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Communication

Spurious phase correction in rapid metabolic imaging

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ABSTRACT

IDEAL-type magnetic resonance spectroscopic imaging (MRSI) sequences require the acquisition of several datasets using optimized sampling in the time domain to reconstruct metabolite maps. Each unitary scan consists of a selective slice (2D) or slab (3D) excitation followed by an evolution time and then the acquisition of the spatially encoded signal. It is critical that the phase variation during the evolution time for each scan is only dependent on chemical shifts. In this paper, we described the apparition of spurious phase due to either the transmit or the receive frequency. The presence of this unwanted phase depends on (i) where the commutation between these two frequencies is performed and (ii) how it is done, as there are two phase commutation modes: continuous and coherent. We present the correction needed in function of the different cases. It appears that some solutions are universal. However, it is critical to know which case is implemented on the MRI scanner, which is not always easy information to have. We illustrated several cases with our preclinical MRI by using the IDEAL spiral method on a ¹³C phantom.

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1. Introduction

Magnetic resonance spectroscopic imaging (MRSI) maps metabolite spatial distribution by exploiting the information contained in the chemical shift (CS). Applications have been used for tumour/lesion identification, treatment and survivorship studies [1,2], tracking changes in metabolic pathways [3–7], fat/water imaging [8–10], and magnetic resonance thermography or quantitative temperature imaging [11,12]. In order to record both spatial and spectral information, different methods were developed.

The first method is the conventional phase-encoded MRSI, currently known as chemical shift imaging (CSI), where the phase encoding gradient amplitude is incremented once per repetition time (TR), leading to a complete separation of the spectral and spatial encoding [13]. Data reconstruction is therefore straightforward, using Fourier transforms. This method offers high sensitivity and localisation performance, but with long acquisition times. To overcome this drawback, the time to acquire either spatial or spectral information must be shortened. One of the most popular approaches to significantly decreasing MRSI experimental

time is the echo planar spectroscopic imaging (EPSI) acquisition scheme, introduced by Mansfield [14]. It is based on a series of periodically inverted gradients, generating a train of echoes, from which both spatial and spectral information can be extracted within one scan. However, increasing the spatial resolution leads to a decrease in the spectral one and vice-versa. Such limitations prevent having a high resolution in both the spatial and spectral dimensions, especially at high magnetic fields.

In order to make the resolutions independent of one another, one solution is to quickly acquire several images recorded at different echo times (TEs). Utilizing this strategy, the spatial information is directly recorded with single-shot trajectories (e.g., EPI, spiral...) [15,16]. As for the spectral information, it is extracted from the signal evolution at different TEs using the iterative decomposition of water and fat with echo asymmetry and least-squares estimation (IDEAL) concept [7,9,17,18]. Fig. 1 illustrates the principle of the IDEAL method combined with a spiral encoding, to give the 2D IDEAL spiral [15]. Such method is particularly useful for hyperpolarized ¹³C metabolic mapping [15]. After a selective slice excitation during t_1 , the spin system is allowed to evolve for a time duration of $t_2 - t_1$ followed by a spiral trajectory image recording. The CS information is recorded through the analysis of the phase evolution occurring during the different shots. This phase evolution depends on the frequency difference between the isochromats

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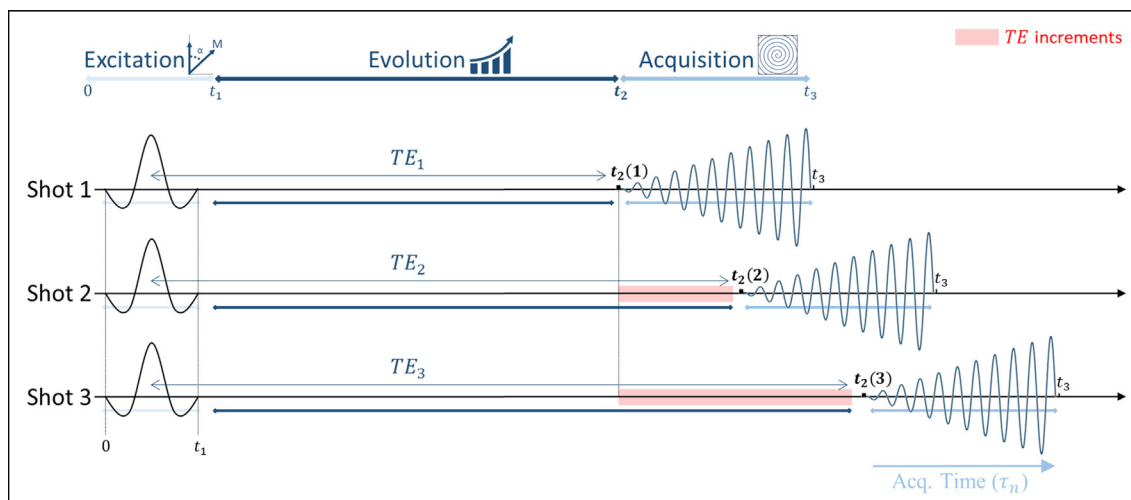


Fig. 1. Illustration of the IDEAL spiral spectral encoding scheme. It consists of radiofrequency (RF) pulses applied during an excitation time (t_1), and an acquisition with spiral spatial encoding ($t_3 - t_2$) applied after an evolution time ($t_2(m) - t_1$). Several shots with different evolution times are used to encode the spectral information.

and the rotating detection frame. To both limit the number of TEs and optimize the TE increments, it is important to have a sparse NMR spectrum as well as prior knowledge on the chemical shift values. In addition, the experiment timing needs to be optimized through the careful choice of the number of signal averages (NSA) [15,17]. Once the experiment is recorded, the various data obtained from the different shots are analysed as one to reconstruct one map per metabolite, as explained in [15]. To obtain a correct reconstruction, it is thus mandatory to get a correct phase, i.e., not prone to spurious influence. Rapid 3D encoding is also possible [19], but obtaining a higher spatial resolution in three dimensions is problematic. Several artefacts, such as motion, may introduce unwanted phase terms. To correct for this, several approaches have been developed [14,20–23]. Another source of phase errors that we address can occur in 2D or 3D with slab selection. Indeed, the radiofrequency (RF) excitation is applied with the transmit frequency (f_T) and the acquisition is done in reference to the receive frequency (f_R). A commutation between these two frequencies has to be made during the pulse sequence. However, depending on the mode and the position of the commutation, phase errors may occur. Two modes of commutation are considered and elaborated later: phase-continuous and phase-coherent switching [24].

The aim of this paper is to elucidate the impact of the frequency commutation’s mode and position on the metabolite map obtained by 2D IDEAL-type method and to show how to overcome the resulting phase errors. This is, to our knowledge, not described in the literature and yet very critical. To experimentally validate this, the IDEAL spiral was applied to a ^{13}C phantom.

2. Theory

The reconstruction of metabolite maps from IDEAL-type sequences requires that the phase variation between shots is only dependent on the CS. All frequencies mentioned in the following are offset values from the reference frequency of the rotating detection frame. In 2D MRI pulse sequences, frequency selective pulses are performed at f_T , which depends on both the slice position and the slice selection gradient G_z intensity. The signal acquisition is performed at f_R .

To the best of our knowledge, there are two modes to commute from $f_T \rightarrow f_R$ set on both clinical and preclinical MRI scanners. The first one is the phase-continuous switch, where the rotation of the

receiver frame starts from the phase where the rotating transmitter frame ended (i.e., $2\pi f_T t$, for a commutation at a time t). The second one is the phase-coherent switch. A numerically controlled oscillator (NCO) is used to count the phase of the reference frame rotating at the on-resonance frequency. At the commutation moment t , the rotation of the receiver frame starts from the phase accumulated by the NCO up to this instant [24].

Fig. 2 illustrates the different cases of the transmit/receive frequency commutation during pulse sequence timing. We identified three options: a commutation before the signal acquisition, one after the slice selection or a combination of the two. In our case, the signal acquired during the m^{th} shot and at the n^{th} k-space sample location \mathbf{k}_n (at the instant τ_n) can be formulated as:

$$S_{m,n} = \sum_{p,q} e^{i\mathbf{k}_n \mathbf{r}_p} e^{i2\pi[(f_T+f_q)t_1+(f_{evol}+f_q)(t_2(m)-t_1)+(f_R+f_q)\tau_n]} X_q(\mathbf{r}_p), \quad (1)$$

where f_q and $X_q(\mathbf{r})$ represent the q^{th} metabolite frequency and its spatial distribution in the image space, respectively; $(t_2(m) - t_1)$ the evolution time of the m^{th} shot and f_{evol} being the frequency of the rotating frame during this time.

In the following sections, we present the three sequence configurations and only phases influenced by the pulse sequence are addressed and analysed, and not those owed to the CS. Therefore, to successfully maintain the unique-dependence of phase to CS during evolution time, the phase variation between shots at $t_2(m)$ (i.e., $\Delta\phi(t_2)$) should be nil. We considered that the phase accumulated up to t_1 is identical for all shots. In other words, a phase-coherent return $f_R \rightarrow f_T$ is done before the following excitation pulse, resulting in the same starting phase at the beginning of each shot.

Acq-Switch: Switch from f_T to f_R at t_2

For this first case, the phase-continuous frequency commutation from f_T to f_R is done once at $t_2(m)$, i.e., before the acquisition, as presented in Fig. 2 and leading to $f_{evol} = f_T$. Here, the phase accumulated at the beginning of the acquisition for the m^{th} shot is

$$\phi_m(t_2) = 2\pi f_T t_2(m). \quad (2)$$

The phase increment between shots can be expressed as

$$\Delta\phi_{t_2} = \phi_{m+1}(t_2) - \phi_m(t_2) = 2\pi f_T (t_2(m+1) - t_2(m)). \quad (3)$$

One can readily see that the phase increment is dependent on f_T , i.e., the slice position. As soon as the slice is not centered, a phase accumulation due to f_T is added to the CS-dependent phase.

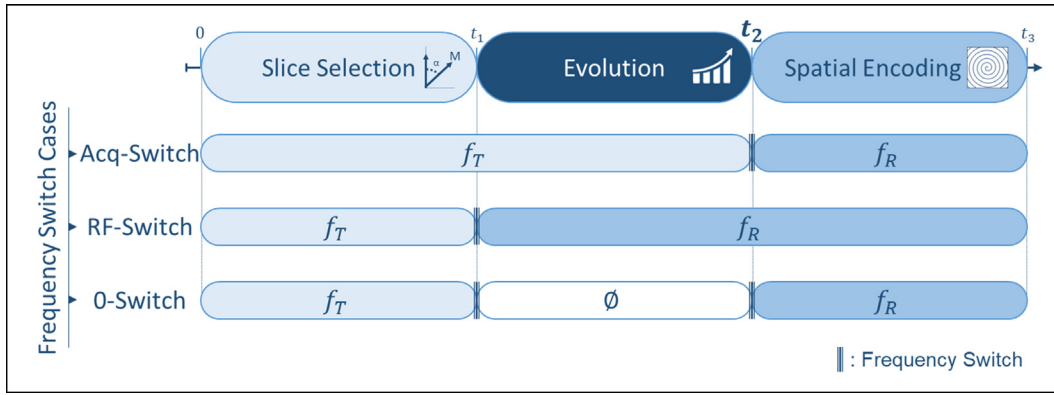


Fig. 2. General imaging pulse sequence timing scheme of a shot (an excitation). Radiofrequency (RF) pulses are applied during the slice selection (t_1) depending on the transmit frequency (f_T). Spatial encoding is applied during the acquisition time ($t_3 - t_2$) depending on the receive frequency (f_R). Spectral information is acquired as the chemical shifts (CS) of interest evolve during an evolution time ($t_2 - t_1$), after the excitation, that is increased for each shot. Three cases of frequency switch are possible, leading to different frequency dependence during evolution times (f_{evol}). **Acq-Switch** case: f_T is switched to f_R right before the acquisition time, **RF-Switch** case: f_T is switched to f_R right before the evolution time, **0-Switch** case: f_T is switched to a 0 transmit frequency before the evolution time (t_1), and this nil frequency is then switched back to f_R at the end of it (t_2).

In practice, this phase shift can be large ($\Delta\phi_{t_2} \gg 2\pi$) compared to the CS-related one and can thus appear to be random due to phase wrapping. To give an order of magnitude, let us consider a pulse bandwidth (BW) of 1 kHz selecting a slice thickness of 1 mm and shifted by 5 mm from the magnet's centre. During a TE of 1 ms, the phase accumulated in this slice is 10π . Incrementing the TE by 0.5 ms adds a spurious phase of 5π . This shot-dependent spurious phase must be removed for each data point (k_n) before metabolite map reconstruction, i.e.,

$$S'_{m,n} = S_{m,n} e^{-i2\pi f_T (t_2(m) - t_2(1))}, \quad (4)$$

where S' and S are the corrected and the raw acquired signal, respectively. The signal has to be corrected with respect to the first shot.

When the frequency commutation from f_T to f_R at t_2 is done in the phase-coherent mode, the rotation of the receiver frame starts from the phase accumulated by the reference rotating frame at this time, achieved by using an NCO. The phase variation due to the excitation is then cancelled and therefore, no spurious phase is accumulated.

RF-Switch: switch from f_T to f_R at t_1

In the second case, the phase-continuous frequency commutation from f_T to f_R is done right after the excitation, at t_1 . The phase variation between consecutive shots depends here on the receive frequency, i.e.,

$$\Delta\phi_{t_2} = \phi_{m+1}(t_2) - \phi_m(t_2) = 2\pi f_R (t_2(m+1) - t_2(m)). \quad (5)$$

Most of the single-shot trajectories require keeping f_R nil to not shift the k-space trajectory. No spurious phase shifts are accumulated between shots ($\Delta\phi_{t_2} = 0$), and therefore, no correction is needed. In the case of $f_R \neq 0$, e.g., for introducing an off-centre shift

as in spin-warp encoding [25], the resulting spurious phase should be corrected in the acquired signal as in Eq. (4) but by substituting f_T by f_R , i.e.,

$$S'_{m,n} = S_{m,n} e^{-i2\pi f_R (t_2(m) - t_2(1))}. \quad (6)$$

Since the commutation is done before echo time increments at t_1 , the spurious phase problem persists for $f_R \neq 0$ in the phase-coherent mode, and the correction presented in Eq. (6) remains crucial.

0-Switch: double switch, from f_T to 0 at t_1 and from 0 to f_R at t_2

In the last case, a double switch is done during the pulse sequence. A first switch from the transmit frequency f_T to a 0 one is done right before the evolution time at t_1 , and then switched again to the receive frequency f_R at t_2 . In this case, for both phase-continuous and phase-coherent modes, no additional phase is accumulated at t_2 even if the slice and/or the readout position are shifted.

Phase correction requirements for the three commutation cases (Acq-, RF- and 0-Switch) and in the two switch modes (phase-continuous and -coherent modes), are summarized in Table 1.

3. Method

All the experiments were performed on a BRUKER 117/16 (11.7 T) horizontal bore magnet equipped with a BGA-9 gradient coil (BRUKER BioSpin MRI GmbH). The magnet reference resonance frequencies were 500.34 and 125.83 MHz for ^1H and ^{13}C , respectively.

The phantom was composed of four syringes filled with either [^{13}C]Pyruvic acid (16.4 M, ~ 0 Hz), [^{13}C]Lactate (4 M, ~ 985 Hz), [^{13}C]Alanine (1.85 M, ~ 135 Hz) or [^{13}C]Urea (16.4 M, ~ 1500 Hz) fixed in 10% gelatine. A $^1\text{H}/^{13}\text{C}$ volume coil (72 mm internal diameter; RAPID Biomedical GmbH, Rimpf, Germany) was used to excite both nuclei and receive the ^1H signal. ^{13}C

Table 1

Phase correction requirements during IDEAL-type sequences for Acq-, RF- and 0-Switch cases and in the phase-continuous and phase-coherent $f_T \rightarrow f_R$ switch modes.

Switch Cases		Switch Modes	
		Phase-Continuous	Phase-Coherent
Acq-Switch		Correction if $f_T \neq 0$ following Eq. (4)	No Correction needed
RF-Switch		Correction if $f_R \neq 0$ following Eq. (6)	
0-Switch		No Correction needed	

signal reception used a single-loop rat brain surface coil (RAPID Biomedical GmbH, Rimpfing, Germany). ¹H images were recorded with a fast low angle shot method (FLASH) to validate the phantom position inside the magnet. For ¹³C, a 15 mm thick slice was set to make sure a sufficient signal to noise ratio (SNR) was reached in a reasonable time. The field of view (FOV) was 50 × 50 mm² with an image matrix of 64 × 64 and a reception BW of 400 kHz. Each one of the RF excitation pulses used was a Shinnar-Le Roux (SLR) set to 90° with a duration of 2.1 ms and a spectral BW of 2 kHz, exciting the whole ¹³C-labelled nuclei window. The TR between each pulse excitation was set to 10 s and 26 averages per scan were acquired to ensure sufficient SNR. Seven scans were recorded; the first one at $t_2(1)$ of 1.69 ms and then increased in increments of 0.86 ms for the other scans. The spatial encoding was performed with a spiral out trajectory.

Images were acquired at two slice positions, 0 and -4 mm, leading to a transmit frequency f_T of 0 and -533 Hz, respectively. For the shifted slice, acquisitions were recorded in the phase-continuous mode, and for both, Acq-Switch and RF-Switch cases. The phase correction was only applied in the Acq-Switch case, following Eq. (4). For metabolic map reconstruction, the two-step process described in [15] was applied. Knowing the resonance frequencies of the metabolites, a k-space data was first reconstructed for each one fitting the signals acquired from all shots. These individual metabolite k-space data were then spatially reconstructed into metabolic maps.

Data processing for all experiments was performed on Matlab® R2019a (MathWorks, Natick, MA, USA) with home-made written

scripts. The dataset of this work is available at the following link <https://doi.org/10.15454/LY4VVKC>.

4. Results

Fig. 3 illustrates the application of both Acq- and RF- switch cases. It shows four columns, one for each metabolite. The ¹³C maps are superimposed on a ¹H reference image of the phantom for clear syringe borders. The 1st row presents the control maps, i.e., generated at the centre of the magnet where $f_T = 0$ (Acq-Switch case). The metabolic maps reconstructed for each of the metabolites fit with the corresponding syringe placement. As soon as the slice was shifted ($f_T \neq 0$), it was impossible to reconstruct the correct metabolic maps (2nd row) without correcting the raw signal to cancel the effect of the spurious phase acquired due to the slice offset (3rd row). When using the RF-Switch case (4th row), such artefacts were not observed. The 0-Switch case was unnecessary, hence not applied.

5. Discussion

Phase correction can be mandatory in some slice-selective IDEAL-type protocols depending on how the transmit/receive frequency switch is performed. Without phase correction, the slice selection or readout frequency offset can bias the CS-related phase evolution by adding different spurious phases during each shot.

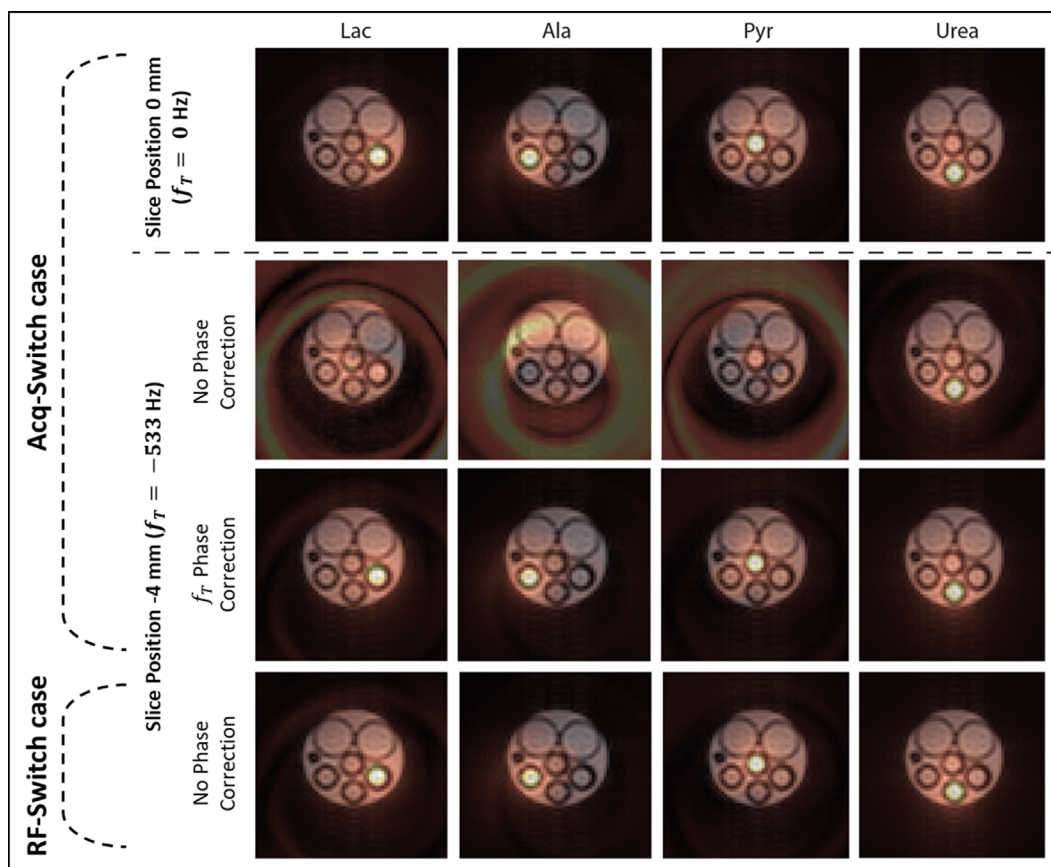


Fig. 3. Reconstruction of the ¹³C metabolite maps acquired with the IDEAL spiral method (Lac = lactate; Ala = alanine; Pyr = pyruvic acid). For a slice centred at 0 mm, the map reconstruction of the data acquired with the **Acq-Switch** case was performed with no correction (top line). Lines 2 and 3 are ¹³C metabolite maps acquired with the same switch case, but with a shifted slice (-4 mm), before and after phase correction. Urea map in line 2 was an artefact result due to frequency aliasing – as its frequency is equal to $3f_T$. Line 4, the **RF-Switch** case was used where no correction is required.

In our practical case, only phase-continuous switch is allowed for the commutation from the transmit to the receive frequency ($f_T \rightarrow f_R$) on the scanner. Although the proposed phase correction is valid to eliminate the possible spurious phases accumulated during the pulse sequence, it is desirable to avoid them. This is achieved by switching from the transmit frequency f_T to the reference frequency at t_1 . To do so, two options are possible: the RF-Switch case if and only if $f_R = 0$, or the 0-Switch case. In return, if the phase-coherent switch mode is at hand, one should favour the $f_T \rightarrow f_R$ commutation at t_2 before the acquisition, as it discharges one from any post-processing phase correction. Lastly, when the commutation mode is unknown, the only case requiring no correction is the proposed 0-Switch case.

Generally speaking, these phase accumulation artefacts are encountered as soon as several images obtained from different excitations with different TEs are processed together to extract the CS-related information. For example, this can be the case in high-spatial resolution B_0 -mapping, e.g., for susceptibility-weighted imaging [26]. Indeed, to reach a sufficient Nyquist limit, the TE must be incremented by a small delay, thus requiring image acquisition from multiple excitations. In this case, the same issues may be encountered and the described solutions remain valid.

While the described approaches cancel unwanted phase accumulation due to frequency commutation's mode and position, they do not correct for other mechanisms leading to additional spurious phase. One of the critical sources of phase errors is any physiological motions. To obtain exploitable data, it is then important to avoid such movements during the signal encoding and acquisition. To do so, using a trigger on one of the physiological parameters, a navigator echo [27] or one of the solutions mentioned in the introduction [21–23] is still mandatory.

We focused on the phase effects in IDEAL-type pulse sequences, due to the transmit-receive commutation before the acquisition time. However, for methods using multiple RF pulses and being phase cycled, similar frequency issues may arise and lead to inoperative coherence selection, as they may spoil the desired phase cycle [24].

To conclude, we demonstrated that the position and the mode of the frequency commutation in the pulse sequence are critical to record only the CS-dependent phase evolution. This point is under-addressed in the scientific literature and therefore relatively unclear for MRSI users. Regardless of the hardware efficiency and the sequence implementation, we proposed several solutions to eliminate possible spurious phase in rapid metabolic imaging.

Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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