

Spatialization of saturated hydraulic conductivity using the Bayesian Maximum Entropy method: Application to wastewater infiltration areas

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- 1 Title: Vertical 2D spatialization of saturated hydraulic conductivity by integrating ERT and infiltration
- 2 test into a Bayesian Maximum Entropy data fusion method: Application to wastewater infiltration
- 3 area
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13 Abstract:

14 Wastewater treatment, a major issue at the European level, focuses on improving surface and groundwater quality, preserving the receiving environment and ensuring a sustainable use of water. 15 Soil infiltration is increasingly practiced downstream of wastewater treatment plants, particularly in 16 17 rural areas without surface water bodies, as is the use of soil as an additional buffer and treatment 18 step. However, the design of infiltration areas on heterogeneous soils remains an extremely complex task due to the costly and time-consuming spatial measurement of saturated hydraulic conductivity 19 20 (Ks). This article proposes integrating 2D electrical resistivity tomography and infiltration tests into a 21 Bayesian Maximum Entropy method, yielding a vertical mapping of soil heterogeneities at a metric 22 scale. This updated method will facilitate infiltration area design in a heterogeneous soil setting.

23 Keywords:

24 Wastewater treatment plant, design, Bayesian Maximum Entropy, saturated hydraulic conductivity,

25 electrical resistivity tomography, infiltration test.

1. Introduction

28 Despite the advances achieved in wastewater treatment plants over the last few decades, treated 29 wastewater (TWW) can still exert a strong impact on downstream receiving rivers (Aubertheau et al., 2017). This is especially true in French rural areas, where treatment plants are mainly dedicated to 30 treating carbonaceous pollution due to their small capacities (< 1,000 population equivalent, 31 32 (MEDDE, 2015)). Consequently, the application of an extensive process like soil infiltration has become increasingly practiced as an option to provide tertiary treatment; it consists of TWW 33 discharge over a large surface area (trenches, ponds, basins or meadows), allowing for gradual 34 infiltration through the soil. The pollutants (nitrogen and phosphorus) are naturally treated by 35 36 biodegradation processes or retained in the soil. The design and management of a TWW infiltration 37 area is mainly based on an estimation of the soil saturated hydraulic conductivity (Ks) in order to calculate the discharge capacity and evaluate its treatment potential (Siegrist, 2014). However, Ks 38 remains one of the most difficult soil properties to determine (Mahapatra et al., 2020) and its spatial 39 40 variability can significantly influence TWW infiltration (Zhang et al., 2019). Infiltration tests are usually carried out using the Porchet constant head method, which outputs direct and local 41 42 measurements of Ks and requires 1 to 4 hours per test depending on the soil type. For 43 heterogeneous soils, the estimation of Ks requires numerous measurements to establish confident predictions of TWW discharge (Warrick et al., 1977); this protocol can prove to be invasive and time-44 45 consuming. Nevertheless, an incorrect estimations of Ks could lead to malfunctions in the TWW 46 infiltration areas via: i) premature clogging (McKinley and Siegrist, 2011), ii) over-infiltration and groundwater contamination, and iii) under-infiltration leading to puddling and olfactory nuisances 47 (Morugán-Coronado et al., 2011). 48

For the estimation of Ks variability, Bisone *et al.* (2017) proposed using geophysical methods on TWW infiltration areas with a subjective delineation of heterogeneity in order to locate a few infiltration tests for an optimal design. Geophysical methods allow visualizing soil structures through the measurement of a given physical parameter (wave speed, electrical resistivity (ER), elasticity) (Romero-Ruiz *et al.*, 2018). Such methods are non-intrusive and yield physical information on large soil volumes yet still involve significant uncertainties (Loke *et al.*, 2013). In the environmental sciences for near-surface (0-2 m) investigations, electrical resistivity tomography (ERT) is a widely used method whenever 2D vertical information is required (Hellman *et al.*, 2017).

The ER signal is a function of a number of soil properties, including: the nature of solid constituents (particle size and distribution), the arrangement of voids (porosity, pore size distribution, connectivity), water content, the ER of the fluid, and the temperature (Samouëlian *et al.*, 2005; Telford *et al.*, 1990). On the other hand, the ER signal has no direct dependence on Ks (Attwa and Ali, 2018; Weller and Slater, 2019); their physical relationship tends to be specific to the given soil type and is difficult to transpose directly to heterogeneous soils (Doussan and Ruy, 2009).

Only a few articles have explored the notion of using ERT to determine soil Ks with ER. Two approaches were found to be extremely attractive: the first employs empirical relationships between ER and Ks (Vogelgesang *et al.*, 2020), while the second adds a hydrodynamic model constrained by geophysics during the inversion process (Farzamian *et al.*, 2015). The former is a simple method yet still generates a high level of Ks estimation uncertainty, whereas the latter is probably the most robust method but requires an extensive numerical approach and tends not to be well adapted to TWW infiltration area design.

The 2D estimation of Ks from geophysical measurements and point measurements necessitates the use of other emerging methods for simple and robust applications, e.g. data fusion methods (Dezert *et al.*, 2019; Li *et al.*, 2019). Data fusion refers to the process of integrating multiple data sources in order to produce more accurate and useful information. Until now, no paper has yet to be published regarding data fusion between ERT and Ks.

Among all data fusion methods, Bayesian Maximum Entropy (BME) seems to be the best adapted in considering the datasets: ERT data (dense with high uncertainty, hard data), and infiltration data (reliable but sparse, soft data) (Christakos *et al.*, 2002). BME is a nonlinear spatial estimator that rigorously accounts for spatial variability and the non-Gaussian characteristic of uncertain data (here, uncertainty is represented by a variance). Christakos *et al.* (2002) showed that BME is a relevant method for predicting spatial data encompassing several environmental parameters. For instance, it has been successfully used to predict water table variations (D'Or *et al.*, 2001) and estimate soil salinity (Douaik *et al.*, 2005). These examples suggest that the BME method is suitable to estimate 2D-Ks maps. The aim of this paper is to merge Ks and ERT measurements in order to obtain the most accurate estimation of Ks, thus providing new TWW infiltration area design elements.

- 85 **2.**
- 86

2. Materials and methods

2.1. General methodology

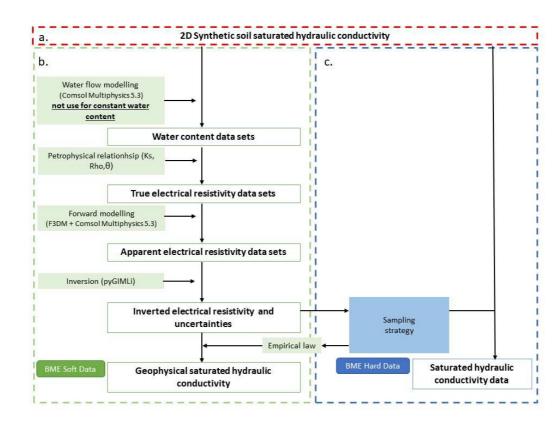
The methodology adopted herein to evaluate the benefit of BME is based on a classical approach widely used in the geophysical literature (Radulescu *et al.*, 2007); it is composed of three steps:

- The first step consists of constructing synthetic datasets based on three synthetic Ks reference 90 models (Ks_{ref}), and then simulating the ERT measurements and infiltration tests for each 91 model.
- The second step adapts, evaluates and determines the BME method limits by means of the numerical datasets created in the previous step, through:
- 94 o Defining the optimal number of hard data points (14, 24 or 50) for a homogeneous
 95 Water Content (WC) of 0.25-m³.m⁻³;
- 96 Validating a robust sampling strategy of hard data;
- 97 Assessing the impact of soil moisture variation in the model.
- The third step validates the BME method on a field dataset.
- 99 2.2. Datasets
- 100 2.2.1 Synthetic datasets

101 The synthetic datasets generated from Ks_{ref} (Figure 1a) are organized into both hard and soft data.

102 Soft data generation consists of simulating the geophysical measurement and deriving hydraulic

103 conductivity, denoted Ks_{Geo}, from ERT (Figure 1b). Hard data, on the other hand, are local estimations of Ks sampled directly from Ks_{ref}; these data correspond to a simulation of the 104 infiltration tests (Figure 1c). As for Ks_{Geo}, the first step entails simulating soil WC based on 105 groundwater flow modeling, which will provide a realistic soil WC data distribution (Section 106 2.2.1.2.1). In taking WC and soil type into account, petrophysical relationships drawn from the 107 literature will be used to calculate true electrical resistivity ER_{True} (Section 2.2.1.2.2) and simulate 108 apparent electrical resistivity (ER_{App}) for each Ks model (Section 2.2.1.2.3.1); next, we will invert 109 ER_{App} data to obtain interpreted electrical resistivity (ER_{Interp}) (Section 2.2.1.2.3.2). Lastly, ER_{Interp} 110 111 data will be transformed into Ks_{Geo} data (Section 2.2.1.3).



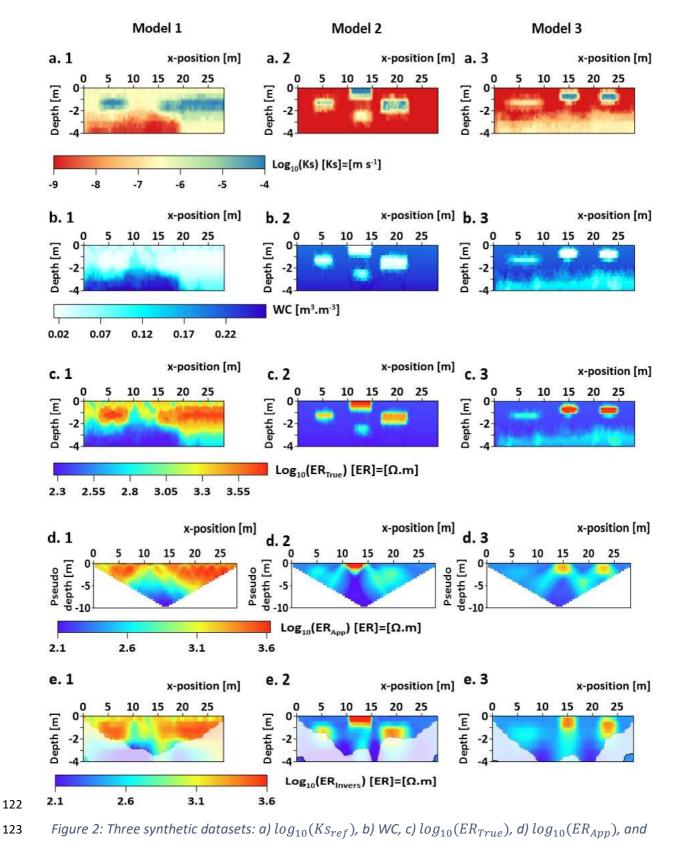
112

113 Figure 1: Schematic diagram for generating synthetic datasets. In green: soft data represent spatial

114 geophysical measurements; in blue: hard data correspond to infiltration tests (Ks measurement).

115 2.2.1.1. Ks reference models

Figure 2a presents three different Ks_{ref} . We have chosen to show Ks_{ref} anomalies with a metric horizontal extension. In the BME framework, all data are introduced in log₁₀ for purposes of 118 computation. The 3 models of $\log_{10}(Ks_{ref})$ have been grouped in Figure 2a. These three models 119 have been chosen based on various criteria. The first model is a field case presented in an article 120 (Bisone *et al.*, 2017a) devoted to a study of an infiltration site. The two other geological 121 configurations are known to be difficult to reconstruct using ERT (Telford *et al.*, 1990).





e) $log_{10}(ER_{Interp})$

2.2.1.2. Soft data generation

126 2.2.1.2.1. Subsurface flow modeling: Water content estimation According to Figure 1b, the first soft data generation step calls for WC simulation using subsurface 127 flow modeling for variably-saturated soils. As suggested in Audebert et al. (2016), we will employ a 128 single continuum model based on Richard's Equation (Richards, 1931), as completed with Mualem-129 130 van Genuchten's retention model, which expresses the relationship between water pressure and effective saturation (retention properties) as well as between relative Ks and effective saturation. To 131 simulate TWW subsurface flow, we ran Comsol Multiphysics 5.4 with a subsurface flow module. The 132 133 study domain is a 2D vertical profile 29.2 m long and 6 m high. The water flow boundary conditions were set as follows: (i) "No flow" on the top and sides; and (ii) "seepage face" for the bottom, as in 134 135 Audebert et al. (2016). To assign all hydraulic parameters, we extracted from the literature 12 soil 136 types with known parameters. Considering $log_{10}(Ks_{ref})$, for each cell in Table 1, we sought the Ks corresponding to the closest Ks_{ref} value and assigned the remaining hydraulic parameters (Θ s, α 137 138 and n).

-	-					
	Mualem-van Genuchten hydraulic					
	ра	rameters				
Textural class	ural class Θs α n <i>l</i>					
	[L ³ .L ⁻³]	[m ⁻¹]	[-]	[Ks]=[m.s ⁻¹]		
Coarse sand	0.33	7.44	2.96	-3.48		
Sand	0.43	14.5	2.68	-6.08		
Loamy Sand	0.41	12.4	2.28	-6.39		
Sandy Loam	0.41	7.5	1.89	-6.91		
Loam	0.43	3.6	1.56	-7.47		
Silt	0.46	1.6	1.37	-8.16		

0.45

0.43

0.41

0.43

0.38

0.36

0.38

-7.90

-6.08

-8.14

-8.71

-8.48

-9.26

-8.26

1.41

2.68

1.31

1.23

1.23

1.09

1.09

2 14.5

1.9

1

2.71

0.5

0.8

 Table 1: Mualem - van Genuchten parameters and saturated hydraulic conductivity (Ks)
 of soil derived from Rosetta (Schaap et al., 2001)

142

Silty Loam

Sandy Clay Loam

Clay Loam

Silty Clay Loam

Sandy Clay

Silty Clay

Clay

140

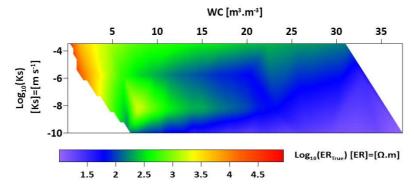
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To simulate variably-saturated soil, the model was initiated with a saturation set to 1. During a requisite time interval, the model was left to simulate soil drainage until the water table was close to 4 m deep. This value was chosen so that the given configuration could be considered free of any water table influence on the infiltration test within the first 2 m of soil. This set-up produced variable 2D-WC maps; for the constant WC model, we simply chose a value of 0.25 m³.m⁻³.

148

2.2.1.2.2. Petrophysical relationship

Just a few articles in the literature include the petrophysical relationship in determining Ks with the 149 150 true electrical resistivity of soil (ER_{True}) (Vogelgesang et al., 2020). Soil WC can be considered as the 151 most influential parameter on ER_{True}; it is necessary therefore to take the variability of WC and Ks 152 into account in the relationship. According to the literature, potential physical relationships between ER and WC are specific to a given soil type (Brunet et al., 2010). For this study, we extracted the (WC, 153 ER) pairs measured in the laboratory for broad sandy, loamy and clayey soil textures (Wunderlich et 154 al., 2013) and associated a $log_{10}(Ks)$ value with each relationship (Mallants et al., 2003). A 2D 155 156 interpolated map of ER_{True} was estimated as a function of Ks and WC (Figure 3). Based on both the WC model and $log_{10}(Ks)$ reference model, for each cell estimating $log_{10}(ER)$, the closest WC and $log_{10}(Ks)$ values were sought (Figure 2c).



159 160

Figure 3: Results of the interpolation of $log_{10}(ER_{True})$ vs. WC and $log_{10}(Ks)$

161

2.2.1.2.3. Electrical resistivity tomography

The ERT measurement has been well described in the geophysical literature (Clement *et al.*, 2020). ER_{App} is measured by injecting electric current into the ground with two current electrodes, in measuring the potential difference between two other electrodes; this device is called a quadrupole. The distribution of ER in the soil is determined by operating many quadrupoles at various positions along a line of electrodes installed at the surface of the soil. At the end of the measurement sequence, all quadrupoles are inverted using an inversion code (Telford *et al.*, 1990).

168

2.2.1.2.3.1. Forward modeling

169 To simulate ER_{App} on each of the three synthetic ER models (Figure 2c), we ran the Comsol Multiphysics and Matlab F3DM 3.08 package, which is commonly used in geophysics forward 170 modeling with the AC/DC module (quasi-stationary electromagnetic field in accordance with 171 172 electromagnetic field theory) to evaluate the potential difference induced by the injected current 173 (Clement and Moreau, 2016). A Gaussian noise distribution with a 3% standard deviation relative error was added to the ER_{App} dataset to simulate the noise commonly recorded in the field (Friedel, 174 175 2003). An acquisition line of 72 electrodes was implemented at a 0.4-m spacing. A complete sequence of 829 quadrupoles was carried out with Wenner Arrays. 176

2.2.1.2.3.2. Inversion procedure

The synthetic ER_{App} was inverted using pyGIMLi, an open-source multi-method library for geophysics modeling and inversion (Rücker *et al.*, 2017). A finite element method, relying on regular grid models, was applied to solve the forward problem in the routine inversion program. An isotropic smoothness-constrained regularization and a quasi-Gauss Newton optimization method were both used along with a fixed regularization parameter (λ = 30, Zweight = 1.0). This inversion procedure produced an ER_{Interp} map (Günther and Rücker, 2011).

184

2.2.1.2.3.3. Uncertainties

An interpreted ERT is not the perfect image of ER_{True} . The smooth nature of electrical current implies a loss of resolution when moving away from the electrodes. In some parts of the inverted model, the ER value of a cell has a very low impact on the measured ER_{App} . It is therefore of paramount importance to account for the uncertainty on ERT.

The total uncertainty of ER depends on: the inversion process, the measured data, and the loss of information with depth. Calculating total uncertainty is a long and complex process; consequently, it is proposed herein to estimate uncertainty by means of simple inversion indicators derived from the geophysical literature, namely: coverage, resolution radius (Friedel, 2003), or DOI (D. Carrière *et al.*, 2014). All inversion indicator calculations require knowledge of the Fréchet derivative matrix G[N×M], also called the Jacobian matrix or sensitivity matrix (Equation 1):

$$G_{i,j} = \frac{\partial d_i}{\partial m_j} \quad i = [1:N], j = [1:M]$$
 Equation 1

where d_i and m_j are the ER_{App} data and model parameter, respectively. A single sensitivity value G_{i,j} indicates the change in apparent resistivity data d_i m with respect to a small change in model parameter m_j . G is used to determine how a change in resistivity of model cell j affects the measured value of d_i . In our case, we have opted for model resolution R_M , where the R_M matrix is calculated by inversion software according to the following formula (Equation 2) (Günther, 2004):

$$R_{M} = (G^{T}W_{d}^{T}W_{d}G + \lambda C^{T}C)^{-1}G^{T}W_{d}^{T}W_{d}G \qquad Equation 2$$

200 where G is the sensitivity matrix, W_d a diagonal matrix containing the data errors, λ the damping parameter, and C the a priori model covariance matrix. The diagonal element $R_{\rm ii}$ indicates how the 201 inverted model of ER is resolved. If all diagonal elements of R_M equal 1, then the "exact model" is 202 perfectly resolved. The further the R_M diagonal element from 1, the poorer the resolution. In 203 accordance with the ideas of (Friedel, 2003), a resolution radius for each model cell can be 204 determined from the diagonal elements of the resolution matrix R_{ii}. Let's assume a piecewise 205 constant cell resolution with rⁱ_{les} as the radius of a cell circle having a perfect resolution of 1. For a 206 207 cell of dimensions Δx_i and $I\Delta z_i$, the resolution radius is defined by Equation 3 below:

$$r_{Res}^{i} = \sqrt{\frac{\Delta x_{i} \Delta z_{i}}{\pi R_{ii}}}$$

Equation 3

The resolution matrix r_{Res} allows assessing the reliability of the inverted models according to the degree of resolution specific to each cell. r_{Res} is therefore the most suitable indicator for unstructured or irregular BERT meshes. For this reason, r_{Res} has been chosen as an uncertainty to be introduced into the BME (Section 2.3).

212 2.2.1.3. Hard data generation: Hydraulic conductivity sampling method

We have sampled hard data $log_{10}(Ks_H)$ by extracting the $log_{10}(Ks)$ value from $log_{10}(Ks_{ref})$ (Figure 2a). It is assumed that our measurements of $log_{10}(Ks_H)$ have a zero variance. We used ER_{Interp} data and a random selection technique to optimize the Ks sample location, as per the following strategy:

• 50% of the number of points were manually sampled above and below the anomalies.

- 25% of the points were sampled in the upper part of the ER_{Interp} map, where R_{res} has low
 uncertainty. Our ER_{Interp} maps were divided into three ranges, between the min and max
 values. In each range, an equivalent number of points were randomly sampled.
- 25% were sampled in the area with the lowest r_{Res}; these points were sampled entirely
 randomly, owing to the poor performance of ERT in this area.

For this step, the spatialization of Ks with the BME has been tested with three differing sample numbers, i.e. 14, 24 and 50.

225 2.2.2. Field data

The experimental site is located in France and had already been studied in previous articles (Benz-226 227 Navarrete et al., 2019). It comprises a fairly heterogeneous agricultural plot and is relatively tabular in its sandy-loam surface, presenting sandy lenses in loam over its depth. ERT acquisitions were 228 229 carried out using Iris Instruments' "Syscal Pro 72-electrodes" resistivity-meter (IRIS Instruments, 230 France). The ERT profile was acquired with a Wenner array-type and a 0.25-m electrode spacing. To cover the proposed profile length (45 m) and maintain reasonable subsurface lateral resolution, the 231 roll-along acquisition technique was performed with 48 electrode overlaps. The contact resistance 232 was continuously measured at less than 4 kOhms. The 2D image of the $ER_{Interp}\xspace$ profile was inverted 233 234 with the pyGIMLi software (Rücker et al., 2017); a 2D flat inversion was carried out. We chose an isotropic smoothness constraint, with a Z-weight of 1 and a lambda value of 30 (Günther, 2004; Loke, 235 1999). Moreover, we used a tetrahedral mesh with 2,920 cells. 236

According to the sampling strategy presented in the previous section, 23 infiltration test locations were selected. The Aardvark permeameter, developed by Soil Moisture Inc. (USA), was employed to measure the infiltration rate. From the measured flow rate, log₁₀(Ks) could be estimated by applying Reynolds and Elrick's equation (Elrick *et al.*, 1989).

241 2.3. BME fusion method

The Bayesian Maximum Entropy (BME) method and its BMElib numerical implementation (Christakos *et al.*, 2002; Serre and Christakos, 1999) provide a mathematically rigorous framework that incorporates information from several data sources featuring different uncertainties and point densities. These data have been organized into both "hard data" corresponding to exact measurements and "soft data" with a given uncertainty. The spatial random field $Y(x,z)=log_{10}(K_S(x,z))$ indicates $log_{10}(K_S)$ of the soil at location (x,z), where x(m) is the longitudinal coordinate along our study transect, and z(m) the depth. Y_h , Y_s and Y_k denote Y at: the hard data points (where Y_h is obtained from geotechnical measurements), the soft data points (where Y_s is derived from ERT and petrophysical relationships), and the estimation point, respectively.

BME relies on two principles: (i) maximum entropy theory processes the general knowledge base of means and covariances $G = \{m_Y, cov_Y\}$ and produces a "prior" f_G PDF (probability density function) describing the spatial process; and (ii) Epistemic Bayesian conditioning updates this prior f_G PDF with the site-specific knowledge base S, which then yields a BME posterior PDF f_k describing the value Y_k at any estimation point. Here, $S = \{Y_h, f_S\}$, where $Y_h = \log_{10}(Ks_H(x, z))$ is the measurement of the hard geotechnical data and f_S is a PDF describing the uncertainty associated with soft geophysical data; moreover, the BME posterior PDF is given by:

$$f_k(Y_k) = A \int f_G(Y_h, Y_S, Y_k) f_S(Y_S) dY_s, \qquad \qquad \text{Equation 4}$$

259 where A is a normalization constant.

The mean m_Y of field Y(x,z) is set to a first-degree polynomial, while the covariance cov_Y is obtained 260 261 by fitting an anisotropic covariance model to experimental covariance values calculated from the Y_h data. A covariance model quantifies the degree of similarity between pairs of measurements in terms 262 263 of their separation distance and the orientation of the line between such pairs. See Chils and Delfiner (1999) for details on how covariance models describe the variability of spatial processes; also, Olea 264 (2006) provided details on fitting a covariance model to experimental covariance values obtained 265 from a covariogram analysis. In this study, the experimental covariance values are calculated based 266 on a sample size (of Y_h measurements). The anisotropy model fitted to these experimental 267 covariance values is assumed to be exponential, with a major direction aligned with the x 268 269 (longitudinal) axis, and a ratio of covariance ranging along the major direction over the covariance 270 ranging along the transverse direction.

271 The soft data PDF $f_S(Y_s)$ is obtained by transforming $log_{10}(ER_{Interp})$ into $log_{10}(Ks_{Geo})$. (Mastrocicco et al., 2010) proposed a log-linear relationship between ER and Ks, hence the need for a 272 linear regression of the observed $log_{10}(Ks_{Geo})$ with respect to their corresponding $log_{10}(ER_{Interp})$. 273 Then, for each node of the inversion grid where a $log_{10}(ER_{Interp})$ is available but for which 274 275 $\log_{10}(Ks_H)$ was not measured, we set $f_S(Y_s)$ to a Gaussian PDF with a mean equal to the value predicted by linear regression $Y_s = \log_{10}(Ks_{Geo})$. However, for BME to work efficiently, we must set 276 the variance $\sigma_s^2(x,z)$ of $f_s(Y_s)$ to a value that captures the uncertainty in the Y_s obtained from 277 $log_{10}(ER_{Interp})$ at location (x,z). This can be accomplished by using the following: 278

$$\sigma_{s}^{2}(x,z) = \frac{r_{res}(x,z)}{mean(r_{res})}\sigma_{Y_{h}}^{2} + \frac{|z|}{mean(|z|)}\sigma_{z}^{2}$$
 Equation 5

where $r_{res}(x, z)$ is the resolution radius (Section 2.2.1.2.3.3), mean($r_{res}(x, z)$) its mean, $\sigma_{Y_h}^2$ the variance of Y_h , |z| the absolute value of depth, mean(|z|) its mean, and σ_z^2 a parameter obtained by maximizing the R^2 of validation (as explained in previous section). The terms $\frac{r_{res}(x,z)}{mean(r_{res})}$ and $\frac{|z|}{mean(|z|)}$ are unitless, while both $\sigma_{Y_h}^2$ and σ_z^2 have units of $\log_{10}(m.s^{-1})^2$. The first term in Equation 5 is equal to the resolution radius normalized to a variance, while the second term is a gradient with depth, also normalized to a variance. Combined, these two terms allow the BME to account for the fact that the uncertainty in the soft geophysical data increases with both r_{res} and depth.

286 2.4 BME validation strategy

We adopted a validation strategy to compare the estimation error of three methods: kriging (of the hard data alone), geophysics (i.e. geophysical data alone), and BME (i.e. fusion of both hard data and geophysical data). For the numerical simulations, we computed the estimation error by comparing the estimated Ks with $\log_{10}(Ks_{ref})$. Our field study was limited to $\log_{10}(Ks_H)$ at nh sampled locations, in which case we conducted a cross-validation analysis (Lee et al., 2009). The validation statistics used to assess model performance were: mean square estimation error (MSE), mean estimation error (ME), variance of estimation error (VE), and square of the Pearson correlation
 coefficient R² (Christensen, 2018).

3. Results 295 3.1. Numerical approach 296 Evaluation of hard data number 297 3.1.1. 298 Figures 4, 5 and 6 show the spatial distribution of log_{10} (Ks) for synthetic models 1, 2 and 3, respectively. The three columns in each figure represent the spatialization result when the number of 299 sampling points where $log_{10}[Ks_H]$ has been sampled equals 10, 24 and 50, respectively. The rows 300 301 offer the following: • Row 1: $\log_{10}(\text{Ks}_{\text{ref}})$. 302 Row 2: $log_{10}(ER_{Invers})$ data. The black circles indicate the sampling locations (where the 303 $log_{10}(Ks_H)$ data has been sampled from $log_{10}(Ks_{ref})$). 304 Row 3: log₁₀ Ks_{Geo}. 305 Rows 4 and 5: results of the spatialization $\log_{10}(Ks_H)$ data by means of kriging 306 ٠ $log_{10}(Ks_{Krig})$, associated with variance map σ^2_{Krig} . 307 Rows 6 and 7: $\log_{10}(Ks_{BME})$ and the estimated variance map σ_{BME}^2 . 308 The columns in each figure present all the results for several Ks samples (nh). Tables 2, 3 and 4 309 respectively summarize the following statistical tools: MSE, ME, VE, and R², applied to evaluate the 310 performance of these estimation methods. 311 3.1.1.1. Model 1 312 Figure 4b.3 shows the $log_{10}(ER_{Interp})$ map for a 50-point sampling (nh=50) conducted on a two-313 layer soil. The surface displays an initial layer (depth: 0-2.5 m) with an estimated $log_{10}(ER_{Interp})$ of 314 1.8. Two anomalies are present in this layer, at x = 5 m and 22 m. The synthetic reference model 315 (Figure 4a) shows two anomalies with the same thickness, whereas the anomalies are deformed and 316

317 stretched downward in Figure 4b. At depth, the layer with $log_{10}(ER_{Interp})$ of 1.4 is more reduced

than that in the reference model; it starts at the x = 2.5 m position and disappears at the x = 17 m position. In Figure 4c.3, the $log_{10}(Ks_{Geo})$ distribution is very similar to the $log_{10}(ER_{Interp})$ map. In Figure 4d.3, the result of kriging based solely on $log_{10}(Ks_{H})$ reveals a highly smoothed map; however, the BME results lie closest to the reference model. The surface anomalies are in the correct position and the shape of the anomaly is closer to reality (Figure 4f.3).

Reducing the number of samples to 24 hard data $(\log_{10}(Ks_H))$ produces no noticeable change in the proposed $\log_{10}(Ks_{Geo}))$ map. Kriging is more likely to overwhelm the anomalies. The BME fusion method provides an attractive $\log_{10}(Ks_{BME})$ estimate, with a reasonable number of samples. Let's note that reducing the number of points at depth reduces resolution of the anomaly at the position x = 10 m and z = 3.5 m.

The 14 sampling points are insufficient to cover all anomalies, which obviously influences the kriging 328 329 results and geophysical transformation by the empirical law; therefore, the BME fusion method is closest to the reference model. Indeed, the BME is capable of delineating large sand anomalies, yet it 330 tends to underestimate the extent of the clay anomaly at depth. This finding can be explained by the 331 lack of resolution of the ERT method at depth, where information from soft data is less reliable. 332 Figures 4e and 4g exhibit the variance for both the kriging and BME methods. The information given 333 by the σ_{Krig}^2 map is weak for data close to the Ks hard value: σ_{BME}^2 is minimized compared to σ_{Krig}^2 . 334 All visual results have been confirmed by error estimators, which are more efficient for the BME. 335

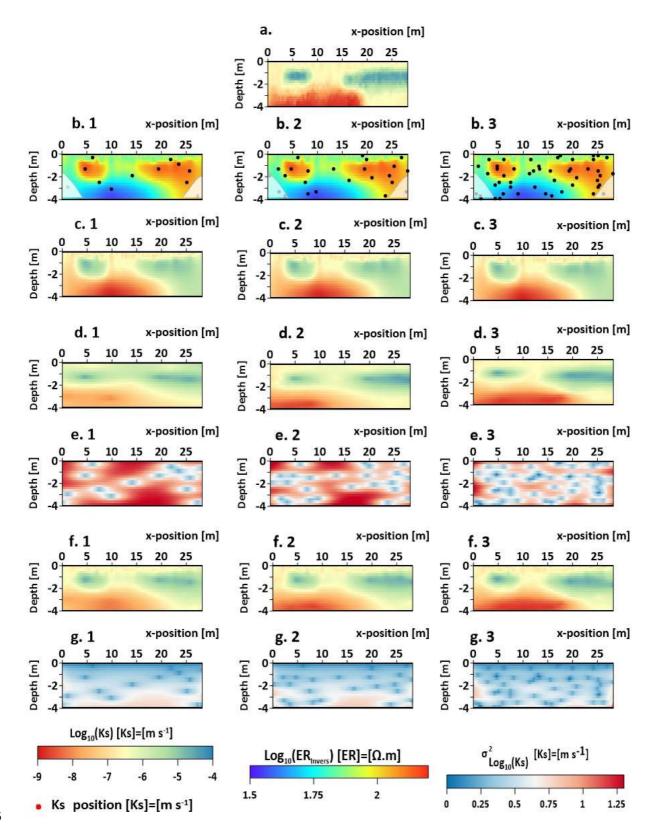




Figure 4: Spatial estimation of $log_{10}(Ks)$ and its variances for Model 1: kriging, geophysical transformation and BME at a constant WC for 14, 24 and 50-point sampling

	Model-1				
Method	nh	MSE	ME	VE	R²
Kriging	14	0.44	0.28	0.36	0.76
Geophysics		0.23	0.02	0.23	0.83
BME		0.23	0.11	0.22	0.88
Kriging	24	0.27	0.13	0.25	0.83
Geophysics		0.23	0.08	0.23	0.83
BME		0.18	0.09	0.17	0.89
Kriging	50	0.12	0.00	0.12	0.91
Geophysics		0.24	-0.04	0.24	0.83
BME		0.11	-0.03	0.11	0.92

Table 2: Statistical analysis of the spatialization of Model 1 for the three samples

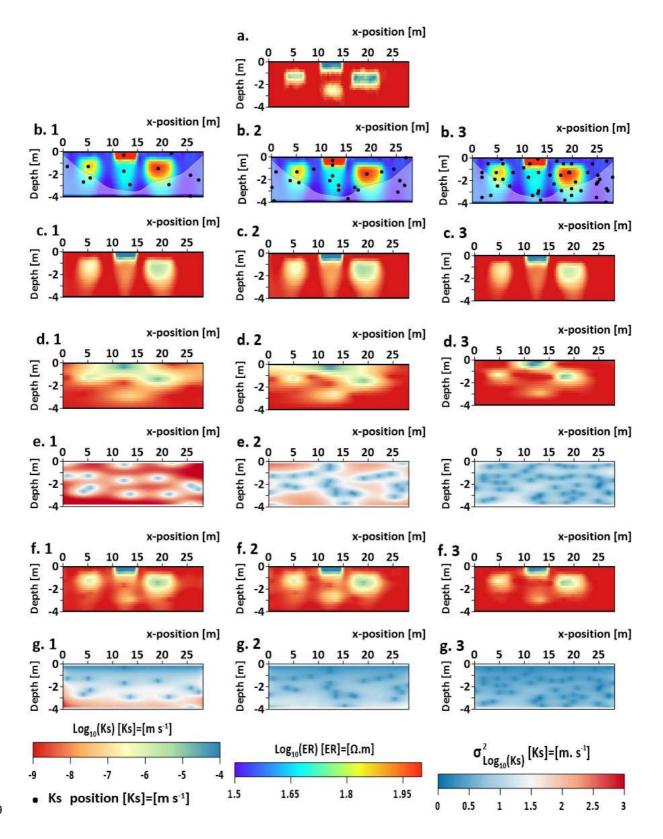
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3.1.1.2. Model 2

Figure 5 shows the spatialization of $log_{10}(Ks)$. Figure 5b.3 presents the $log_{10}(ER_{Interp})$ map and 343 estimated $\log_{10}[Ks_H]$ for 50 sampling points. In Figure 5c.3, $\log_{10}(Ks_{Geo})$ reveals the three clay 344 345 anomalies on the surface, but the silty anomaly is not apparent. The clay anomalies are stretched towards the bottom. In Figure 5d.3, kriging serves to identify the four anomalies; however, even with 346 such a large sample, kriging merges the two near-surface anomalies at the position x = 16 m. In 347 348 Figure 5f.3, the anomalies are correctly delineated with BME. We can observe that kriging deteriorates and merges the anomalies. BME would appear to be better with 24 points than with 50 349 350 because the loam anomaly is more sharply defined with 24 points. In reality, this outcome is due to the differentiation in the selected sampling points. More specifically, with a minimal number of 14 Ks 351 hard data, results maintain the same trend as with 50 and 24 points. Table 3 shows that for 50 352 $\log_{10}(Ks_H)$ sampling points, the BME method slightly improves the estimation result in terms of 353 correlation (R²=0.82 for nh=14 vs. R²=0.84 for nh=50) and targeting (MSE around 0.3). The increase in 354 355 number of samples (from 14 to 24 points) degrades the kriging estimate in terms of correlation; this 356 trend is linked to the random sampling that in this case has selected points of lesser interest. 357 Regardless of the number of samples, the R² calculation demonstrates that BME once again produces

358 the highest value in this second model.



360Figure 5: 2D estimation of $log_{10}(Ks)$ and variances for Model 2: kriging, geophysical transformation361and BME at a constant WC for 14, 24 and 50-point sampling

	Model-2				
Method	nh	MSE	ME	VE	R²
Kriging	14	1.52	0.75	0.97	0.43
Geophysics		0.41	0.07	0.41	0.75
BME		0.36	0.26	0.29	0.82
Kriging	24	1.46	0.57	1.14	0.39
Geophysics		0.45	0.22	0.41	0.75
BME		0.36	0.27	0.29	0.82
Kriging	50	0.51	0.03	0.51	0.69
Geophysics		0.40	-0.07	0.40	0.75
BME		0.28	-0.05	0.28	0.84

Table 3: Statistical analysis of the spatialization of Model 2 for the three samples

365

3.1.1.3. Model 3

Figure 6 presents the results of the spatialization of $log_{10}(Ks)$. For 50 points (Figure 6b.3), 366 $log_{10}(ER_{Interp})$ indicates the presence of two sand anomalies with a $log_{10}(ER_{Interp})$ of 2 and one 367 loam anomaly with a $log_{10}(ER_{Interp})$ of 1.7; meanwhile, ERT does not show the deep clay layer. In 368 Figure 6c.3, $log_{10}(Ks_{Geo})$ follows the $log_{10}(ER_{Interp})$ map. The kriging result in Figure 6d.3 exposes 369 370 a deep loam layer with well delimited anomalies. At the surface however, the method tends to merge anomalies. The BME results in Figure 6f.3 clearly identify the 3 anomalies as well as the loamy 371 layer. With 24 points, kriging (Figure 6d.2) of the surface anomaly is merged. The near-surface 372 anomalies and deep layer are well distinguished in Figure 6g.2 with BME methods; however, the first 373 anomaly on the left has been attenuated. With 14 points, BME correctly reproduced (Figure 6g.1) the 374 375 near-surface anomalies except for the loamy layer at depth. Visually, the BME method produces the best results. 376

Table 4 of the statistical indicators confirms that BME is, regardless of the number of points, always higher than kriging or geophysical transformation. In conclusion, the BME method seems to extract the best information from geophysical transformation and kriging; however, the number of samples does influence the spatialization of Ks by BME. In taking the results and statistical analysis into account, we feel that 20 infiltration test points offers a valuable number of points.

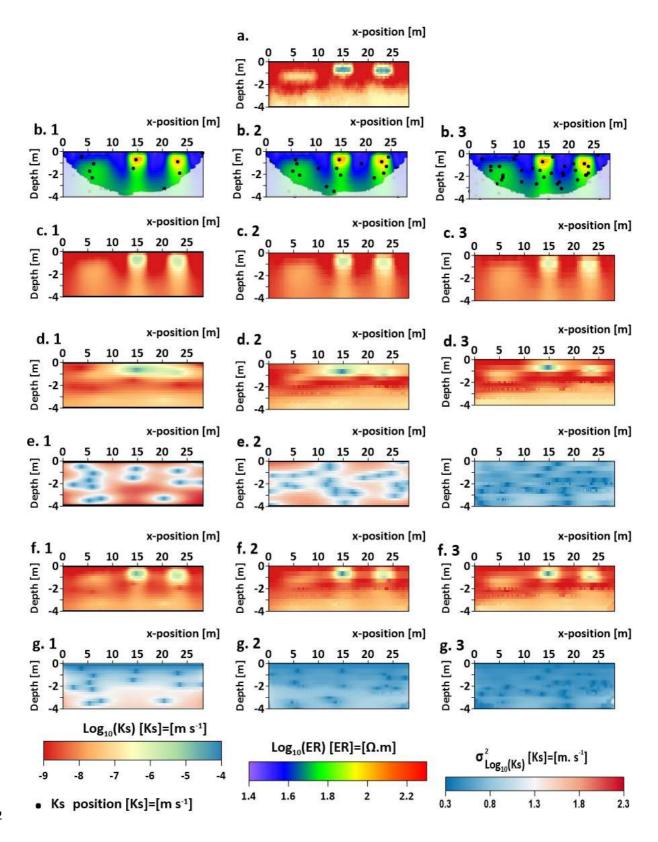




Figure 6: Spatialization of $log_{10}(Ks)$ for Model 3: kriging, geophysical transformation and BME at a constant WC for 14, 24 and 50-point sampling

	Model-3				
Method	nh	MSE	ME	VE	R²
Kriging	14	1.13	0.33	1.02	0.23
Geophysics		0.83	-0.37	0.69	0.43
BME		0.44	-0.13	0.43	0.68
Kriging	24	0.85	0.21	0.81	0.36
Geophysics		0.79	-0.32	0.69	0.43
BME		0.33	-0.11	0.32	0.81
Kriging	50	0.37	0.02	0.37	0.71
Geophysics		0.76	-0.24	0.71	0.43
BME		0.29	-0.08	0.28	0.83

388

3.1.2. Influence of variable soil WC

This section will consider the influence of variable soil WC, with 24 hard data values and the three same $\log_{10}(Ks_{ref})$ models. All results are presented in Figure 7; each column of the figure lists all results for the various models.

Figure 7b displays $log_{10}(ER_{Interp})$, which has decreased in depth and increased at the surface. This 392 393 change can be explained by the variable WC obtained from the groundwater flow model. Model 1 in Figure 7 shows that the simple petrophysical transformation of the data does not highlight the 394 variations in $log_{10}(Ks)$. Let's also note that the anomalies are heavily distorted, along with the 395 presence of an artifact at the 15-m position of the clay anomaly at depth. For Model 2, four 396 397 anomalies are distinguished, though a deep stretching of the central anomaly can be observed 398 (Figure 7c.2). Model 3 exhibits the three anomalies, but the clay layer is poorly defined; the loamy layer $(\log_{10}(Ks_{ref})=-7)$ (Figure 7a.3) at depth has been replaced by a clay layer $(\log_{10}(Ks_{Geo})=-9)$ 399 (Figure 7c.3). 400

The BME method is the one that best estimates the $\log_{10}(Ks)$ data. Compared to the reference models, the BME spatialization ($\log_{10}(Ks_{BME})$) actually reproduces all anomalies of the three distinct models.

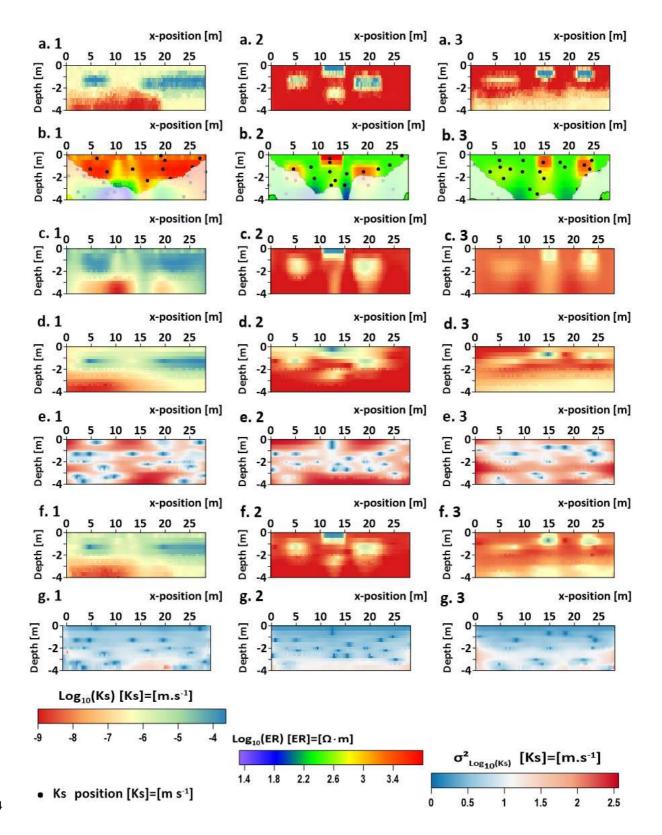


Figure 7: Spatialization of $log_{10}(Ks)$ for Models 1, 2 and 3: kriging, geophysical transformation and BME at a variable WC for 24-point sampling

Method	Model	MSE	ME	VE	R²
Kriging	1	0.28	0.14	0.26	0.81
Geophysics		0.46	0.10	0.45	0.68
BME		0.29	0.16	0.26	0.82
Kriging	2	1.23	0.38	1.08	0.41
Geophysics		0.48	0.06	0.48	0.70
BME		0.33	0.10	0.32	0.80
Kriging	3	0.42	0.12	0.41	0.66
Geophysics		1.14	-0.14	1.12	0.08
BME		0.43	0.05	0.43	0.77

Table 5: Statistical analysis of spatialization with BME, kriging and petrophysical relationshipfor all three models

Table 5 reports on the statistical tools used to evaluate the performance of estimators (kriging, 411 geophysics, BME) for all three models. It can be observed that the statistical analysis applied to the 412 models studied shows a strong correlation between the reference model and the BME method 413 result. For example, on Model 3, the correlation coefficient R² equals 0.77 for the BME vs. 0.66 for 414 kriging or 0.08 for kriging geophysics. The lower MSE value obtained with BME (0.43) reflects BME's 415 416 high accuracy and targeting. Although data from the $log_{10}(ER_{Interp})$ map are degraded, this has nevertheless allowed BME to improve the Ks spatialization, an extremely encouraging result that 417 underscores BME performance. 418

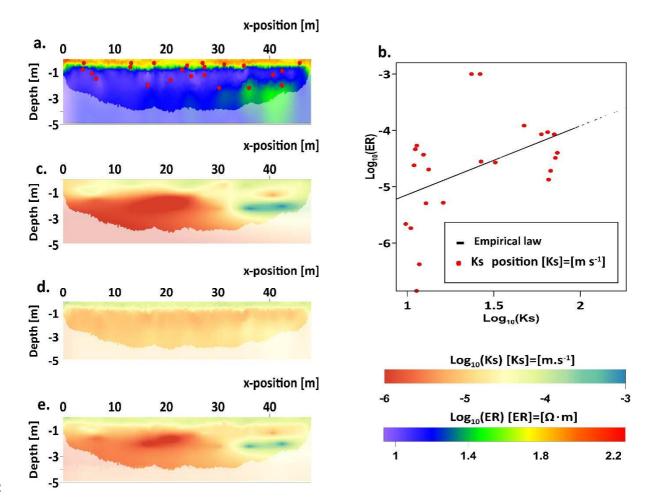
419 3.2. Field validation

420 Figure 8 presents the field result of a single ERT profile and 23 infiltration test $log_{10}(Ks_H)$ values. In Figure 8a, ERT results are presented on a 45-m line; also, the $log_{10}(ER_{Interp})$ points of low sensitivity 421 (coverage < 0.7) are masked. It can be acknowledged that the $log_{10}(ER_{Interp})$ measurement in this 422 area is not realistic. The $log_{10}(ER_{Interp})$ data show variations from 1 to 2.2 ($log_{10}(\Omega.m)$). Infiltration 423 tests (as represented by black points) have allowed us to determine that the $log_{10}(Ks_H)$ of the 424 parcel varies between -3 and -7 ($\log_{10}(m.s^{-1})$); this value is standard for Limagne soils, which are 425 often called "black soil". These soils contain varying clay and sand contents, which explains the 426 427 $\log_{10}(Ks_H)$ (Bornand *et al.*, 1984). The position of $\log_{10}(Ks_H)$ was identified according to the

sampling strategy presented above. Figure 8c presents the mapping of $log_{10}(Ks_{Krig})$ based solely on infiltration test data. Observations can be made of: a surface layer with an average value of -5 ($log_{10}(m.s^{-1})$), a deep anomaly (at the position x = 20 m and y = -2 m) with a value of -6 ($log_{10}(m.s^{-1})$), and another deep anomaly (at the position x = 4 m and y = -2 m) with a value of -3 ($log_{10}(m.s^{-1})$).

Figure 8d provides the map of $\log_{10}(Ks_{Geo})$ from the petrophysical relationship. Let's note the various layers between 0 and -1 m, with values on the order of $\log_{10}Ks_{Geo}$ =-4) ($\log_{10}(m.s^{-1})$). We can also distinguish a deep layer with values between -5 and -6 ($\log_{10}(m.s^{-1})$) inclusive. BME behaves here as the fusion of kriging and geophysical data. The surface layer is taken into account, and the deep anomalies highlighted by $\log_{10}(Ks_{H})$ appear in the final model of Ks. From a visual standpoint, BME takes the best features from both kriging and geophysics.

Based on cross-validation and statistical analysis (MSE, ME, VE and R²), BME slightly improves results with a high R² correlation index of 0.78 and a low root mean square error of 0.46. According to our statistical analysis, the BME method proves to be the most highly focused, accurate and correlated method.



442

443Figure 8: Spatialization of Ks on the data field: a) location map of infiltration tests on the $log_{10}(ER)$ 444profile (RMS = 3.55%); b) empirical law between $log_{10}(ER)$ and $log_{10}(Ks)$; c, d and e) Results of445the spatialization of $log_{10}(Ks)$ by kriging, geophysics and BME, respectively

446

Table 6: Statistical analysis of the spatialization of Ks on field data

Method	MSE	ME	VE	R²
Kriging	0.47	-0.08	0.49	0.77
Geophysics	0.51	-0.07	0.53	0.75
BME	0.46	-0.09	0.47	0.78

448 **4. Discussion**

449 Previous results lead the ensuing discussion to three points, namely: (i) the lack of validation data for

450 BME generalization, (ii) the sampling strategy, and (iii) its future applications.

452 4.1. Lack of validation data

453 Due to the lack of validation data, it is extremely difficult to consolidate these approaches in the 454 field. This work has proposed a static analysis to evaluate the BME data fusion methodology as a means of overcoming the absence of validation data. Nevertheless, the statistical indicator for 24 455 points is not adequately significant, and the method would require validation at other sites with a 456 larger set of available Ks data. In spite of this fact, the method has allowed obtaining, for the very 457 first time, an impressive map of Ks based on the available parcel information. To improve these BME 458 methods in the future, an expanded number of measurements at well-known reference sites will be 459 necessary. To date, the BME is an efficient method but cannot be definitively generalized. 460

461 4.2. Sampling strategy

The sampling strategy is based on ERT data for selecting the optimal Ks measurement location in the 462 463 field. Such a strategy has proven to be successful but is still capable of being improved. Indeed, ERT 464 does not recognize all potential anomalies. We have limited this bias by splitting our sampling strategy into two parts: first, sampling by electrical resistivity (ER) over a range with low uncertainty 465 for the ERT measurements; then, sampling randomly where uncertainty is high. However, when using 466 the numerical dataset, an evaluation of the hard data sampling number (Section 3.1.1.2) showed that 467 14 points could be better than 24 points for the kriging method, which means that the Ks sampling 468 point location could be improved even further. 469

Sampling remains a highly critical issue, especially with such strong constraints on the number of Ks measurements; these constraints are time-consuming and therefore expensive. As a result, the number of tests should be minimized and optimally located when investigating a TWW infiltration area of use for the BME. This challenge still needs to be addressed in the future. The authors are convinced that a better sampling protocol will improve kriging and therefore the BME results.

475 4.3. Future applications and outlook

476 Ks is an essential parameter for dimensioning a TWW infiltration area; it allows evaluating the 477 maximum TWW discharge load for a specific soil surface. Its main drawback however involves the difficulty in obtaining a sufficient number of Ks measurements (due to both time and financial costs) 478 in field applications. The geophysics and BME approach proposed in this paper was initially suggested 479 to solve such an issue. The method yields an accurate distribution of Ks by fusing 24 experimental 480 481 measurements of Ks with the ERT method. Yet for infiltration area design, conducting 24 infiltration tests remains too expensive. Consequently, it can only be applied to those cases representing a 482 serious risk for the environment. In order to overcome this method use limitation, we are proposing 483 484 to focus future research efforts on combining ERT and infiltration tests with less time-consuming methods, e.g. dynamic penetrometer. The BME method could also be generalized to other soil 485 parameters (e.g. WC) and applications, especially in the field of water resources management. 486

487 **5.** Conclusion

488 This article has proposed a new approach to obtain Ks spatial distribution based on the integration of ERT and infiltration test data in the BME method. This method allows for the fusion of point-specific 489 490 data, with a null variance (Ks), and distributed data, with a specific variance (ER). We have adapted the BME method to the specificities of both geophysical and geotechnical datasets. The results of this 491 492 study show that BME is a high-performance method producing maps with a lower variance than any of the other methods tested (kriging, petrophysical relationship). Indeed, BME offers a first-level Ks 493 distribution as well as many new possibilities, namely: i) the development of a new multi-method 494 approach to coupling geophysical and geotechnical methods, ii) application to other fields of 495 geosciences, and iii) use of results in hydrodynamic modeling for TWW infiltration area design. 496

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