variance and skewness are mixed. We only find significant effects when considering left-skewed lotteries. However, it is also evident that there is considerable heterogeneity in behavior.

4. Results II: Can Individual Risk Preference Parameters Explain Behavior?

In this section, we first describe the estimation of mean and individual risk preferences using the RDU model based on the 60 lottery choices in the second part of the experiment (Section 4.1). We then link these individual risk preference parameters with heterogeneous skewness seeking/avoiding and risk taking behavior in the eight lotteries in the first part of the experiment (Section 4.2).

4.1 Estimation of Individual Risk Preference Parameters

The two parameters of the RDU model, utility curvature and probability weighting as shown in equations (1) and (2), are estimated with Maximum Likelihood (ML) using the 12,505 active choices of the 210 subjects. The mean results are reported in Table 3. As shown, the estimated parameters $\hat{\alpha}$ and $\hat{\gamma}$ are both significantly lower than one, which is indicative of a concave utility function and an inverse s-shaped probability weighting function, respectively. The latter indicates that, on average, subjects overweight small probabilities and underweight large probabilities.

	Estimated Coefficient (Standard Error)
Utility curvature parameter ($\hat{\alpha}$)	$0.877***$
	(0.014)
Probability weighting parameter $(\hat{\gamma})$	$0.879***$
	(0.014)
$#$ Observations	12,505
$#$ Individuals	210
Log likelihood	-7607.049
Test of equality of parameters to one.	
	$\hat{\alpha} = 1$ Rejected*** $\hat{\gamma} = 1$ Rejected***

Table 3. ML Estimates of RDU Preference Parameters

Notes: *** stands for p<0.01; Standard errors have been clustered at the individual level.

We next estimate risk preference parameters for each individual in the sample. Summary statistics are provided in Table 4. The estimated value for the α parameter varies from 0.18 to

1.94, with a median equal to 0.97, so we have both concave and convex utility functions in our subject pool. The estimated γ parameter varies from 0.12 to 3.59 with a median at 0.88. The mean of both parameters is close to $1²⁰$

Variable	Obs.	1st	Median	3rd	Mean	SD	Min	Max
		Ouart.		Ouart.				
Utility curvature parameter $(\hat{\alpha})$ 210 0.863 0.971 1.098 0.975 0.231							0.180	1.944
Prob.-weighting parameter ($\hat{\gamma}$)			210 0.737 0.877 1.042		0.946	0.397	0.123	3.591

Table 4. Summary Statistics for Estimated Individual Risk Preference Parameters

Slightly over half of the subjects (56%) are found to have a concave utility function and more than two-thirds (72%) exhibit an inverse s-shaped probability weighting function. Based on these two estimated characteristics we classify subjects into four categories as summarized in Table 5. The most common pattern (45% of the sample) is to exhibit both concave utility and inverse sprobability weighting.

		Probability weighting function $(\hat{\gamma})$		
		≤ 1		
	≤ 1	45% (95 subjects)	10% (22 subjects)	117
Utility curvature parameter $(\hat{\alpha})$		27% (57 subjects)	17% (36 subjects)	93
Total		152	58	210

Table 5. Frequency of Subjects with Risk Preference Parameters Above and Below 1

4.2 Can Individual Risk Preference Parameters Explain Behavior?

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In this section, we aim to link subjects' individual risk preference parameters to their

²⁰ Figure F1 in Appendix F shows the distribution of the two parameters in the sample.

behavior in the first part of the experiment. Results discussed in Section 3 showed evidence of considerable heterogeneity in behavior. In line with earlier literature (e.g. Harrison and Rütström, 2009) we allow for heterogeneous behavior by specifying a latent-class Logit (LCL) model to describe the decision made by each subject when facing the choice between a lottery and a sure amount in part one of the experiment (see Appendix E for a description of the LCL model).

Each subject in the first part of our experiment made 170 binary choices (between a lottery and a sure amount). We characterize each alternative by its first three moments (mean, variance, and skewness). For the alternative corresponding to the sure amount, the second and third moments are equal to zero. The specification that best fits the data models the discrete choice between the lottery and the sure amount as a function of the mean, variance, and skewness of each alternative. In addition, class membership depends on gender (a dummy variable that takes the value one if the subject is a male, and zero otherwise) and the two parameters characterizing a subject's utility curvature and probability distortion (as obtained from the estimation of the RDU model). Other subject characteristics such as age, university major and current degree, were insignificant and were excluded from the model.

The LCL model is suitable to analyze heterogeneity in discrete choice behavior and is an alternative to the traditional multinomial logit model and the mixed logit model. The underlying theory behind the LCL model assumes that the discrete choice made by each individual depends on observable characteristics of the alternatives she is facing and on *latent heterogeneity* which is unobserved by the econometrician. Contrary to the mixed logit model, which relies on continuous distributions of heterogeneity, the LCL model approximates the underlying continuous distributions of parameters with *discrete distributions*. This is done by assuming that the population is implicitly sorted into *C* classes characterizing heterogeneity, with classmembership being unknown to the analyst. Since the LCL model relies on a discrete approximation of continuous distributions it might be considered less flexible than the mixed logit model but the discrete approximation makes the model free of any assumptions about the distributions of parameters across individuals. 21

Researchers commonly use criteria to choose the number of (latent) classes. The most common criteria are the Akaike Information Criterion and the Bayesian Information Criterion, both criteria being based on the log-likelihood the model reached at convergence. In our model, both criteria were minimized for a number of classes equal to 20. However, such a large number of classes is problematic for two reasons: first, the significance of parameter estimates in the model decreases with the number of classes and second, the characterization of each class becomes more difficult. This is especially true when the number of variables used to explain class membership is small (three in our case). We thus decided to limit the number of classes. In terms of parameter interpretation and significance of parameter estimates, a model with two classes was found to be most suitable.²²

Estimation results using 35,700 observations (170 binary choices made by each of the 210 subjects) are shown in Table 6. Subjects in both classes value the mean positively and the coefficient is of the same magnitude in the two classes. However, subjects in Class 1 prefer alternatives with a lower variance but are indifferent to the third moment or skewness, whereas subjects in Class 2 prefer alternatives with a higher variance and a lower skewness. We find that the probability of being in Class 1 increases if the subject is a female, if subjects have a lower

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²¹ The multinomial logit model relies on the assumption of independence from irrelevant alternatives, which is considered strong in most settings. For this reason, the mixed logit model and the LCL model are often preferred. Various competing models have been tried (multinomial logit, conditional logit, mixed logit) with the latent-class logit model offering the best compromise since it allows identifying sub-groups of subjects with heterogeneous underlying preference patterns, and also performs well in terms of parameter significance.

²² Estimated parameters (and corresponding standard errors) obtained for a three-class LCL model do not allow identifying a third group of subjects in addition to the two classes identified with the two-class LCL.

utility curvature parameter $(\hat{\alpha})$, and for subjects who are characterized by a more inverse sshaped probability weighting function (lower $\hat{\gamma}$ parameter). On the contrary, male subjects, those with a higher utility curvature parameter and an s-shaped probability weighting function are more likely to be in Class 2. The LCL model demonstrates the importance of individual heterogeneity and suggests there may be a connection between probability weighting and skewness seeking/avoidance behavior.

	Coefficient	Std Error	P-value
Class-1 model			
Mean	$0.845***$	0.0124	0.000
Variance	$-0.157***$	0.0064	0.000
Skewness	0.040	0.0780	0.604
Class-2 model			
Mean	$0.861***$	0.0154	0.000
Variance	$0.433***$	0.0103	0.000
Skewness	$-0.329***$	0.0906	0.000
Probability of Class-1 membership			
Constant	1.429	0.7582	0.060
Male $(0/1)$	$-0.659**$	0.2975	0.027
Utility curvature parameter $\hat{\alpha}$	$-1.943***$	0.7122	0.006
Prob-weighting parameter $\hat{\gamma}$	1.139**	0.4908	0.020
# Observations	35,700		
# Individuals	210		
Log-likelihood	-11749.805 \sim \sim \sim		

Table 6. Estimation of the Latent-Class Logit Model with Two Classes

Notes: *** p<0.01, ** p<0.05, * p<0.1

To check how well the model performs in differentiating between the two classes, we look at the highest (posterior) probability of class membership (the higher this probability, the better the model in terms of class differentiation). Over the 210 subjects, the average highest probability is greater than 0.99 and the minimum is 0.78, which indicates that the model performs well in distinguishing between subjects' preference patterns.

Finally, Table 7 reports the average characteristics within each class where each subject is assigned to either Class 1 or Class 2 based on the highest posterior probability of membership in one class or the other. Approximately half of the sample falls into each class. As expected, we find a lower proportion of males in Class 1 compared to Class 2. The average subject in Class 1 has a slightly concave utility function and does not distort probabilities. In contrast, the average subject in Class 2 is characterized by an inverse s-shaped probability weighting function and has a linear utility function.

	$#$ Ind.		Male $(0/1)$ Utility curvature parameter $\hat{\alpha}$	Prob-weighting parameter $\hat{\gamma}$
Class 1	117	0.47	0.937	0.992
Class 2	93	0.62	1.024	0.889

Table 7. Average Characteristics within Each Class

We then try to answer the question: are subjects more risk taking when skewness increases? To do this we create an interaction term between variance and skewness and reestimate the two-class LCL model assuming that the choice between the lottery and the sure amount depends on the mean, the variance, and the above interaction term. Results are shown in Table 8. For those in Class 1 the interaction term is not significant so subjects do not take more or less risk if skewness increases. This is consistent with class members being indifferent to skewness. For those in Class 2, the interaction term has a positive sign, which indicates that subjects in this class are willing to pay more for riskier lotteries if skewness increases, and that their dislike for skewness is somewhat reduced if variance increases.

	Coefficient	Std Error	P-value
Class-1 model			
Mean	$0.844***$	0.0120	0.000
Variance	$-0.155***$	0.0065	0.000
Skewness	-0.198	0.2426	0.414
Var. x Skewness	0.056	0.0546	0.303
Class-2 model			
Mean	$0.861***$	0.0150	0.000
Variance	$0.437***$	0.0103	0.000
Skewness	$-1.181***$	0.2888	0.000
Var. x Skewness	$0.201***$	0.0646	0.002
Probability of Class-1 membership			
Constant	$0.595**$	0.2661	0.025
Male $(0/1)$	$-0.647**$	0.2997	0.031
Utility curvature parameter $\hat{\alpha}$	$-0.119**$	0.0492	0.015
Prob-weighting parameter $\hat{\gamma}$	0.265	0.1744	0.129
# Observations	35,700		
# Individuals	210		
Log-likelihood	-13537.375		

Table 8. Estimation of the Latent-Class Logit Model with Interaction Term

Notes: *** p<0.01, ** p<0.05, * p<0.1

5. Discussion

 In order to study skewness seeking/avoiding behavior and its interaction with risk taking, we designed a novel laboratory experiment that elicits CEs over lotteries where the variance and skewness of the outcomes are orthogonal to each other. We then related these choices to individual structural parameters elicited in a separate experimental task and estimated using the RDU model. At the aggregate level, we observed frequent skewness avoiding and risk taking behavior. However, these aggregate level results mask considerable individual heterogeneity in behavior. By linking these decisions to estimated individual risk preference parameters, we identified two classes of subjects. Slightly over half of our subjects (55%) dislike variance but are indifferent to skewness, while the remainder (45%) like greater variance but dislike greater skewness. Importantly, class membership is related to individual risk preference parameters. Specifically, the average member in the first class has a slightly concave utility function and barely probability weights, while those in Class 2 have nearly linear utility functions and sshaped probability weighting functions implying they overweight small probabilities and underweight large ones. Our results are the first to demonstrate the link between probability weighting and skewness seeking/avoidance behavior at the individual level. Crucially, our findings highlight the importance of accounting for individual heterogeneity.

At the aggregate level, we found evidence of an interaction between risk taking and skewness avoiding behavior only for left-skewed lotteries, where subjects are more risk taking the smaller the skewness was. This interaction effect is consistent with the average finding of risk taking skewness avoiders being more willing to take on risks they like. However, we also find evidence of substantial individual heterogeneity in this behavior. Our LCL model finds that subjects who are indifferent to skewness (i.e. those in Class 1), are similarly unaffected by the interaction with variance. On the other hand, those in Class 2 dislike skewness, although this dislike is moderated by greater variance. That is, the interaction between variance and skewness seeking is positive for those in Class 2.

Our finding of skewness avoiding behavior is novel in the experimental literature. Even though this aggregate level behavior masks individual level heterogeneity, our LCL model reveals that nearly half of our subjects (i.e. those in Class-2) display similar behavior. Further, even those in Class 1 are actually neutral about skewness. In contrast, the predominant finding in the previous literature is skewness seeking (e.g. Ebert, 2015; Ebert and Wiesen, 2011), or the even stricter criteria of prudence (see Trautmann and van de Kuilen, 2018, for a survey of prudence experiments).²³ Nevertheless, almost all of these existing studies consider only the special case of choosing between simple binary lotteries. Our design instead uses a more general form of lottery that involves three outcomes over mixed gains and losses and includes both leftand right-skewed lotteries. Our more complex lottery design generates results closer to those of Symmonds et al., (2011) who found that preference for left skewness was actually more prevalent than skewness seeking in a neuroeconomics experiment involving complicated lotteries with between three to nine outcomes.²⁴

Another difference in our experimental design is that we elicit certainty equivalents rather than using lottery choices. This is crucial for our purpose because measuring the intensity of preferences allows us to study the interaction between risk taking and skewness seeking/avoiding behavior.²⁵ Our method of eliciting CEs is employed in numerous recent experimental studies of individual behavior (e.g. Etchart-Vincent and L'Haridon, 2011; Diecidue et al., 2015; Cubbitt et al., 2015; Ifcher and Zarghamee, 2016). Even within the experimental prudence literature, the prevalence of prudence varies greatly with the elicitation method. In particular, significantly less prudence is observed with simple compared with compound lottery formats (Maier and Ruger, 2012; Haering et al., 2017). On the other hand, while Deck and Schlesinger (2018) find no

²³ Recall that prudence is a preference for skewness that is robust to changes in kurtosis.
²⁴ Diecidue et al. (2015) demonstrate how the measurement of second-order risk preferences (also via CEs) is similarly affected by lottery complexity. Specifically, they find evidence of risk seeking behavior over complicated lotteries (defined as having three or five outcomes) but risk aversion when lotteries were less complex (having only two outcomes).

²⁵ Most prudence experiments use compound binary lottery choices to align with theoretical constructs. Exceptions are Ebert and Wiesen (2014) who elicit how much compensation subjects require to choose the imprudent option over the prudent one, and Heinrich and Mayrhofer (2018) who use the same method to investigate if higher order risk preferences are influenced by social settings. In an unpublished study, Tarazona-Gomez (2004) elicits certainty equivalents using a design strongly motivated from expected utility theory, and finds only weak evidence of prudence.

difference in aggregate prudence preferences between simple and compound lottery formats, at the individual level the correlation between what people do in the two formats was insignificant.

6. Conclusion

Overall, our study finds evidence of frequent skewness avoiding or neutral behavior and uniquely links this behavior to individual risk preference parameters of utility curvature and probability weighting. Our results regarding the prevalence of skewness avoiding and neutral behavior are unusual in the experimental literature. This suggests caution on two levels. First, researchers should be cautious when extrapolating that subjects are universally skewness seeking based on experiments that use only a very specific design (i.e. compound binary lottery choices). Our results suggest very different behavior when lotteries are more complex and CEs are elicited. While the focus on prudence is of theoretical importance, we suggest that it has limited the scope of experimental designs and resulted in missing other potentially important patterns of behavior. Second, we should be similarly cautious when extrapolating from our single set of experimental results based on a novel design. Because our design involved mixed gain and loss lotteries in the context of both left- and right-skewed lotteries, the stakes had to be relatively low in order to keep net payments non-negative. An obvious extension would develop a similar design involving larger stakes and possibly just gain lotteries. Our design also omitted symmetric lotteries (i.e. with zero skew) although arguably this should not matter as the lotteries are presented in a non-transparent manner. Overall, we encourage future researchers to explore different types of lotteries using a similarly orthogonal design in order to verify the robustness of our findings and to explore skewness seeking/avoiding behavior in different contexts. Other studies could vary the likelihood of the different options to check the robustness of the

relationship to probability distortion.

Our findings also generally reinforce the call for the use of more flexible models than EUT (such as Rank-Dependent Utility or Cumulative Prospect Theory models) to describe observed behavior under risk (Barberis, 2013). Risk aversion may not be sufficient to fully characterize individuals' preferences under risk in most risky situations. Parameters such as preference towards skewness (either positive or negative) as well as probability weighting and loss aversion may help better understanding individuals' decisions. This is true in both experimental and real life settings. The latter can be exemplified by the agricultural economics literature, which is producing growing empirical evidence on the role of downside risk aversion and probability weighting in explaining farmers' decisions such as technology adoption and insurance contracting (Chavas and Nauges, 2020). Among other examples, Liu (2013) showed that Chinese cotton farmers who are more risk averse, or more loss averse, adopt the genetically modified Bt cotton later, whereas farmers who overweight small probabilities adopt Bt cotton earlier. In addition, Babcock (2015) showed that loss aversion and the choice of the reference point that determines gains and losses are major factors in predicting crop insurance decisions of US farmers.

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Appendix A: Experimental Instructions (Translated from French)

Introduction

Thank you for participating in this experiment in decision making. You will be compensated with whatever you earn during the experiment according to the procedures described in the instructions.

The instructions will be read to you in a short while. You may consult these instructions at any time during the experiment. In case you should have any questions or doubts, please raise your hand and an experimenter will come and assist you in private.

Even if you agree to participate, you are free to withdraw at any time during the experiment. Should you decide to withdraw, you will forgo your earnings from the experiment and receive only the show-up fee.

Please consider each decision carefully. Take a careful look at outcomes and the probabilities associated to them before taking a decision. Remember that your final payoffs from this experiment will depend on the decisions you make (and of course, on chance).

This experiment consists of three parts. Once everybody has finished the tasks in Part I, new instructions will be read to you for Part II, and then for Part III.²⁶ At the very end of the experiment, you will be asked to fill out a questionnaire. The answers to the questionnaire as well as all your answers to each of the tasks will be private, and cannot be traced back to you personally. Once you are finished completing the questionnaire, an experimenter will call you up. Your payoff will then be determined in private, you will be given the money you won, after which you can leave. Payoffs are measured in Euros.

Do not talk during the experiment and do not write on the documents which are given to you. Please remain seated when you are finished with the tasks and please switch off your mobile phone.

We will start with Part I of the experiment.

Good luck!

1

PART I

Choice tasks – illustrative example

In this part, you will be asked to choose repeatedly between a fixed amount of money and a lottery. The lottery will always give you a chance to win one of three amounts of money. Figure 1 shows a typical choice task.

Let's comment on this EXAMPLE. For each row, you are asked to indicate whether you would prefer to play the lottery or to obtain the sure amount of money by ticking the preferred option. If you choose the lottery, a number between 1 and 100 will be randomly drawn to determine your payoff.

In the example shown on Figure 1, you will receive 500 if the number being drawn falls between 1 and 10 (which has a 10% chance of happening). If the number that is drawn falls between 11 and 50 (a 40% chance of happening) then you will get 100. If the number that is drawn falls between 51 and 100 (a 50% chance of happening) then you will get 200. Please pay close attention to the amounts to be won as well as to the odds associated with each outcome, since they change across decisions.

 26 Since results from Part III are not analysed in this paper we omit the instructions for this part.

Figure 1: Example of a typical decision task

We are interested in the amount for which you will switch from preferring the lottery to preferring the sure amount. Most likely, you will begin by choosing the lottery for small sure amounts, and at a certain point switch to the sure amount as the latter increases. If you do not want the lottery at all, you can choose to get the sure amount in the first row and then continue with the sure amount for all choices (if you prefer 100 with certainty over the lottery you should also prefer 150 over the lottery, etc.). Where you will switch from the lottery to the sure amount depends entirely on your preferences—there are no right or wrong answers. You are allowed to switch only once.

THE ABOVE WAS JUST AN EXAMPLE. The decision tasks that you will face in Part I will be based on different values for the initial endowment, the lottery outcomes, and the sure amounts.

Types of choices

You will be asked to take 8 decisions. For each one, you will receive an initial endowment of 6 Euros. You will need to decide between a lottery and a series of sure amounts as exemplified in Figure 1 above. Please pay close attention to the amounts to be won as well as the probabilities (% chance) associated with each outcome since they vary from one decision problem to the other. Since your final payoff depends on these decisions, it is crucial for you to pay close attention to these features. All amounts are in Euros.

Payoff determination

Payoff determination
After you have taken all the 8 decisions, one of your decisions will be randomly drawn for real pay, i.e. the amounts indicated in the decision problem will be paid out for real. First, either Part I, or Part II, or Part III will be randomly selected for real play (with equal chance of being selected). If Part I is selected, then one of the 8 decision tasks is drawn at random, using a chance device with equal probability for each decision task to be selected. For the selected decision task, one of your decisions, corresponding to one row for which you had to indicate your preference between the sure amount and the lottery, will then be drawn at random with equal probability for each row. If for the row that is drawn you have indicated that you prefer the sure amount of money, you will simply be paid that amount. In case you have chosen the lottery for the randomly determined row, then that lottery will be played according to the probabilities indicated. You will then be paid the outcome corresponding to the number that is drawn. The initial endowment of 8 Euros will be added to your payment.

Should any questions arise, please raise your hand and I will come and answer you in private.

PART II

Choice tasks - illustrative example

In this part, you will be asked repeatedly to choose or state indifference between a lottery A and a lottery B. There are no right or wrong answers. Your decision depends only on your personal preferences. Just pick the lottery that you prefer or state indifference. Figure 3 provides an EXAMPLE, on which we will now comment.

Figure 3: Example of a choice task

You have to indicate whether you prefer playing the lottery A or the lottery B by ticking the preferred option or of you are indifferent. On the above graphs, the red colour indicates a loss of 800, the yellow color indicates a loss of 300 and the green colour indicates a gain of 800.

In lottery A, you stand 38% chance of losing 800 and 62% chance of gaining 300. A number between 1 and 100 is randomly drawn.

- If the number that is drawn falls between 1 and 38, you lose 800.
- If the number that is drawn falls between 39 and 100, you earn 300.

In lottery B, you stand 49% chance of losing 800, 38% chance of winning 800 and 13% chance of winning 300. A number between 1 and 100 is randomly drawn.

- If the number that is drawn falls between 1 and 49, you lose 800.
- If the number that is drawn falls between 50 and 87, you win 800.
- \bullet If the number that is drawn falls between 88 and 100, you win 300.

You have to indicate if you prefer option A, option B or if you are indifferent.

THIS WAS JUST AN EXAMPLE. Decision tasks to be undertaken in Part II will include different lottery outcomes.

Types of choices

You will be asked to take 60 decisions. For each one, you will receive an initial endowment of 8 Euros. You will need to decide between a lottery A and a lottery B or indicate indifference as exemplified in Figure 3 above. Each amount in Euros will always be associated to the same colour:

- *Red* will represent an amount of -8 Euros (hence a loss of 8 Euros)
- *Blue* will represent an amount of -3 Euros (a loss of 3 Euros)
- *Yellow* will represent an amount of 3 Euros (a gain of 3 Euros)
- *Green* will represent an amount of 8 Euros (a gain of 8 Euros)

Please pay close attention to the amounts to be won as well as the probabilities (% chance) associated with each outcome since they vary from one decision problem to the other. Since your final payoff depends on these decisions, it is crucial for you to pay close attention to these features.

Payoff determination

After you have taken all the 60 decisions, one of your decisions will be randomly drawn for real pay, i.e. the amounts indicated in the decision problem will be paid out for real. First, either Part I, or Part II, or Part III will be randomly selected for real play (with equal chance of being selected). If Part II is selected, then one of the 60 decision tasks is drawn at random, using a chance device with equal probability for each decision task to be extracted. For the selected decision task, the lottery that you have selected (A or B) will be played. If you have chosen indifference, the computer will flip a coin and randomly chose the lottery (A or B) to be played. You will then be paid the amount corresponding to the lottery outcome to which the initial endowment of 8 Euros will be added.

Should any questions arise, please raise your hand and I will come and answer to you in private.

FINAL QUESTIONNAIRE

Please answer the following questions about yourself. All answers are confidential and cannot be traced back to you.

Age: Gender: □ male□ female Nationality: Are you a university student? \Box yes \Box no What is your studies major? What is your current degree? Have you participated in an economics experiment before? \Box yes \Box no

Thank you for taking part in this experiment. Please remain seated until an experimenter calls you up.

Appendix B: The 60-Lottery Choice Task

Appendix C: Part I Lottery Sequences

Appendix D – Estimation of the Risk Preference Model

Respondents face a series of binary lottery choices $j = \{1, 2, ..., 60\}$ where a choice has to be made between two lotteries $Left$ and $Right$. We model the decision as a discrete choice model. We consider a latent variable y_i^* for individual *i*. We observe only the choices y_i (1 if Left, -1 if $Right$ and 0 if $Indifferent$) individual i makes:

$$
y_i = \begin{cases} 1 & \text{if } y_i^* > 0 \\ -1 & \text{if } y_i^* < 0 \\ 0 & \text{if } y_i^* = 0 \end{cases}
$$

For individual *i* and for a given lottery $k = \left| (p^k, x_h^k), ((1 - p^k), x_h^k) \right|$, the expected utility is:

$$
EU_i^k = \Gamma(p^k) \cdot U(x_h^k) + \Gamma(1-p^k) \cdot U(x_l^k)
$$

Subject *i* chooses lottery $Left (y_i = 1)$ if $\Delta EU_i = EU_i^{Left} - EU_i^{Right} > 0$, lottery Right $(y_i = -1)$ if $\Delta EU_i = EU_i^{Left} - EU_i^{Right} < 0$ and *Indifference* $(y_i = 0)$ otherwise. The probability of choosing lottery Left is given in the equation below with ε a normally distributed error term with mean zero and variance one, and $\Phi(.)$ the standard normal distribution function.

$$
Prob(\Delta EU_i > 0) = \Phi(\Delta EU_i)
$$

We use Maximum Likelihood (ML) to estimate the two parameters of interest: concavity α and the shape of the probability weighting function γ . The log-likelihood function is given in the equation below where I(.) is the indicator function, $y_i = 1$ when lottery Left is chosen by individual *i*, $y_i = -1$ when lottery *Right* is chosen and $y_i = 0$ when *Indifference* is chosen.

$$
\ln L(\alpha, \gamma) = \sum_{i} \left\{ \left[ln(\Phi(\Delta EU_i)) \right] \cdot I(y_i = 1) + \left[ln(\Phi(1 - \Delta EU_i)) \right] \cdot I(y_i = -1) \right\}
$$

$$
+ \left[ln\left(\frac{1}{2} \Phi(\Delta EU_i) + \frac{1}{2} \Phi(1 - \Delta EU_i) \right) \right] \cdot I(y_i = 0) \right\}
$$

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Appendix E – Description of the Latent-Class Logit Model

The description that follows borrows from Greene and Hensher (2003) and Pacifico and Yoo (2013).

We model a case in which each individual $n(n=1,...,N)$ is offered a total of T choice situations. For each choice situation, the individual has a choice between *J* alternatives. Each of the alternatives is characterized by a vector of observables characteristics, here gathered in vector *m*. The individual choice is described by a dummy variable y_{nit} , which takes the value 1 if subject *n* chooses alternative *j* in scenario *t*, and 0 otherwise. For subject *n* belonging to class *c*, the probability of choosing the alternative *j* in choice situation *t* is specified as a traditional logit model for discrete choices:

Prob[subject n in class c chooses alternative j in choice situation t] =
$$
\frac{\exp(m'_{nj}, \beta_c)}{\sum_{j=1}^{J} \exp(m'_{nj}, \beta_c)}
$$
(E1)

where β_c are class-*c* specific parameters. The probability of observing his/her sequence of choices over the *T* choice situations is a product of conditional logit formulas:

$$
P_n(\beta_c) = \prod_{t=1}^T \prod_{j=1}^J \left\{ \frac{\exp(m'_{njt}\beta_c)}{\sum_{j=1}^J \exp(m'_{njt}\beta_c)} \right\}^{y_{njt}}
$$
(E2)

Class membership is assumed to depend on subject-specific characteristics that are constant over time and gathered in vector z_n .

Since class membership is not known ex-ante, we consider the following unconditional likelihood of subject's *n* choices which is a weighted average over classes of the above probability, with $\pi_{cn}(\theta)$ representing the population share of class *c*:

$$
L_n(\theta, \beta) = \ln \sum_{c=1}^{C} \pi_{cn}(\theta) P_n(\beta_c)
$$
 (E3)

The weight $\pi_{cn}(\theta)$ is usually modelled as fractional multinomial logit:

$$
\pi_{cn}(\theta) = \frac{\exp(z'_n \theta_c)}{1 + \sum_{c=1}^{C-1} \exp(z'_n \theta_c)},
$$
 with $\theta = (\theta_1, \theta_2, ..., \theta_{C-1})$ class-membership parameters and θ_c

normalized to 0 for identification.

The log likelihood for the entire sample reads as follows:

$$
L(\theta, \beta) = \sum_{n=1}^{N} L_n(\theta, \beta) = \sum_{n=1}^{N} \ln \sum_{c=1}^{C} \pi_{cn}(\theta) P_n(\beta_c)
$$
 (E4)

Our sample includes *N* subjects indexed by *n* = 1 to 210. Each subject is offered a total of *T*=170 choice situations (*t* = 1 to 170) and for each choice situation she has a choice between *J* alternatives. In our case $J = 2$ since each of the 170 choices has to be made between a lottery and a sure amount. Each alternative *j* is described by the vector of its first three moments: its mean m_{njk}^1 , its variance m_{njk}^2 and its skewness m_{njk}^3 . When the alternative is the sure amount then $m_{njk}^2 =$ $m_{nji}^3 = 0$. In our model z_n includes the subject's gender and two parameters measuring the curvature of the utility function and probability distortion as elicited from the estimation of a RDU model.

Appendix F: Additional Results

Figure F1: Distribution of Estimated Individual Parameters (210 Subjects)

 \sim .5 1 1.5 2 $\frac{1}{2}$ Density $\ddot{\Omega}$ \circ \circ $\frac{1}{5}$ $\overline{1}$ 1.5

Utility curvature $(\hat{\alpha})$ Probability weighting function $(\hat{\gamma})$

