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1 Development and validation of a comprehensive 1-D model to simulate gas hold-up

2 and gas-liquid transfer in deep air-water bubble columns

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Abstract

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This study proposed to develop a model coupling hydrodynamics and mass transfer in order to gain an understanding of measurements taken on air-water bubble columns with low gas hold-up. Three experimental datasets with various operating conditions (water quality, liquid height, air flow range) were chosen. The model analyzes and interprets the significant impact of the local hydrostatic pressure and the effects of contamination on hydrodynamic and mass transfer parameters. The oxygen concentration in gas significantly depletes with the distance from diffusers, which explains the difference between the calculated mean of the local $\langle k_L a \rangle$ and global $\langle k_L a \rangle$ coefficients. This difference is highly significant for a high bubble column and/or systems with a low mean bubble size. The impact of water quality on mass transfer can be characterized by the contamination angle using comprehensive 1-D modeling and highlights a differentiated impact on the hydrodynamic or mass transfer parameters.

Keywords

24 1D Model, Oxygen mass transfer, Aeration, Wastewater treatment, Bubble column

1. Introduction

In the domain of water and wastewater treatment and recovery, gas-liquid reactors are often used to perform gas-liquid oxygen mass transfer. In particular, air bubbles are injected in aeration tanks to provide microorganisms with the oxygen they require for their growth. Aeration systems in these processes must be efficient in terms of mass transfer coefficients, easy to construct, with no moving parts and a low pressure drop through the air diffusers (Manjrekar 2016). In this study, an analogy is made between bubble columns and wastewater aeration tanks, since they can both operate in the bubbly flow regime with similar heights and gas hold-up ranges. Indeed, using a deep bubble column allows one to reproduce the water heights and gas-liquid contact times encountered in aeration tanks (Gillot and Héduit 2008, Duran et al. 2016, Baeten et al. 2020). Similarly, air flowrates can be set to obtain gas superficial velocities and gas hold-ups ranges used in aeration tanks (Shah et al. 1982, Duran et al. 2016, Amaral et al. 2018). This analogy aims at helping reach a better understanding of fundamental phenomena that affects gas-liquid mass transfer in the bubbly flow regime, in order to optimize the aeration systems that remain the main energy consumer in water resource recovery facilities (Rosso and Stenstrom 2005, Longo et al. 2016). For systems with low gas hold-ups (< 5%) and fine bubble diffusers, air bubbles are spherical or ellipsoidal with few coalescence and break-up phenomena (Talvy et al. 2007a, Colombet et al. 2015). However, bubble coalescence is more likely to occur in systems with denser bubble swarms and higher gas hold-ups and bubble diameters. In an air-water bubble column with fine bubble diffusers, the homogeneous flow regime without coalescence can be maintained under a transitional gas superficial velocity between 0.04 and 0.08 m/s (Mudde et al. 2009). In Besagni et al. (2016), the coarse gas sparger used led to an early disruption of the bubbly flow due to both non-uniform distribution and changes in bubble size generation. Loubière et al. (2003) also pointed out that bubble size variation depended upon the type of diffuser with a flexible porous membrane, the initial bubble size increases as the superficial gas velocity rises, whereas when using a rigid orifice, bubble size varies slightly depending on superficial gas velocity.

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In air-water systems, the effect of bubble contamination on mass transfer is another frequently observed process and is mainly due to surfactants (Pöpel and Wagner 1994; Capela et al. 2002; Sardeing et al. 2006, Rosso et al. 2006, Jimenez et al. 2014) as well as aqueous salt solutions such as in biological media (Zlokarnik 2005). Contaminated bubbles yield lower mass transfer coefficients than perfectly clean bubbles, even though the level of bubble contamination may be difficult to quantify (Sardeing et al. 2006, Xu et al. 2018). Water height also has an impact on overall mass transfer (Deckwer et al. 1974, Giovannettone and Gulliver 2008) since the gradients of the gas-phase composition and pressure appear to have highly interactive non-linear effects (Baeten at al. 2020). First, bubble diameter varies with hydrostatic pressure (Capela et al. 2002, Giovanettonne et al. 2009, Fayolle et al. 2010, Amaral et al. 2018), which has an influence on the gas-liquid interfacial area. In addition, the oxygen saturation concentration varies depending upon column height (Rubio et al. 1999) and the dissolved oxygen concentration profile at steady state can be very pronounced, suggesting local variation of the transfer rate even if the overall net transfer of oxygen is close to zero (Giovannettone and Gulliver 2008). The combination of these phenomena induce oxygen depletion in air bubbles, essentially explained by competition between the transfer rate and bubble convection (Talvy et al. 2007a, Giovanettonne and Gulliver 2008, Baeten et al. 2020). To provide a comprehensive description of gas transfer inside deep air-water bubble columns, the classical one-dimensional two-fluid model (Wallis 1969, Cockx et al. 1997, Camacho-Rubio at al. 2001, Vitankar and Joshi 2002) developed in previous studies for airlift reactors, aeration tanks or bubble columns has been extended (Talvy et al. 2007a, Talvy et al. 2007b, Colombet et al. 2013). Since the transfer rate gradient increases with the height of the bubble column via the various wellidentified mechanisms discussed above, all these phenomena need to be combined in a new model structure where both hydrodynamics and mass transfer are solved together to consider the effect of pressure and gas depletion.

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One-dimensional (1-D) models are simple but rigorous and appear to be relevant when applied to bubble columns since gas flows are mainly in the vertical axis. Most existing models consider a constant superficial gas velocity since they apply to low height columns (Talvy 2007b, Colombet et al. 2013) and thus the pressure effect can be ignored. However, this may not be the case for columns with a high liquid height, as shown in studies taking the effect of pressure on gas solubility into account (Dhaoudi et al. 2008), or both gas solubility and gas flowrate (Giovanettone and Gulliver 2008, Baeten et al., 2020). In these investigations, the overall mass transfer coefficient K_La was considered, even though representing hydrodynamic variations together with changes in mass transfer (separating k₁ from a) would be more useful to better interpret experimental results. In this context, the aim of this study was to develop a model that couples hydrodynamics and mass transfer in order to gain an understanding of measurement results obtained on systems with low gas hold-up under different configurations. Based on a literature review, the correlations that can be used to represent hydrodynamic and mass transfer phenomena (drag coefficient, mass transfer coefficient, collective bubble effects due to high gas hold-up) were identified. The simulation results were compared to observed data obtained in three experimental setups showing contrasting operating conditions (in terms of water height, gas hold-up, bubble diameter and interface contamination). Their specific relevant hydrodynamic and oxygen transfer phenomena were analyzed by modeling and simulation. To begin, after presenting the experimental datasets, the different processes considered in the comprehensive model are described. Subsequently, the simulated results are compared with the experimental data to choose between the different options concerning the model structure (closure relations) and to interpret the experimental results obtained under varied operating conditions.

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2. Material and methods

The proposed 1-D model is used to investigate the results extracted from three experimental datasets obtained in clear water (Colombet et al. 2015, Duran et al. 2016, Amaral et al. 2018).

2.1 Experimental datasets

The database is composed of three experimental datasets obtained in bubble columns showing a low gas hold-up (less than 6%). They were selected because of their wide range of operating conditions (superficial gas velocity and gas hold-up) and the availability of data. Table 1 presents the main operating conditions for the three experimental datasets.

Table 1. Experimental conditions for the bubble column datasets

Dataset	Continuous fluid phase	Bubble sparger type	H _∟ (m)	d _B expressed at P _{atm} (× 10 ⁻³ m)	j _g at P _{atm} (× 10 ⁻³ m/s)	ε _g (%)	Reference
D1	Tap water	EPDM membrane	1.30	1.5 - 1.8	0.3 - 1.2	0.1 - 0.4	Amaral et al. (2018)
D2	Tap water	EPDM membrane	4.40	3.0 - 4.0	2.0 - 4.5	0.5 - 1.5	Duran et al. (2016)
D3	Filtered tap water	Capillaries	0.76	2.3 - 3.4	2.0 - 15.5	0.5 - 6.0	Colombet et al. (2015)

With : d_B mean bubble diameter, P_{atm} standard atmospheric pressure (1013 hPa), j_g superficial gas velocity, ϵ_g

overall gas hold-up, H_L liquid height.

The water quality slightly differed from one dataset to another. In particular, the liquid used in Dataset D3 was filtered tap water (15 μ m cutoff threshold) and tap water for D1 and D2.

Datasets D1 and D2 were obtained in bubble columns equipped with EPDM membrane diffusers, similar to the ones installed in full-scale aeration tanks. For Dataset D1, the water height was quite low (1.30 m). The superficial gas velocity and associated mean bubble size and gas hold-up were significantly lower in comparison to the other datasets. Dataset D2 corresponds to the experimental bubble column with the highest liquid height (4.5 m) in the lower range of liquid heights found in industrial aeration tanks, which allows for the study of the impact of hydrostatic pressure on hydrodynamics and mass transfer phenomena. A more complete description of this experimental dataset is provided in the following section, given that clear water results are not fully described in the published article (Duran et al. 2016).

Figure 1 presents hydrodynamic and mass transfer characteristics as a function of the superficial gas velocity for Dataset D2.



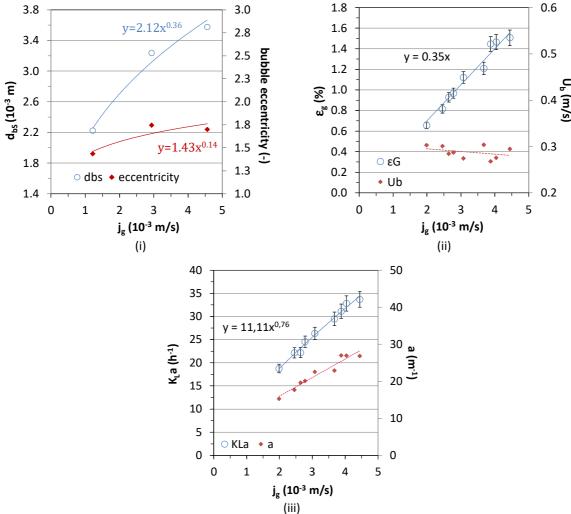


Figure 1. (i) Mean bubble Sauter diameter and mean bubble eccentricity measured at 1 m in height from the diffuser, (ii) overall gas hold-up (ϵ_g) and mean bubble rise velocity (U_b) at 20°C, (iii) overall oxygen transfer coefficient K_La expressed at 20°C and gas–liquid interfacial area (a) as a function of the superficial gas velocity – dataset D2

The mean bubble Sauter diameter increased from 2.2 to 3.6 mm with an increase in the superficial gas velocity (j_g) from 1.2 to 4.6 mm/s. The effect of the airflow rate on bubble size was more significant at lower superficial gas velocities because the membrane stretches and the pore size increases under the effect of the pressure associated with the airflow rate. Concerning the bubbles'

shape, their eccentricity slightly increased from 1.4 to 1.7 with the increase of the superficial gas velocity. Classically, the overall gas hold-up is a linear function of the superficial gas velocity, whereas the oxygen transfer coefficient follows a power law. The mean bubble rise velocity deduced (U_b = j_g/ϵ_g , for homogeneous distribution of gas along the column's surface) slightly decreased as the superficial air velocity increased. The reduction of Ub can be attributed to the collective effects (the interaction between bubbles) that ended up with higher bubble drag coefficients, as explained by Colombet et al. (2011). Since the estimated K_L coefficient ($K_L=K_La/a$) remains almost constant within the range of the jg studied, the increase in the overall oxygen transfer coefficient (KLa) is mainly related to the increase in the interfacial area (estimated form d_{bs} , ϵ_g and bubble eccentricity; see Eq. 30 below). Dataset D3 includes a wide range of superficial gas velocities and gas hold-up, even though the water height is lower in comparison with the other datasets. The bubble injection system consists of a network of stainless steel capillaries (with an inner diameter of 0.2 mm), that makes it possible to obtain a homogeneous bubble swarm. In contrast, the diffuser of the two other datasets, a porous EPDM membrane, provides a more heterogeneous initial bubble size distribution as commonly found in water treatment. In order to focus on low gas hold-up systems, the data considered were limited to gas hold-up lower than 6%, despite the wider range in the complete study (Colombet et al. 2013). On the basis of transfer numbers (N_T), these datasets were compared with different previous databases from lab-scale (Capela et al., 2002) to full-scale aeration tanks (Fayolle et al. 2010, Fayolle et al. 2011). This dimensionless group ($N_T = \frac{K_L a_{20}}{j_g} \left(\frac{\mu_L^2}{\rho_L^2 g}\right)^{1/3}$) defined by Zlokarnik (1979) and Roustan (1996) has the same physical meaning as the specific standard oxygen transfer efficiency (SSOTE in %) per meter of diffuser submergence for clear water operating conditions (Gillot et al. 2005). Figure 2 presents the transfer number as a function of the mean Sauter bubble diameter for

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the different databases selected and datasets D1-D3.

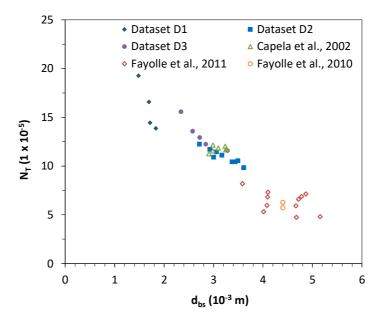


Figure 2. Transfer number (N_T) versus bubble Sauter diameter for selected databases (lab-scale [Capela et al., 2002] and full-scale [Fayolle et al., 2010 and 2011]) and datasets 1−3.

For reactors with different configurations (from pilot scale to full-scale reactors), the transfer number (N_T) seemed to be determined by the Sauter diameter, which fixes the bubble surface mobility and the G-L interfacial area by controlling the overall gas hold-up. The results also clearly demonstrate that the transfer number is an adequate scale-up factor for systems equipped with fine bubble diffusers. Likewise, through the comparison with data obtained at full-scale, these results validate the representativeness of the three datasets in terms of mass transfer mechanisms.

2.2. Two-Phase One-Dimensional Model

The proposed model is a 1-D model derived for low soluble gas mass transfer into a liquid in deep bubble columns, applied to an air—water system (O₂ is considered to be the only gas transferred). Since the calculated variables are homogenous and evenly distributed along the cross section, a 1-D approach can be considered. The model first calculates hydrodynamic variables (gas hold-up, changes in bubble diameter, gas velocity) considering steady-state conditions. Then, hydrodynamic results are used as input values to calculate the transient oxygen mass transfer from the gas phase to

the liquid phase. The impact of the oxygen transfer on the bubble size and associated hydrodynamics is ignored.

Contrary to other existing 1-D models (Giovannettonne and Gulliver, 2008, Baeten et al. 2020), the impact of pressure on gas superficial velocity and bubble diameter is taken into account and its impact on gas hold-up and mass transfer is fully considered and analyzed. The model is based on a simplified Eulerian two-fluid model such as reported in Talvy et al. (2007a,b), where mass balance for the gas and liquid phases and momentum interactions between the two phases are considered. The proposed model implies different hypotheses related to the considered system (oxygen transfer in batch air-water bubble column with low gas hold-up): (i) the impact of the mass transfer on the bubble size and associated hydrodynamics is neglected, (ii) no vertical liquid flow is considered, (iii) the bubbly flow is homogeneously distributed along the cross-section of the bubble column and (iv) coalescence is neglected. The column is discretized along its height (50 layers along z), so the variables are calculated locally at each discretization point.

Table 2 summarizes the values considered for the fluid properties and the main parameters of the model (T = 20°C and $P_{ref} = 1$ atm).

Table 2. Physico-chemical properties of the system (T = 20° C and $P_{ref} = 1$ atm)

Parameter	Value	Unit
Water density, ρ∟	998.2	kg/m³
Water dynamic viscosity, μ∟	1.10 ⁻³	Pa.s
Water surface tension, σ	73	mN/m
Air density, ρ _G	1.2	kg/m³
Oxygen diffusivity in water, D	2.10 ⁻⁹	m²/s
Gravity constant, g	9.81	m/s²
Temperature, T	20	°C
Atmospheric pressure, (P _{ref})	1	atm

2.2.1. Equation of the 1-D model

All variables were averaged along each cross section of the column in order to provide a simple 1-D model. As an example, the local gas hold-up in a cross-section S is given in Eq.1 (Talvy et al., 2007b).

$$\varepsilon_k = <\alpha_k> = rac{1}{S} \iint_A \alpha_k dS$$
 (Eq. 1)

- where ε_k is the mean gas hold-up in the section, and α_k is the local gas hold-up at a specific point in the section. For the velocities, only the averaged axial components are different from zero and
- velocity vectors are thus reduced to scalars in the following.
- 202 2.2.2. Model structure: steady state hydrodynamic calculation
- The hydrodynamic equations solved in the model are presented in the following sections.
- 205 2.2.2.1 Mass and flow rate conservation equation
- The mass balance equation in a diphasic system is written as follows (Talvy et al. 2007a):

$$\frac{\partial \alpha_k \rho_k}{\partial t} + \nabla \alpha_k \rho_k \overline{U_k} = \overline{m_K}$$
 (Eq. 2)

- where α_k is the volume fraction, ρ_k the density and $\overline{U_k}$ the average velocity of phase k, which stands
- for gas (g) or liquid (l). The first term on the left side corresponds to mass variation over time in
- 209 phase k, the second to mass transport by advection in the phase k, and the term on the right side
- 210 $(\overline{m_K})$ corresponds to a statistical average mass transfer between the two phases.
- 211 In a 1-D system, Eq.2 becomes:

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$$\frac{\partial (\varepsilon_k \rho_k)}{\partial t} + \frac{\partial}{\partial z} (\varepsilon_k \rho_k U_{kz}) = \langle m_k \rangle \tag{Eq. 3}$$

- 212 With a steady state flow and assuming that average mass transfer between phases implied in the
- 213 mass balance is ignored, the equation becomes for the liquid and the gas, respectively:

$$\varepsilon_l \rho_l U_l = Cst = \rho_l \frac{Q_l}{S} = \rho_l j_l \tag{Eq. 4}$$

$$\varepsilon_g \rho_g U_g = Cst = \rho_g \frac{Q_g}{S} = \rho_g j_g$$
 (Eq. 5)

- where Q_k and j_k are the flow rate and the superficial velocity (m/s), respectively, of phase k.
- 215 If it is considered that there is no liquid flow (j_i = 0, as in a batch bubble column), only the equation
- 216 for the gas phase remains and the previous equation becomes:

$$\varepsilon_g = rac{j_g}{U_g}$$
 (Eq. 6)

since the sum of the different phase volume fractions is equal to unity:

$$\varepsilon_l = 1 - \varepsilon_q$$
 (Eq. 7)

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- 2.2.2.2 Gas velocity equation: the Zuber and Findlay drift flux model
- 220 Zuber and Findlay (1965) proposed the following interfacial momentum transfer model:

$$U_q = C_0 j + G = C_0 (j_q + j_l) + G$$
 (Eq. 8)

- 221 Gas velocity (Ug) has two components, the first one corresponds to the gas transport resulting from mixing (induced by mixture velocity j composed of gas and liquid superficial velocity, j_{g} and j_{l} 222 respectively) and the second one is gas slip velocity G, which corresponds to gas transport due to 223 224 buoyancy. The latter will be further developed below. The drift-flux coefficient (C₀) is related to the 225 non-uniformity of the gas-liquid flow field in the cross section and can be estimated from 226 computational fluid dynamics (CFD) simulations, as in Talvy et al. (2005). However in the case of a 227 homogeneous flow it can be considered close to 1. On the other hand, its extreme value would be 228 1.5 in the case of a spatially heterogeneous bubbly flow (Talvy et al. 2005).
- 229 With a homogeneous flow ($C_0 = 1$) and without the liquid flow rate ($j_L = 0$), the previous equation
- 230 becomes:

$$U_g = j_g + G \tag{Eq. 9}$$

- For homogeneous bubble columns at a low gas flow rate, $j_g << G$ and then the gas velocity U_g is finally
- assumed equal to the bubble slip velocity G.
- 233 Note that when the drift flux coefficient C₀ is equal to 1, radial gas fraction profiles are not considered
- and thus radial interfacial forces as lift and turbulent dispersion are neglected for the axial resolution
- 235 (Talvy et *al.*, 2007a, b).

2.2.2.3 Gas slip velocity equation

A force balance applied to a rising gas bubble in a quiescent liquid and at steady state where the bubble has reached its terminal rising velocity consists in equilibrium between buoyancy and drag forces. The added mass force can be neglected in 1D models after a very short distance from the bubble sparger, when the fully developed gas velocity is established (Talvy et *al.*, 2007a, Colombet et *al.*, 2013). Thus, after simplification, the slip velocity G between the two phases can be calculated using Eq. 10 (Talvy et al. 2007b):

$$G = \sqrt{\frac{4}{3} \frac{d_v^3}{d_p^2} \frac{(\rho_l - \rho_g)}{\rho_l} \frac{g}{C_D}}$$
 (Eq. 10)

with g the gravity constant (9.81 m/s 2), d_V the volume equivalent bubble diameter (m), C_D the drag coefficient (-), and d_P the surface equivalent bubble diameter (m).

Furthermore, if the two equivalent diameters are considered equals ($d_v = d_p = d_B$, for a spherical bubble, for example) and if gas density is ignored in comparison with liquid density, the following simplified equation is obtained:

$$G = \sqrt{\frac{4}{3} d_B \frac{g}{C_D}}$$
 (Eq. 11)

251 2.2.2.4 Drag coefficient equation

Several correlations to calculate the drag coefficient exist in the literature, mostly expressed through dimensionless numbers. In the case of a single rigid particle, the following law involving the Reynolds number can be applied (Schiller and Naumann 1938):

$$C_D = \begin{cases} \frac{24}{Re} * (1 + 0.15 Re^{0.687}) for Re < 1000 \\ 0.44 for Re > 1000 \end{cases}$$
 (Eq. 12)

- 255 However, even though this correlation is often used for rigid spherical bubbles, it is not suitable for 256 oblate ellipsoidal bubbles where the eccentricity effect drastically affects the drag coefficient (Talvy 257 et al. 2007b).
- 258 With ellipsoidal bubbles, when the surface tension effects are significant, drag laws based on the 259 Eötvös number are more relevant (Tomiyama et al. 1998, Dijkhuizen et al. 2010). The Eötvös number
- 260 (Eo), the ratio of buoyancy to surface tension, is defined as follows:

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$$Eo = \frac{\left(\rho_l - \rho_g\right) g \ d_B^2}{\sigma} \tag{Eq. 13}$$

- where d_B is the bubble diameter (m) and σ is the liquid surface tension (N/m).
- To analyze the impact of the effects of contamination on hydrodynamics, two drag laws depending on the Eötvös number were selected. On one hand, the drag law proposed by Dijkhuizen et al. (2010), developed using direct numerical simulation (DNS) and without contamination effects, is considered as representative of a perfectly clean bubble surface (Eq. 14).

$$C_{D0} = \frac{8}{3} \frac{Eo}{\frac{19}{3} + \frac{2}{3} Eo}$$
 (Eq. 14)

On the other hand, the drag law proposed by Tomiyama et al. (1998), based on experimental results, is considered as representative of classical experimental conditions with a slightly contaminated system (Eq. 15).

$$C_D = max \left\{ min \left\{ \frac{24}{Re} (1 + 0.15Re^{0.687}), \frac{72}{Re} \right\}, \frac{8}{3} \frac{Eo}{(4 + Eo)} \right\}$$
 (Eq. 15)

These drag laws are based on single bubbles rising in liquid. For bubble swarms, a corrective factor, depending on gas hold-up, can be taken into account to consider a hindered slipping gas velocity (Eq.16; Wallis 1961):

$$C_D = C_{D0} \left(1 - \varepsilon_g \right)^{-2} \tag{Eq. 16}$$

2.2.2.5 Hydrostatic pressure equation and impact on gas superficial velocity and bubble diameter

275 Hydrostatic pressure at a height z in a deep bubble column is given by Eq. 17.

$$P(z) = P_0 + \rho_m g (H - z)$$
 (Eq. 17)

- where P₀ is the atmospheric pressure (Pa), g the gravity constant (m/s²), H the column height (m),
- and ρ_m the mix density (or apparent density), defined as:

$$\rho_m = \rho_l \left(1 - \varepsilon_g \right) + \rho_g \varepsilon_g \tag{Eq. 18}$$

- Where ρ_l and ρ_g are the liquid and gas densities, respectively (kg/m³).
- 280 Moreover, bubble diameter evolves with pressure according to the following equation (Pöpel and
- Wagner 1994; Fayolle et al. 2010), derived from the ideal gas equation when the mass transfer can
- be ignored in the mass balance (Eq. 19):

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$$d_B = d_{B0} \sqrt[3]{\frac{P_0}{P}}$$
 (Eq. 19)

- where d_{B0} is the bubble diameter at atmospheric pressure P₀ (m), and d_B the bubble diameter at
- 284 pressure P(z). The bubble diameter at atmospheric pressure is an input datum that must be
- measured or estimated since it depends on the gas sparger and water properties.
- Gas superficial velocity j_{g0} at atmospheric pressure P_0 and superficial gas velocity j_g at pressure P(z)
- are bound through the following equation, which is also derived from the ideal gas equation:

$$j_g(z) = j_{g0} * \frac{P_0}{P(z)}$$
 (Eq. 20)

290 2.2.3. Mass transfer calculation

Even though the hydrodynamic phenomena can be considered to reach a steady state, mass transfer is fundamentally a transient phenomenon, using as input the hydrodynamic variables previously calculated (gas hold-up, gas velocity, pressure, and bubble diameter along the column height). To simulate oxygenation dynamics measured via reaeration tests (see 3.2), species transport equations are presented for oxygen in a two-phase flow as in Talvy et al. (2007a) and further modified in order to integrate the pressure effect for deep bubble columns.

When considering a perfectly mixed liquid without a liquid flow rate (batch bubble column), the oxygen concentration equation in the liquid is written as follows for a 1-D system:

$$\frac{\partial C_l(t)}{\partial t} = \langle \frac{k_L a(z)}{1 - \varepsilon_g(z)} \left(C_l^*(z, t) - C_l(t) \right) \rangle \tag{Eq. 21}$$

$$C_l^*(z,t) = He_{02}(T) M(O_2) x_q(z,t) P(z)$$
 (Eq. 22)

The oxygen concentration in the liquid (C_1) is expressed as a mass concentration and C_1^* is the saturation concentration at equilibrium. The variation of oxygen concentration in the liquid phase over time results from a transfer term from the gas to the liquid. The parameters $k_L a$ and E_g are the mass transfer coefficient and gas hold-up, respectively, $He_{O2}(T)$ the Henry law coefficient at temperature T for oxygen solubility in water ($1.24 \times 10^{-5} \text{ mol/m}^3/Pa$ at $25^{\circ}C$), $M(O_2)$ the oxygen molar mass (32 g/mol), $x_g(z)$ the local oxygen molar fraction in the gas phase at height z and P(z) the local hydrostatic pressure.

Because of the perfectly mixed liquid assumption, only one equation for the whole liquid volume is considered, and the parameters $k_L a$, ϵ_g and C_I are taken as their average value in the column for the calculation. The oxygen concentration in the gas phase $C_g(z)$ can be calculated by the ideal gas equation from the oxygen molar fraction $x_g(z)$. As for the liquid, the oxygen concentration in the gas phase changes over time, although it is difficult to measure.

Thus, for low soluble gases, the 1-D transfer equation in the gas phase gives (Talvy et al., 2007):

$$\frac{\partial \varepsilon_g C_g(z,t)}{\partial t} + \nabla \varepsilon_g(z) C_g(z,t) U_g(z) = -k_L a(z) (C_l^*(z,t) - C_l(t))$$
 (Eq. 23)

The first term on the left side corresponds to the evolution over time and the height of the oxygen concentration in the gas phase, the second to the transport term of oxygen by the gas velocity and

the term on the right side is the oxygen transfer term from the gas to the liquid. In the gas phase, neither diffusion nor reaction is considered, since the model applies for homogeneously dispersed bubbly flow where no coalescence between bubbles occurs.

When solving the equation of the oxygen molar fraction in the gas phase, it gives an expression with a first order discretization for the gas phase convective transport:

$$\frac{\partial x_g(z,t)}{\partial t} = -\frac{k_L a(z)}{\varepsilon_g(z) * \frac{M(O_2)}{RT} \left(P(z) - P_{vap}\right)} \left(C_l^*(z,t) - C_l(t)\right) - \frac{U_g(z)}{\Delta z} \Delta C_g(z,t) \tag{Eq. 24}$$

where $k_La(z)$ is the local mass transfer coefficient, R the ideal gas constant (8.314 J/mol/K), and $U_g(z)$ the local bubble velocity. The gas concentration variation over time therefore results from a negative transfer term from the gas to the liquid, and from a transport term related to the gas phase velocity. Equation 24 is solved for each z-position in the column following the z-axis: the oxygen molar fraction in the gas $x_g(z)$ is then calculated for each height over time with the local hydrodynamic parameters solved from the equations provided in section 2.2.2. In this model, the hydrodynamic parameters have a local impact on local mass transfer, but the reverse is not considered given that the oxygen depletion in the gas phase can be ignored for the gas flow rate (Talvy et al. 2007a, Baeten et al. 2020).

2.2.4. Models for mass transfer coefficients

The mass transfer coefficient $k_L a$ could be expressed in terms of the interfacial area a and the liquidside mass transfer velocity k_L (m/s). To estimate the latter, there are several existing models and, as for the drag coefficient, they depend on whether or not the bubble interface is contaminated (Dani et al. 2007, Xu et al. 2018).

On one hand, the Higbie model is very commonly used and corresponds to the ideal case of perfectly clean (non-contaminated) bubbles, which have a renewable interface: the diffusional oxygen transfer in the liquid film surrounding gas bubbles occurs when the liquid elements reach the gas-liquid

338 interface and during a short contact time (t_c) they attain the concentration equilibrium with the 339 interface. Under these conditions, the mass transfer coefficient is written as (Higbie 1935):

$$k_L = 2\sqrt{\frac{D}{\pi t_c}} = 2\sqrt{\frac{D G}{\pi d_B}}$$
 (Eq. 25)

- where k_L is the liquid side mass transfer coefficient (m/s), D the diffusion coefficient of oxygen in 340 water (m^2/s) , t_c the contact time (s), G the gas slip velocity (m/s) and d_B the bubble diameter (m).
- 342 On the other hand, the case of completely contaminated bubbles is described by the Frössling model,
- 343 which assumes that bubbles have a rigid, non-renewable interface. The mass transfer coefficient is
- 344 then expressed as (Frössling 1938):

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$$k_L = \frac{D}{d_B} * (2 + 0.6 * Re^{0.5} * Sc^{0.33})$$
 (Eq. 26)

where the Reynolds and Schmidt dimensionless numbers are defined as: 345

$$Re = \frac{\rho_l d_B G}{\mu_l}$$
 (Eq. 27)

$$Sc = \frac{\mu_l}{\rho_l D}$$
 (Eq. 28)

- where ρ_l and μ_l are respectively density (kg/m³) and the dynamic viscosity (Pa.s) of the liquid. 346
- 348 In practice, the k coefficients calculated with the Frössling correlation are much lower than with the Higbie model, i.e., that bubbles are contaminated and thus mass transfer is hindered due to the 349 350 impurity molecules (e.g., surfactants) adsorbed at the bubble surface. The k₁ coefficients measured
- 351 are thus always between these two asymptotic and ideal cases (Xu et al. 2018).
- 2.2.5 Volumetric bubble interfacial area a 353
- The interfacial area of spherical bubbles is given by (Eq. 29): 354

$$a = \frac{6}{d_B} \varepsilon_g \tag{Eq. 29}$$

where a is the bubble's interfacial area (m^2/m^3), d_B the bubble's diameter (m), and ϵ_g the gas hold-up (-).

357 If the bubbles are ellipsoidal, a correction factor that includes bubble eccentricity K (the ratio of major axis to minor axis) is taken into account (Cockx et al. 1997, Colombet et al. 2011):

$$a = \frac{6}{d_B} \, \varepsilon_g \, f(K) \tag{Eq. 30}$$

$$f(K) = \frac{1}{2K^{1/3}} * (K + \frac{\ln(K + \sqrt{K^2 - 1})}{\sqrt{K^2 - 1}})$$
 (Eq. 31)

Ellipsoidal bubbles have a higher interfacial area than spherical ones, thus f(K) is always higher than

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2.2.6 Numerical method, boundary and initial conditions.

First, the 1D steady state model runs using Matlab® for a fully developed bubbly flow (equations 5 to 20 with the algebraic solver function fsolve) in order to obtain axial profiles of the gas fraction, the gas velocity, the pressure and the bubble diameter along the column height (50 layers along z) as a function of the input parameters (inlet bubble diameter, gas flow rate, column height). Then, mass transfer between the gas and the liquid phase are calculated from hydrodynamics results with a transient solver (ode23t function for equations 21 to 24 with closure relations 25 to 31). This one-way coupling hydrodynamics and mass transfer is only valid with the assumptions that the mass transfer does not modify hydrodynamic parameters (i.e. similar molar flow rates in the gas phase). For all the simulations presented hereafter, the initial molar fraction of oxygen in the gas was set to the inlet atmospheric condition at the bottom of the column (xg(z) = 0.21) for all discretization layers along column height, physically corresponding to the fact that fresh air is continuously supplied in the column from the bottom, so that the oxygen molar concentration in the gas at the inlet does not vary. The initial dissolved concentration in the liquid phase was considered as an initial condition: depending on the simulated experiments, its value was set to the initial experimental dissolved oxygen concentration (mostly equal to zero). Finally, the simulated length of time is also adjustable,

and it has to be long enough to allow the system to reach an equilibrium state, i.e. when the oxygen concentration in liquid is equal to the saturation value. The time to reach steady state conditions depends on the mass transfer from bubbles and on experimental conditions. For the bubble columns considered, the simulated time period lies between 500 and 20,000 s.

3. Results and discussion

3.1 Hydrodynamic characterization of the datasets studied

A pragmatic approach is applied to select the combinations of correlations and closure laws that make it possible to obtain a reliable description of the three experimental datasets with the 1-D model, in terms of global gas hold-up changes with the superficial gas velocity. The combinations of the closure laws considered are presented in Table 3.

Table 3. Selected combinations of closure laws for appropriated modelling of each datasets.

Dataset	Pressure effects on bubble size	Contamination effects regarding	Collective effects
	and gas superficial velocity	hydrodynamics (via the drag law	(via Eq. 16)
		considered)	
D1	Included	Contaminated (Tomiyama drag law)	Included
D2	Included	Contaminated (Tomiyama drag law)	Included
D3	Included	No contamination (Dijkhuizen drag law)	Included

The selected model structures include pressure and collective effects for all datasets. The drag law correlation of Tomiyama et al. (1998) is used for the datasets obtained with unfiltered tap water (D1 and D2), whereas the correlation proposed by Dijkhuizen et al. (2010) is used to simulate the hydrodynamics for the dataset obtained with filtered tap water (D3). For each dataset, the model including the closure laws presented in Table 3 is called the "base model" in the following.

Figure 3 presents the simulated and experimental gas hold-up as a function of the superficial gas velocity.

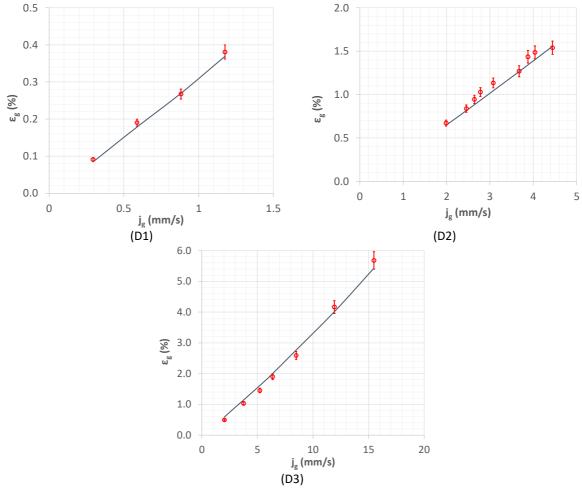


Figure 3. Global gas hold-up for different superficial gas velocities and for each dataset – Base models (O:

Good accuracy is obtained comparing simulated and experimental values (with an average difference between the experimental and simulated values of 4.6, 5.1 and 8.0 % for D1, D2 and D3 respectively). These results highlight that the 1-D model, considering appropriate closure laws, is relevant to model steady-state hydrodynamics of the bubble column along the vertical direction. The model is used in the following section in order to analyze the impact of selected closure laws and physics and to propose a deeper analysis of the different datasets on the basis of the effects considered (pressure, contamination effects and collective effects). The impact of the effects considered is analyzed per dataset by modifying the associated closure law in the model presented in Table 3.

3.1.1. Analysis of the pressure impact on hydrodynamics

Experimental data / —: Base model / Error bars: ± 5%)

The pressure effects on hydrodynamics is integrated into the model via bubble diameter (Eq. 19) and gas superficial velocity (Eq. 20), in order to take into account gas volume expansion (and associated bubble size) with variation in the local hydrostatic pressure. Since the mean bubble diameter varies with pressure following a cubic root law, the impact of pressure on this parameter is not as high as for gas superficial velocity.

Figure 4 presents the changes in the overall hold-up as a function of the superficial gas velocity for

the modified model (i.e. without considering the pressure effect on bubble size and superficial gas velocity along z), the base model (Table 3) and the experimental data for each dataset.

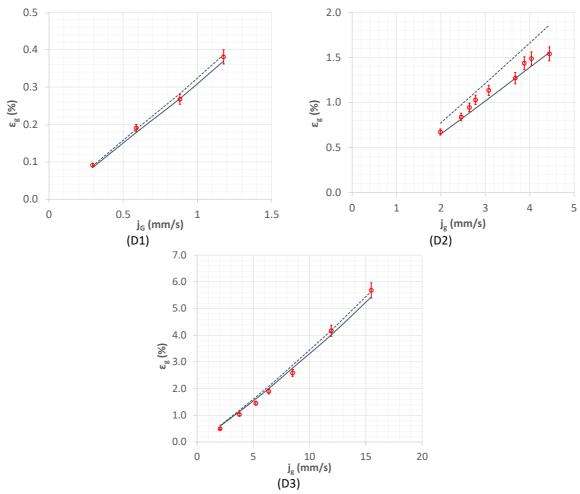


Figure 4. Overall gas hold-up for different superficial gas velocities and for each dataset. Impact of the pressure effects (O: Experimental data / ___: Base model (with pressure effects) /: :Modified model (without pressure effects) / Error bars: ± 5%)

As expected, the deviation due to the pressure effects is the most significant for dataset D2, because the water height is highest (4.5 m). The simulated gas hold-up is lower when the pressure effects are considered (28 % of the overall gas hold-up overestimation when the pressure impact is not accounted for), and experimental points are better described in that case. For datasets D1 and D3, since the water height is low (1.3 and 0.8 m, respectively), the simulation results are less affected. For deep bubble columns, the impact of hydrostatic pressure on the gas-liquid hydrodynamics (i.e. ϵ_g) along the column height are significant mainly due to its influence on gas superficial velocity (and to a lesser extent due to its influence on bubble size) and must be taken into account to appropriately model gas hold-up. For low soluble gases and a bubble size between 3 and 5 mm, the slip velocity is almost constant and the effect of local pressure on gas hold-up can be estimated considering a linear correlation, deduced from the ideal gas law:

$$\frac{\varepsilon_g}{\varepsilon_{a0}} = \frac{1}{2} \left(1 + \frac{P}{P_0} \right) \approx 1 - \frac{\rho_m g H}{2 P_0} \approx 1 - \frac{H}{20} \tag{Eq. 32}$$

Using Eq. 32, the reduction of the overall gas hold-up over the column height can be roughly estimated at 5% per meter (1/20).

3.1.2. Analysis of contamination effects on hydrodynamics

The impact of contamination effects is then analyzed via the drag law considered included in the model.

Since the bubbles are ellipsoidal, drag laws applied to the three datasets are focused on correlations depending on the Eötvös number (see Table 3). Since different water qualities could be considered in regards to experimental conditions (clean water [filtered water] for D3 and contaminated water [tap water] for D1 and D2), consistent drag correlations were selected to analyze their impact on hydrodynamics. As indicated in section 2.2.2.4, Dijkhuizen's drag correlation was selected for clean bubble surfaces, whereas Tomiyama's was considered for contaminated bubbles. Please note that the base model for D3 included Dijkuizen's drag law, whereas the base model for D1 and D2 included Tomiyama's drag law.

Figure 5 presents the overall hold-up as a function of the superficial gas velocity for models including Dijkhuizen's or Tomiyama's drag correlations and the experimental data for each dataset. The other closured laws considered in the respective models remain similar to Table 3.

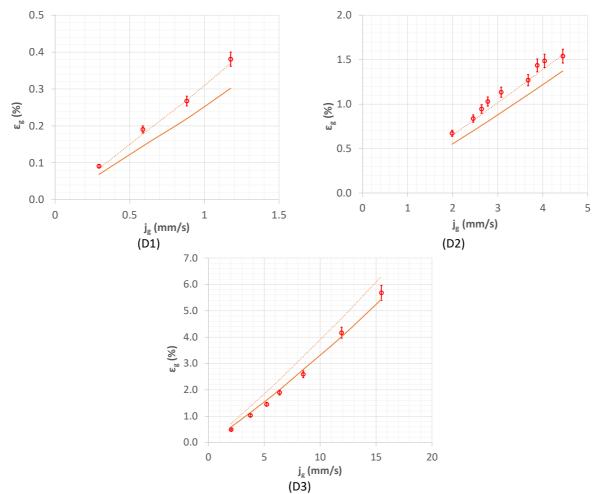


Figure 5. Overall gas hold-up for different superficial gas velocities and for each dataset (**O**: Experimental data / —: Dijkhuizen's drag correlation / ••••• : Tomiyama's drag correlation / Error bars: ± 5%)

The gas hold-up modeled was significantly impacted by the modification of the drag law considered, related to the contamination effects. The mean modeled values considering Tomiyama's drag correlation are from 15 to 22 % higher in comparison with modelled results obtained with Dijkhuizen's drag law, depending on the dataset considered and on the gas flow rate. The results obtained with the model that included Dijkhuizen's drag law fit the experimental points of dataset D3 better. This is a reasonable result related to the water quality of this dataset, which could be considered close to clear water (filtered water) and to the air diffuser (capillaries): the high air flow rate applied induces a lower contact time between nascent bubbles and liquid during bubble

formation along the capillary (Loubière et al. 2003). In the case of datasets D1 and D2, the experimental data are better described by the model integrating Tomiyama's drag correlation. This is in accordance with the water quality during these experiments (tap water). Considering hydrodynamics, the bubble surface for datasets D1 and D2 must be considered as contaminated, whereas it must be considered as clean for dataset D3. These results highlight that drag laws must be selected in accordance with actual operating conditions in order to consider bubble interface contamination by real water.

Due to the narrow gas hold-up range in the datasets selected, the deviation in the simulation hydrodynamics results related to the collective effects are less significant than for the effects discussed above. The mean deviation is lower than 5%, with the highest values observed for dataset D3 due to the wider range studied in terms of gas hold-up. From the model (using Eq. 16), we can estimate, by limited development of Eq. 12, that the gas fraction increase is around 2% of relative deviation per percentage of gas hold-up. Therefore, the collective effect cannot be ignored for gas hold-up from 3% (deviation greater than 6%, the data are given in supplementary material – Figure S1).

471 3.2 Mass transfer results

The simulated time variation of the dissolved oxygen concentration in liquid $C_I(t)$ allows one to calculate an overall K_La coefficient for the entire bubble column (Cockx et al. 2001) through the following classical equation:

$$C_l(t) = C_l^* - (C_l^* - C_{l0}) e^{-K_L a \cdot t}$$
 (Eq. 33)

where C_{10} is the dissolved oxygen concentration at t=0 (mg/L) and K_L a is the overall mass transfer coefficient (h⁻¹). For example, the experimental dissolved oxygen over time obtained by Duran et al. (2016) was compared with simulated dissolved oxygen (cf. supplementary materials – Figure S2). K_L a is also called the apparent mass transfer coefficient, since it assumes a constant equilibrium oxygen concentration C_1^* , although it actually varies with the oxygen concentration in gas during

reoxygenation (see Eq.22). Furthermore, the K_La coefficient is considered as a whole, with no distinction between K_L and a. This overall apparent K_La coefficient differs from the local k_La coefficient, which results from the multiplication of the local liquid-side mass transfer coefficient k_L (for example modeled with the Higbie penetration model) and the local interfacial area a. This local k_La coefficient varies locally essentially with z in a bubble column and can be averaged in the whole liquid volume. Moreover, it is quite difficult to determine experimentally k_L and a separately in a real bubble column (Colombet et al. 2011, 2015).

In the following section, global K_La values determined experimentally are compared with simulated global K_La coefficients with the Higbie and Frössling models for k_L , in order to see which transfer model fits the experimental points better when contamination of the bubbles is not fully controlled (real water).

- 3.2.1 Comparison of the Higbie and Frössling transfer models
- Figure 6 presents the overall K_La versus the superficial gas velocity for the three experimental datasets and associated modelling results.

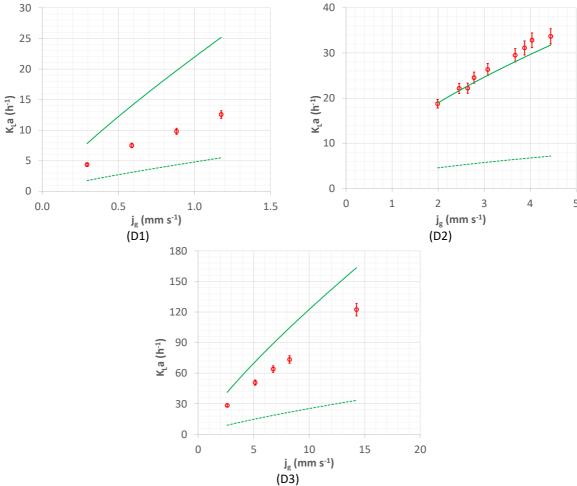


Figure 6. Overall *K*_L*a* transfer coefficients for different superficial gas velocities and for datasets D1−D3 (O: Experimental data /—: Modelled global K_La with Higbie model / —: Modelled global K_La with the Frössling model / Error bars: ±5%)

For dataset D3, the mass transfer is closer to the Higbie model (clean bubble surface) than to the

Frössling model (contaminated bubble surface). From the 1-D transient simulation, it can be deduced that the transfer interface is slightly contaminated (bubble size between 2.3 and 3.4 mm) even if the hydrodynamic simulation results show that filtered water does not reduce the bubble velocity (apparent clean interface for the drag force).

For dataset D2, the water quality is lower (tap water) and consequently induces contamination of the bubble surface, affecting the drag coefficient, which is confirmed by the hydrodynamics results (see section 3.1.2). However, Figure 6 highlights that the overall mass transfer is not really impacted because the transfer simulation shows that the non-contaminated Higbie model (clean bubbles)

works better than the Frössling model (fully contaminated bubbles). This apparent contradiction can be explained by the fact that for dataset D2, the bubbles are larger and ellipsoidal, between 3 and 4 mm. In this case, the contaminants at the bubble interface are transported to the rear of the bubble where local mass transfer is drastically lower than at the front where interface renewal is greater (Dani et al. 2007, Figueroa and Legendre 2010). For this reason, the bubble slip velocity could be reduced for large bubbles in tap water as observed in Figure 5, but not the mass transfer velocity (Figure 6). For dataset D1, experimental K_La values are much lower compared to D2 and D3 and seem slightly closer to the Frössling model. This can be related to the fact that bubbles in these experiments are significantly smaller and spherical (below 1.8 mm) and more likely to be contaminated, with a more rigid and less renewable bubble interface. In this case, the slip velocity behaves like a completely contaminated bubble and the mass transfer velocity is clearly lower than for larger bubbles also with tap water (as observed for dataset D2). These results confirm that when tap water is used, the Higbie transfer model is the most accurate for large bubbles (dataset D2, bubble size, 3.0-4.0 mm) and less relevant for small ones (dataset D1, bubble size, 1.5–1.8 mm), with significant contamination effects. For filtered water, the Higbie model is also the most suitable, although the presence of small contaminants could have slightly reduced the mass transfer velocity for intermediate bubble size (2.3–3.4 mm) because the water could not be considered as really pure (Colombet et al. 2015) except when rigorous experimental conditions are maintained with ultra-pure water. A complementary discussion on transfer contamination is detailed in section 3.2.3 after analysis of the depletion effect which can imply bias in transfer velocity

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estimation.

3.2.2 Comparison of mean local k_La and overall K_La: the oxygen depletion effect

In the previous discussion, the apparent $K_L a$ is compared to the simulation results with two asymptotic models for clean bubble interfaces (Higbie model) and fully contaminated ones (Frössling

model). During this comparison, the pressure effect on the gas fraction, the bubble diameter and the oxygen saturation was modeled to take into account all the relevant physical phenomena that modify hydrodynamic and mass transfer parameters. With the "base model" (Table 3), it is also possible to clarify the effect of pressure and height on the mass transfer. In Figure 8, experimental overall K_La values are compared to both simulated overall K_La coefficients and to mean local values (spatial average $\langle k_La \rangle$) calculated using the Higbie transfer model for simplicity.

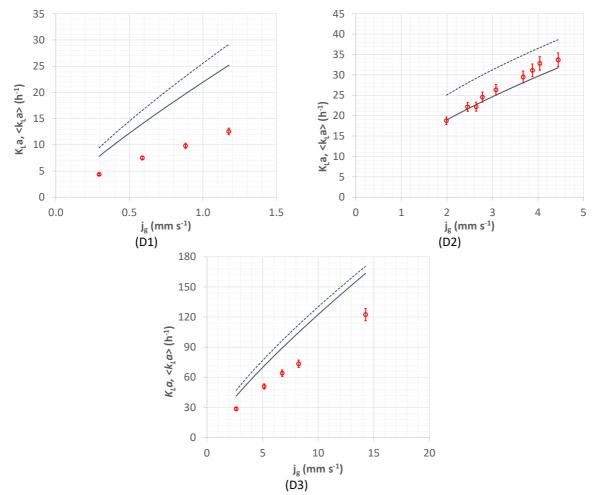


Figure 7. Experimental and modeled overall $K_L a$ and mean local $<\!k_L a>$ for different superficial gas velocities and for datasets D1–D3 (O: Experimental global $K_L a$ / : Simulated global $K_L a$ with the Higbie model / ::: Simulated spatial average $<\!k_L a>$ with the Higbie model / Error bars: $\pm 5\%$)

The simulated global K_La coefficients are systematically lower than the simulated mean local $< k_La>$ coefficients, the difference stemming from the oxygen depletion in the gas (due to the column height) and thus a decrease of the equilibrium concentration C_I^* (Eq.24). Simulated global K_La

coefficients describe the experimental points more accurately since this parameter is deduced from reoxygenation curves versus time as for the experimental data, especially for dataset D2. Indeed, oxygen depletion in the gas is significant due to the high column height (4.5 m of water). For the other datasets, given the high superficial gas velocity and the low column height in the case of D3 (0.76 m), the difference between mean local and global $K_L a$ is the least significant. Surprisingly for dataset D1, since the column height is relatively low (1.3 m) and the superficial gas velocity is very low, the difference between the two $K_L a$ coefficients modeled is also relatively substantial (mean difference, 55%)

To understand and model this depletion effect in the gas, a simplified analysis is proposed in the following section.

3.2.3. When mean local $< k_L a >$ differs from overall $K_L a :$ modeling the depletion effect

The following development aims at explaining more deeply the effect of superficial gas velocity, column height and other process parameters on oxygen depletion. Compared to the mass transfer time $(1/K_La)$, the bubble convection time or residence times (H/U_g) are smaller. The convection time and mass transfer time values are provided in the supplementary materials for the three datasets (Table S1).

Moreover, oxygen depletion in the gas occurs essentially at the beginning of the reoxygenation process, during a transient period (t << $1/K_La$) when the oxygen concentration in the liquid $C_l(t)$ is close to 0 mg/L. During this transient period, Eq. 23 becomes:

$$\nabla \, \varepsilon_g C_g(z) U_g = \, -k_L a(C_l^*(z) - 0) \tag{Eq. 34}$$

It appears that the depletion in the gas is given by the mass transferred. By estimating the oxygen saturation with the Henry' law (Eq. 22) and the interfacial area (Eq. 29), with the exchange coefficient m (Talvy, 2007), Eq. 34 becomes:

$$\nabla \, \varepsilon_g C_g(z) U_g = \, -k_L \frac{6. \, \varepsilon_g}{d_B}. \, m. \, C_g(z) \tag{Eq. 35}$$

564 with $m = He_{02}.RT$.

Assuming that the gas velocity is kept constant along the height of the bubble column, the integration gives the following variation in the concentration along z:

$$\varepsilon_g C_g(z) = \varepsilon_{g0} C_{g0}. e^{-k_L \frac{6}{d_B}.m.\frac{z}{U_g}}$$
 (Eq. 36)

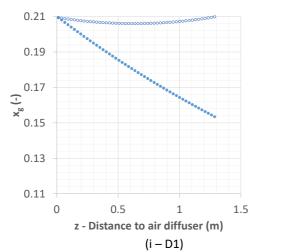
- The depletion in the gas (C_g/C_{g0}) decreases exponentially with (i) the mass transfer velocity k_L , (ii) the solubility m (iii) the distance from the diffuser z, and (iv) the inverse of bubble size and the associated slip velocity.
- In this equation, $\varepsilon_g C_g$ is the mass of soluble gas per unit of volume (m_g) by introducing a depletion factor (DF) for the whole column as:

$$DF = k_L \frac{6}{d_B} \cdot m \cdot \frac{H}{U_g}$$
 (Eq. 38)

It is possible to estimate the decreasing ratio of mass in the gas along the height the bubble column using Eq. 39:

$$\frac{\mathrm{m}_g}{\mathrm{m}_{a0}} = \frac{\varepsilon_g C_g}{\varepsilon_{a0} C_{a0}} = e^{-DF \cdot \frac{Z}{H}} \tag{Eq. 39}$$

For example, the depletion factor for D1 and D2 are close to 0.3 and 0.4, respectively, which corresponds to depletion loss in the gas of 26% and 33 % using Eq. 38 at the top of the bubble column. For dataset D3, the depletion factor is close to 0.05 and the decrease in the oxygen molar fraction in the gas is lower than 5%. In our study, as the solubility is constant and the mass transfer velocity k_L is quite constant for millimetric bubbles for oxygen, the substantial variation in the depletion factor is mainly related to the length ratio H/d_b , which is about 800, 1200 and 200 for datasets D1,D2 and D3, respectively. To illustrate the accuracy of the depletion model (Eq. 39), Figure 10 presents the oxygen molar fraction in the gas as a function of the distance from the diffusers at the initial time (t=0) and in the stationary state (t>>1/ K_La) for D1 and D2 when the depletion effect is significant (Figure 7).



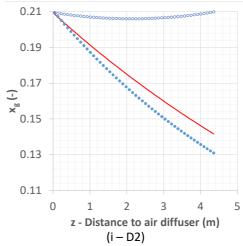


Figure 10. x_g as a function of z (distance from the diffuser) − Modelled for C_I = 0 mg/L (•) / Depletion law for C_I

= 0 mg/L (—__)/ Modelled (\bigcirc) for Cl = Cl* - jg = 1.2 and 4.4 mm/s for D1 and D2 respectively

The oxygen depletion estimated with the relation (Eq. 39) is in good accordance with the comprehensive 1D model. The depletion factor (Eq. 38) can then be used to identify the experimental conditions inducing a significant impact of the gas depletion effects on the global mass transfer coefficient $K_L a$.

This depletion effect is clearly increased by (i) a long bubble residence time (H/U $_8$ =4.3 s and 18.3 s for D1 and D2, respectively), (ii) the high solubility of the gas considered passing into the liquid phase (here m = 0.0034 is relatively low for oxygen in water) and (iii) the low transfer time at the bubble scale (d_B/k_L =2.8 s and 9.4 s for D1 and D2, respectively).

In comparison with the relative simplicity of the estimation of the mean bubble residence time (H/U $_8$) in a bubble column, it is much more difficult to determine the bubble transfer time (d_B/k_L) precisely, which can vary along the column height due to substantial bubble size changes with increasing hydrostatic pressure. However, this bubble transfer time could be estimated through the inverse ratio of the global volumetric transfer coefficient to the global gas fraction ($K_L a/\epsilon_B$). This last parameter is also close to the transfer number N_T (Figure 2) but both approximations imply a certain

bias because all the nonlinearity effects on average values are ignored.

3.2.4 Mass transfer and bubble contamination angle

In this section, the level of bubble contamination is studied through their contamination angle, according to the theory developed by Sadhal and Johnson (1983). The level of bubble contamination is characterized through a contamination angle, corresponding to the contaminated interface occupied by the adsorbed contaminants at the bubble surface, expressed as the angle between the rear of the bubble and the limit of the contaminated surface. The contamination angle varies between 0° and 180°, depending on whether the bubble surface is completely clean or completely contaminated, respectively. For all experimental data, the experimental global K_La coefficients lie between the ideal K_La coefficients obtained with the Higbie and Frössling mass transfer models (Figure 6). The contamination angle is obtained from the dimensionless drag coefficient with the following correlation (Sadhal and Johnson 1983; Dani 2007):

$$C_D^*(\theta_{cap}) = \frac{1}{2\pi} (2\theta_{cap} + \sin(\theta_{cap}) - \sin(2\theta_{cap}) - \frac{1}{3}\sin(3\theta_{cap}))$$
 (Eq. 38)

with θ_{cap} the drag contamination stagnant cap angle (in radian).

On the other hand, the dimensionless drag coefficient $C_D^*(\theta_{cap})$ is related to the Sherwood numbers of the bubble (experimental), of a completely clean bubble (Higbie correlation) and of a completely contaminated bubble (Frössling correlation) as follows (Takemura and Yabe 1999, Dani 2007, Xu et al. 2018):

$$C_D^*(\theta_{cap}) = 1 - \left(1 - \frac{Sh - Sh_{Higbie}}{Sh_{Fr\ddot{o}ssling} - Sh_{Higbie}}\right)^2$$
 (Eq. 39)

with Sh the experimental Sherwood number, Sh_{Higbie} the Sherwood number of a completely clean bubble and Sh_{Frössling} the Sherwood number of a completely contaminated bubble.

The Sherwood number is defined as follows:

$$Sh = \frac{k_L * d_B}{D} \tag{Eq. 40}$$

with k_L the experimental mass transfer velocity estimated from the experimental reoxygenation curves using the 1-D model (via iterative calculation).

Table 4 presents the Sherwood numbers of the real bubbles calculated from the comprehensive model of a completely clean and a completely contaminated equivalent bubble. The transfer contamination angle is then deduced from Eq. 38 for datasets D1 and D3.

Table 4. Sherwood numbers and contamination angle and for the experimental dataset D1 and D3

Dataset	jg expressed at P _{atm} (mm/s)	d _b expressed at P _{atm} (× 10 ⁻³ m)	k _L (× 10 ⁻⁴ m/s)	Sh _{exp} (-)	Sh _{Higbie}	Sh _{Frössling}	Ө _{сар} (°)
D1	0.29	1.48	3.80	313	625	120	105
	0.59	1.69	3.47	286	568	109	105
	0.88	1.71	3.01	248	562	108	113
	1.18	1.83	3.00	247	536	103	110
D3	2.62	2.34	3.85	450	699	134	88
	5.14	2.58	3.65	471	716	138	86
	6.76	2.72	3.58	487	723	140	84
	8.23	2.84	3.42	486	729	141	85
	14.26	3.28	3.47	569	749	147	73

For each dataset, the contamination angles vary slightly with superficial gas velocity and the water quality appears to be specific for each dataset.

For dataset D1, the transfer contamination angle lies between 105 and 113°, which indicates a high level of bubble contamination that substantially reduces the mass transfer compared to an equivalent clean bubble (around 50%). This angle designation is consistent with the fact that the experimental hydrodynamics (i.e. ϵ_g) of dataset D1 was adequately reproduced using a drag coefficient set for contaminated bubbles (Figure 5).

For dataset D3, lower transfer contamination angle values were obtained in comparison with dataset D1. Even if the water is very clean (filtered tap water), the mass transfer is still hindered compared to a clean equivalent bubble (between 24 and 36%), but the decrease of the drag coefficient due to the water contamination remains negligible (Figure 5).

For dataset D2, since experimental global K_La values fit well with the Higbie model (see Figure 6), it can be deduced that bubbles have transfer contamination angles close to zero and are equivalent to completely clean bubbles. This means that the greater the bubble size, the less the drag contamination impact has an effect on mass transfer:1.5-, 2.5- and 3.5-mm bubbles correspond to 105°, 88° and 0° contamination angles, respectively. This means that when the bubble size increases, it becomes ellipsoidal and the mass transfer occurs intensively at the front of the bubble where the transfer contamination tends to become negligible (Dani et al., 2021).

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3.2.5 Discussion on mass transfer modeling

Hydrodynamic parameters calculated with the 1D model in steady state conditions (bubble diameters, gas hold-up and gas velocity) were validated and then used in order to calculate reoxygenation and global K₁a mass transfer coefficients. A distinction was made between mean local <kla> and apparent global Kla. The latter is calculated from simulated curves of dissolved oxygen concentration over time, and takes into account oxygen depletion in the gas phase and therefore the variation in the equilibrium concentration versus time. A comparison with the experimental data of global K_La therefore provides accurate results, especially for deep bubble columns and/or a low gas flowrate when oxygen depletion in the gas increases (Eq. 36). The depletion factor (Eq. 37) is adapted to characterize and interpret situations where the effects of oxygen depletion influence the gasliquid transfer due to gradient in the gas phase composition. Moreover, for the three experimental datasets, the Higbie and Frössling mass transfer models were used to interpret mass transfer results with no bias related to the quality of the liquid phase composition (Baeten et al. 2020). When tap water was used for experiments (D1 and D2), the smaller the bubbles, the more they were contaminated. Consequently, the global mass transfer coefficient could be drastically reduced (up to 50% by model comparison with clean bubbles with dataset D1). Surprisingly, even if contamination reduces the slip velocity in dataset D2, mass transfer is not affected by the contamination because the bubbles are big enough to be ellipsoidal: in this case the

transfer occurs mainly at the front of the bubble interface (Dani et al. 2006). For dataset D3 obtained using filtered water, the mean slip velocity of bubbles corresponds to that obtained for pure water. However, for this relatively clean water, the bubble surface was still characterized as partially contaminated (contamination angle estimated at 100°).

In the context of oxygen transfer in aeration processes, it is then possible to ignore the effect of contamination with tap water for ellipsoidal bubbles greater than 3 mm (as for dataset D2). However, for small bubble sizes (under 2 mm), the quality of the tap water can drastically reduce the mass transfer (more than 50% compared to clean bubbles). In both situations, depletion effects are substantial in deep bubble columns but must also be taken into account for relatively low column height and specific studies (low mean bubble size or high solubility of the component studied).

In addition, the impact of eccentricity on the modeled mass transfer coefficient is given in supplementary information (Figure S3). For datasets D2 and D3, the mean local <kia> values modeled are slightly higher when eccentricity is taken into account. To remain physically consistent, eccentricity must be systematically considered to calculate the interfacial area of ellipsoïdal bubbles.

4. Conclusions

The main conclusions of this study are:

The proposed 1-D model is able to reproduce experimental hydrodynamic (global gas hold-up) for three different experimental datasets in bubble columns with an air/clear water system. The closure laws considered must be rigorously selected in order to integrate the impact of contamination, collective and pressure effects on hydrodynamics, and the mass transfer parameters. Depending on the experimental water height, hydrostatic pressure influences on the hydrodynamic parameters plays a major role and must be considered in the model (an appromimately 5% decrease on gas hold-up per meter of depth). The importance of the drag law choice is also highlighted, depending on the water quality and its influence on bubble contamination.

- The gas oxygen concentration significantly depletes due to the transfer to liquid and thus the equilibrium concentration varies, which explains the difference between the mean local <k_La> and global K_La coefficients. This difference becomes substantial for high soluble gas with high transfer rate and/or a high bubble column and/or low mean bubble size d_b. A depletion factor is proposed in order to warn of situations in which the experimental determination of the overall mass transfer coefficient must be conducted rigorously by considering this depletion effect through an estimation from the reoxygenation curves. The substantial impact of the depletion in the gas phase composition is drastically increasing with the length ratio H/d_b.
- The suitability of the Higbie k_L model for clean water transfer modelling is demonstrated, especially for ellipsoidal bubbles over 3 mm in full-scale aeration processes. For smaller bubbles or millimetric bubbles, mass transfer is more sensitive to water contamination and water quality remains the most important factor.
- The impact of water quality on oxygen transfer can be estimated by the contamination angle using comprehensive 1D modeling as developed in this study. This will make it possible to provide a more in-depth understanding of the impact of water quality and the main operating parameters on mass transfer in industrial tanks where the liquid phase is a complex matrix.

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Hydrodynamic calculation Input data (steady state/input for mass transfer) ■ Physico-chemical parameters Gas hold-up ϵ_{G} □ Column height Slip velocity/gas velocity Gas superficial velocity j_{G} Hydrostatic pressure Bubble diameter d_B Bubble diameter variation N layers Mass transfer (dynamic) \Box $C_L = f(t)$ (perfectly mixed liquid) \Box $C_G = f(t)$ for each height z