Consideration of maintenance in wine fermentation modeling

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Abstract

We show that a simple model with a maintenance term can satisfactorily reproduce the simulations of several existing models of wine fermentation from the literature. The maintenance describes a consumption of the nitrogen that is not entirely converted into biomass. We show also that considering a maintenance term in the model is equivalent to write a model with a variable yield that can be estimated from data.

Key words: Wine fermentation, mathematical modeling, population model, maintenance, variable yield.

1 Introduction

The overall principle of wine fermentation consists in the conversion of sugar into ethanol by yeast. It has been observed from a long time that nitrogen consumed during the yeast growth is also playing an important role. The fermentation can be indeed modeled by a two-steps process where the yeast first grows on nitrogen as a limiting resource and then degrade the non-limiting sugar into ethanol and carbon dioxide. However, experimental observations have shown

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that the consumed nitrogen was not entirely converted into biomass. Several mathematical models have been proposed to take into consideration this characteristics. For instance, in [9, 13], the biomass growth follows a logistic law whose carrying capacity depends on the initial quantity of nitrogen. In [6], a model that distinguishes part of nitrogen used for yeast growth from another part responsible of the synthesis of proteins (hexose transporters [8]) has been developed. Both models have been calibrated with experimental data and provide satisfactory fitting. However, both models present some drawbacks. The dependency of the dynamics on the initial condition of the first model makes it sensitive to the precise knowledge of the initial quantity of nitrogen (that needs to be "memorized" in the dynamical equations of the model). Moreover it does not allow to consider non-batch operations or continuous addition of nitrogen, such as in [3] for instance. The second model relies on the knowledge of the time-varying concentration of transporters, which is in general not easily accessible to experimental measurements, and several assumptions have been necessary to estimate it from biomass measurements.

The observation of the ratio of produced biomass over nitrogen consumption along the whole fermentation, determined on experimental database or numerical simulations of models [6, 13], shows that this ratio is non-constant and depends on the initial quantities. This highlights that the conversion of nitrogen into biomass can be viewed as a variable yield process. The experimental evidence that nitrogen is not entirely used for growth therefore advocates for the consideration of a maintenance term in the modeling (see for instance [10]), without necessarily requiring a detailed representation of the internal mechanism or cells. The rationale of the results presented here is to test if the introduction of a maintenance term (see [15, 16, 17] or [1, 11, 21]) can improve the wine fermentation modeling. One of the originality of the proposed approach is to view the nitrogen consumption as a global consumption for growth by considering a variable yield. This allows to avoid to consider a specific structure to model the maintenance. The purpose of the present work is thus to investigate the ability of a simpler model with a maintenance term to reproduce and predict wine fermentation kinetics. It focuses mainly on the new modeling of the growth of yeast on nitrogen.

2   The proposed model

We denote by N, S, E, CO_2 and X the concentrations of (total) nitrogen, sugar, ethanol, dioxide carbon and biomass, respectively. For simplicity, we derive here a model under isothermal conditions.

For the first step $N \rightarrow X$ (yeast growth on nitrogen), we propose the following

equations

$$\frac{dX}{dt} = \mu_N(N, X)X \tag{1}$$

$$\frac{dN}{dt} = -\frac{\mu_N(N, X)X}{Y} - m(N, X)X \tag{2}$$

where Y is the growth yield, μ the Contois growth function

$$\mu_N(N, X) = \frac{\mu_N^{max} N}{N + K_N X}$$

and m a *maintenance* function, which is positive for $N > 0$ and $X > 0$. We choose here a ratio-dependent kinetics function μ_N to reproduce the observation that the growth is slowing down under an excess of yeast, with a Contois expression as in [6]. In the literature, the maintenance m is often considered as constant [15, 16], which has been validated in continuous culture (chemostat). However, as already investigated in [21], maintenance terms have to depend on the level of available resources, say R (N here). In particular, a constant maintenance in a batch model would imply $\frac{dR}{dt} < 0$ when the resource is exhausted i.e. $R = 0$, and thus R could take unrealistic negative values, as underlined in [17]. In [1, 11], the maintenance is directly related to the microbial activity which is stopped in absence of nutrients. This is why here we consider a maintenance function proportional to the growth activity, with a factor that might depend on the nitrogen concentration (one may expect that it decreases when the substrate N becomes rare)

$$m(N, X) = \alpha(N)\mu_N(N, X)$$

where α is a positive function equal to zero for $N = 0$. Then one can consider the function y defined as follows

$$y(N) := \frac{Y}{1 + \alpha(N)Y}, \quad N \geq 0$$

Formally, model (1)-(2) can be rewritten equivalently as

$$\frac{dX}{dt} = \mu_N(N, X)X \tag{3}$$

$$\frac{dN}{dt} = -\frac{\mu_N(N, X)X}{y(N)} \tag{4}$$

where the function y is playing the role of a *variable yield*. Identifying the function m or the function y is thus formally equivalent. However, we shall see in the next section that identifying the function y instead of m presents some practical advantages.

For the second step $S \rightarrow E + CO_2$, we follow the model proposed in the literature [6]

$$\frac{dE}{dt} = \frac{dCO_2}{dt} = \left[\mu_N(N, X) + \beta\nu(E) \right] \mu_S(S) X \tag{5}$$

$$\frac{dS}{dt} = -k\frac{dE}{dt} \tag{6}$$

where μ_S is a Monod function and ν_E a function inhibited by the ethanol

$$\mu_S(S) = \frac{\mu_S^{max} S}{K_S + S}, \quad \nu_E(E) = \frac{1}{1 + K_E E} \tag{7}$$

The inhibition by the consumption of sugar S by ethanol E has been reported many times in the literature [2, 5, 12, 18, 20]. The constant yield of production k of CO_2 and consumption of S follows a mass balance assumption, verified experimentally [7] and that can be determined with thermodynamics considerations [19].

Note that this model can be extended to anisothermal conditions, considering that the maximal specific rate parameters μ_N^{max}, μ_S^{max} and affinity constants K_S, K_E are temperature-dependent, as in [6].

3 Calibration of the model

From model equation (1), the parameters of the function μ_N can be identified independently of the yield and maintenance terms. To validate the hypothesis of ratio-dependency of the function μ_N, one can first plot from experimental data the slope of the logarithm of X versus the ratio $r = N/X$ and check if it follows qualitatively a function of the form

$$\mu(r) = \frac{\mu_N^{max} r}{K_N + r}$$

Then, a classical least-square method can be applied to fit parameters μ_N^{max}, K_N on the data. Alternatively, one can plot the inverse of the slope of the logarithm of X versus the inverse of the ratio r to check if it follows qualitatively a linear dependency, as one get from equation (1)

$$\left(\frac{d\log X}{dt} \right)^{-1} = \frac{1}{\mu_N^{max}} + \frac{K_N}{\mu_N^{max}} \left(\frac{N}{X} \right)^{-1} \tag{8}$$

However, for the accurate identification of the parameters μ_N^{max}, K_N, a linear regression on equation (8) is expected to be less reliable than a non-linear least

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square optimization on the solution $X(\cdot)$ of (3), because $\left(\left(\frac{d}{dt}\log X\right)^{-1}, \left(\frac{N}{X}\right)^{-1}\right)$ data might be far to be uniformly distributed.

Note from equations (1)-(2) that one has

$$\lim_{t \to +\infty} N(t) = 0$$

(because the derivative of N cannot vanish when N is not exhausted). In absence of the maintenance term m, one gets $\frac{dX}{dt} + Y\frac{dN}{dt} = 0$ which implies that one should have

$$Y = \frac{X(+\infty) - X(0)}{N(0) - N(+\infty)} = \frac{X(+\infty) - X(0)}{N(0)}$$

To test the validity of the model with maintenance, one can plot from experimental data the ratio $\frac{X(+\infty)-X(0)}{N(0)}$ for different values of $N(0)$ to check that it is not constant. If it is the case, one can then look for identifying a non-constant function y. For this purpose, we write from equations (3)-(4)

$$X(+\infty) - X(0) = -\int_0^{+\infty} y(N(t))\frac{dN}{dt}(t)\, dt$$

and as $t \mapsto N(t)$ is a monotone decreasing function, one can make the change of variable $n = N(t)$ in this last integral to obtain

$$X(+\infty) - X(0) = \int_0^{N(0)} y(n)\, dn$$

Therefore, if one fits a differential function f such that $f(0) = 0$ that satisfies

$$X(+\infty) - X(0) = f(N(0))$$

for experimental data with different values of $N(0)$, then one simply get $y = f'$.

Let us underline that identifying the function y in this way can be done independently to the knowledge of the kinetics μ_N, differently to the function m, what clearly presents some robustness advantages. Once the function μ_N is identified, the maintenance function can then be determined as

$$m(N, X) = \left(\frac{1}{y(N)} - \frac{1}{Y}\right)\mu_N(N, X)$$

where $Y = y(0)$ (to fulfill $\alpha(0) = 0$).

For model equations (5)-(6), the coefficient k is kept from the literature, and the parameters β, μ_S^{max}, K_S, K_E are identified (with a least-square method) from experimental data of CO_2 production rate.

4 Validation of the model on synthetic data

We have used synthetic data generated by models of the literature that have been previously validated on experimental data [6, 13] for a certain range of initial conditions and operating conditions.

4.1 Validation on simulations of a model with transporter

We have considered the model with transporters developed in [6], which is more complex with two additional state variables: the concentrations of hexose transporters and the nitrogen dedicated to these transporters. Data have been generated by simulating this model with the parameters given in [6] and operating conditions given in Table 1.

$X(0)$	$0.02\ g.l^{-1}$
$N(0)$	$0.071 - 0.57\ g.l^{-1}$
$S(0)$	$200\ g.l^{-1}$
time horizon	350 hours
temperature	constant equal to 24°
others	no initial transporter
	no nitrogen addition

Table 1
Operating conditions for the simulation of the model with transporters

This model distinguishes explicitly two forms of nitrogen, one available for the yeast N_X and the other one N_{tr} for the transporters. To compare with the variable N of our model, we have considered the total nitrogen $N = N_X + N_{tr}$.

4.1.1 Estimation of the Contois function

Figure 1 shows a good fitting of the Contois function μ_N on data $\left(\frac{N}{X}, \frac{\frac{dX}{dt}}{X} \right)$ of the transporter model, with parameters given in Table 2.

μ_N^{max}	$0.103\ h^{-1}$
K_N	$0.0381\ g.l^{-1}$

Table 2
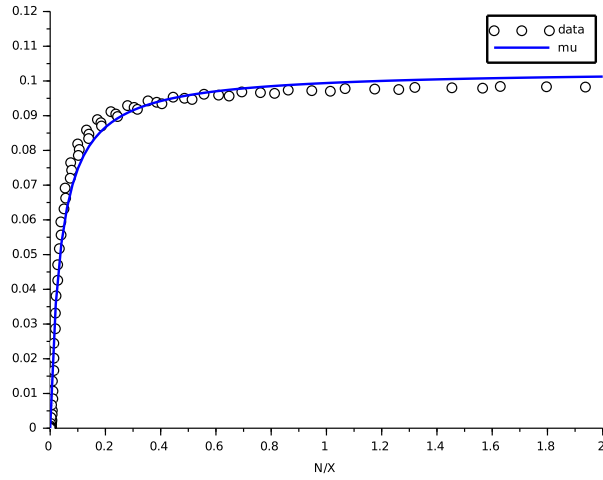Parameters of the Contois function μ_N

Fig. 1. Fitting of the Contois function on data of the model with transporters

4.1.2 Estimation of the variable yield function

On Figure 2, data $X(T) - X(0)$ versus $N(0)$ from the model with transporters have been plotted for $T = 350$ hours (we have checked that N is quasi-null at T and that X does no longer increase after T). One can see that the points are aligned but the line that passes through these points does not touch 0, which is not possible for a constant yield (for a constant yield, the points have to be aligned on a line that passes through 0 because when $N(0) = 0$ there is no biomass production).
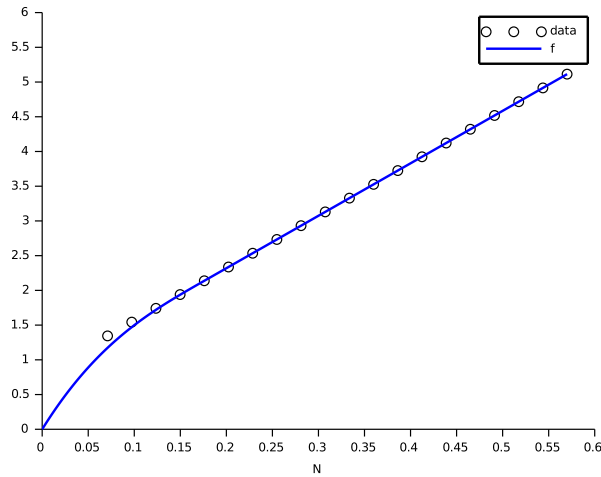

Fig. 2. Fitting the function f on data of the model with transporters

Then we have fitted a C^2 function f such that $f(0) = 0$ with the following

expression

$$f(N) = \begin{cases} aN + b\left(1 - \left(\frac{N_\dagger - N}{N_\dagger}\right)^3\right), & N < N_\dagger \\ aN + b, & N \geq N_\dagger \end{cases}$$

whose parameters are given in Table 3.

a	7.55
b	0.808 $g.l^{-1}$
$N_\dagger$	0.176 $g.l^{-1}$

Table 3
Parameters of the variable yield function y

Then, we obtain the variable yield function y as the C^1 function

$$y(N) = f'(N) = \begin{cases} a + b\frac{3(N_\dagger - N)^2}{N_\dagger{}^3}, & N < N_\dagger \\ a, & N \geq N_\dagger \end{cases}$$

and the function α which describes the maintenance as

$$\alpha(N) = \frac{1}{y(N)} - \frac{1}{y(0)} = \begin{cases} \frac{N_\dagger^3}{aN_\dagger^3 + 3b(N_\dagger - N)^3} - \frac{N_\dagger}{3b + aN_\dagger}, & N < N_\dagger \\ \frac{3b}{a(3b + aN_\dagger)}, & N \geq N_\dagger \end{cases}$$
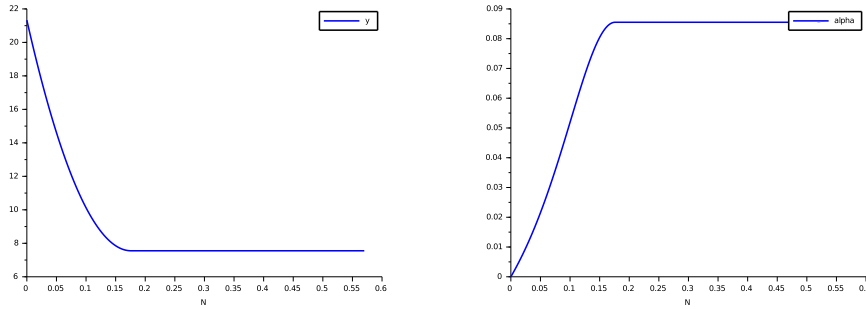
that are both depicted on Figure 3.

Fig. 3. The variable yield function y and the function α

Note that the model with transporters has been validated only for $N(0)$ in the interval $[0.071, 0.57]$ $g.l^{-1}$, and that we have no a priori information about the behavior of the yield for values of $N(0)$ smaller than 0.071 $g.l^{-1}$. The threshold parameter $N_\dagger$ has been simply chosen so that the simulations of the variables X and N of the model (3)-(4) were the closest from the ones of the transporter model.

4.1.3 Estimation of the other parameters and comparison of the models

For the model of the second step $S \rightarrow E+CO_2$, the stoichiometric parameter k has been taken for the literature, while the other parameters β, μ_S^{max}, K_S, K_E have been estimated with a least-square optimization on the CO_2 chronicles only (the CO_2 production rate being a variable that is usually measured in experiments), starting from values in [6]. Values are given in Table 4.

k	2.17
β	2.41
μ_S^{max}	0.197 h^{-1}
K_S	21.1 $g.l^{-1}$
K_E	72.7 $g.l^{-1}$

Table 4
Parameters for the second step $S \rightarrow E + CO_2$ model

Finally, we present on Figures 4, 5, 6 simulations of the new model for three largely different initial values of nitrogen from 0.170 $g.l^{-1}$ to 0.567 $g.l^{-1}$. The evolution of the ethanol concentration E has not been reproduced as it is proportional to the CO_2 concentration.

These simulations shows the ability of the new model to reproduce, with a single set of parameters, close simulations to the model with transporters, in terms of production of biomass and dioxide carbon, estimation of the peak of the CO_2 production rate and depletion of (total) nitrogen and sugar.
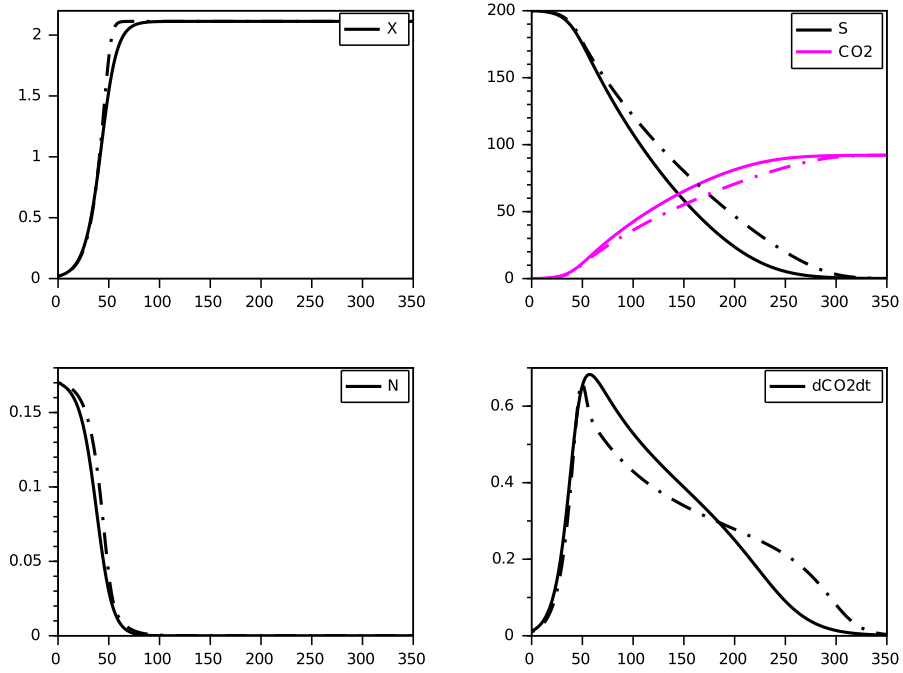
Fig. 4. Comparison with the model with transporters (in dashed) for $N(0) = 0.170\,g.l^{-1}$
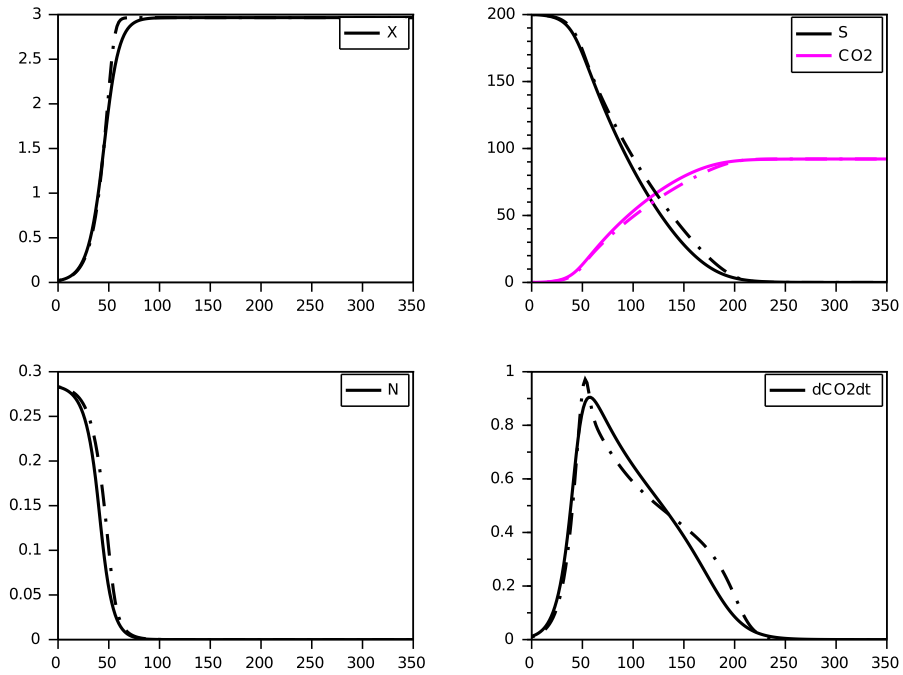

Fig. 5. Comparison with the model with transporters (in dashed) for $N(0) = 0.283\,g.l^{-1}$

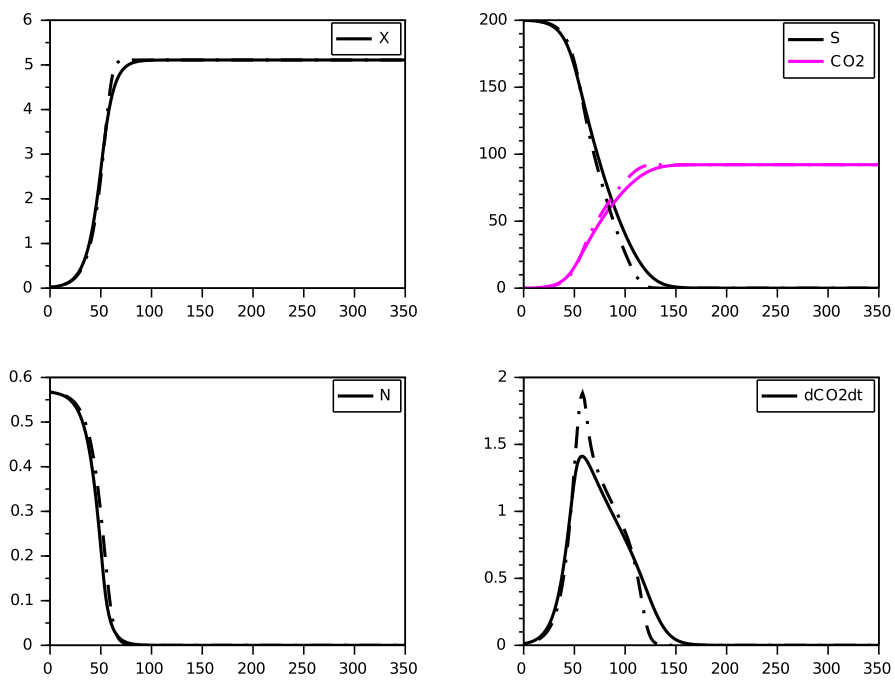Fig. 6. Comparison with the model with transporters (in dashed) for $N(0) = 0.567 \, g.l^{-1}$

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The model proposed in [13] does not consider explicitly transporters with an additional state variable as the previous model, and present instead more complicated expressions of the dynamics that depend on the initial condition, with an additional latency term at the beginning of the simulations. Therefore, this is not a Markovian model. It has been validated on different operating conditions, and has been encoded into the SOFA software exploited for decision making [9]. We have launched simulations of this model for the same operating conditions than for the previous model (Table 1). Although simulations look qualitatively similar, they do not overlap, especially for the biomass chronicle. This could be explained by the fact that this model is intended to predict a number of cells and not precisely a biomass (an average number of $4.15\,10^9$ cells for one g of biomass has been used to have X expressed in $g.l^{-1}$ as for the previous model). We have proceeded to a new validation of our model on these data.

4.2.1   Estimation of the Contois function

Figure 7 shows that the data $\left(\frac{N}{X}, \frac{\frac{dX}{dt}}{X}\right)$ do not follow precisely the graph of a function (this is most probably due to the fact that the model is not Markovian). Indeed, this happens mainly for large value N_0 of the initial nitrogen. We believe that this could be explained by the dynamics of the biomass X of this model, which is a logistic law with a carrying capacity given by an heuristic expression that depends on N_0, and not a dynamics coupled with the dynamics of N (indeed the interval of tested values of N_0 might be larger than the validity of this model). However, we have fitted the graph of a Contois function to these data with the parameters given in Table 5, which has been able to reproduce satisfactorily the trajectories of the model for a large amplitude of values of N_0, as we shall see later on. As one can see on Table 5, the values of μ_N^{max} and K_N are significantly larger and smaller (respectively) than in Table 2, which is consistent with the observation that this model predict a faster convergence of the biomass to its maximal value, despite the latency term (compare Figures 4, 5, 6 with Figures 10, 11, 12).

μ_N^{max}	0.270 h^{-1}
K_N	0.00952 $g.l^{-1}$

Table 5
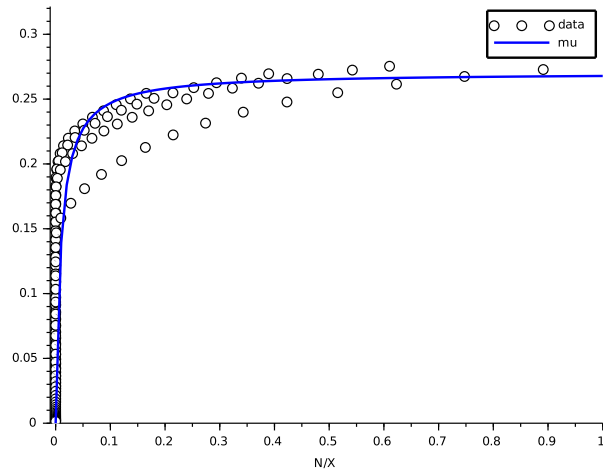Parameters of the Contois function μ_N

Fig. 7. Fitting of the Contois function on data of the SOFA model

4.2.2 Estimation of the variable yield function

Data $X(T) - X(0)$ from the simulation of the SOFA model have been plotted on Figure 8 at $T = 350$ hours, for different values of $N(0)$ in the interval $[0.071, 0.57]\, g.l^{-1}$ (here also we have checked that the fermentation was quasi-ended at T). On can see that the points follows an increasing concave curve and further increase very slowly, quite differently to the model with transporters (see Figure 2).
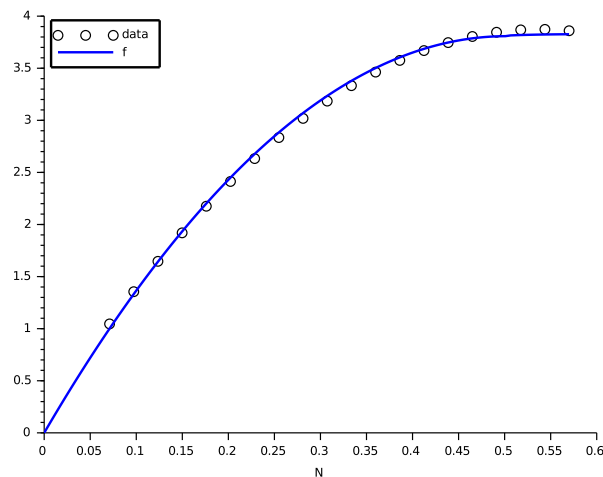

Fig. 8. Fitting the function f on data of the SOFA model

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We have then fitted a C^2 function f with $f(0) = 0$ for the expression

$$f(N) = \begin{cases} bN - aN^2, & N < N_\dagger \\ bN - aN^2 + bN + \frac{A}{B}\left(e^{-BN_\dagger} - e^{-BN}\right) & N < N_\dagger \end{cases}$$

with

$$A = (b - 2aN_\dagger)e^{BN_\dagger}, \quad B = \frac{2a}{b - 2aN_\dagger}$$

and parameters a, b, $N_\dagger$ given in Table 6.

a	15.1 $l.g^{-1}$
b	15.2
$N_\dagger$	0.465 $g.l^{-1}$

Table 6
Parameters of the variable yield function y

Then, we obtain the expression of the variable yield function

$$y(N) = f'(N) = \begin{cases} b - 2aN, & N < N_\dagger \\ Ae^{-BN}, & N \geq N_\dagger \end{cases}$$

as well as the function α

$$\alpha(N) = \frac{1}{y(N)} - \frac{1}{y(0)} = \begin{cases} \frac{1}{b - 2aN} - \frac{1}{b}, & N < N_\dagger \\ \frac{e^{b(N - N_\dagger)}}{b - 2aN_\dagger} - \frac{1}{b}, & N \geq N_\dagger \end{cases}$$
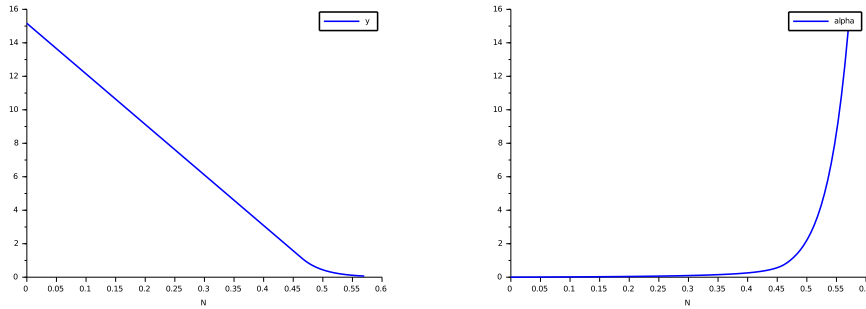
whose graphs are drawn on Figure 9.

Fig. 9. The variable yield function y and the function α

4.2.3 Estimation of the other parameters and comparison of the models

For the second step, the same stoichiometric parameter k has been taken for the literature, and the other parameters β, μ_S^{max}, K_S, K_E have been estimated

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with a least-square optimization on the CO_2 chronicles only (see Table 7).

k	2.17
β	3.22
μ_S^{max}	$0.197\ h^{-1}$
K_S	$17.6\ g.l^{-1}$
K_E	$36.4\ g.l^{-1}$

Table 7
Parameters for the second step $S \to E + CO_2$ model

Figures 10, 11, 12 show the comparison between the SOFA model and our calibrated model for the same initial condition than for the former comparison with the model with transporters. Here also, we see that the proposed model reproduces quite faithfully the simulations of the SOFA model, with the advantage of being a simpler Markovian model. Indeed, the difference between the model with transporters and the SOFA model can be translated into different maintenance terms (see Figures 3 and 9): for large values of nitrogen, the model with transporters behaves like a model with a maintenance proportional to the growth, while the SOFA model amounts to have a strongly increasing maintenance. Recall that the simulations for the largest value of $N(0)$ showed the most differences between these two models (for $N(0) = 0.567\ g.l^{-1}$, the model with transporters predicts a biomass production of $5.11\ g.l^{-1}$, while the SOFA model predicts $3.88\ g.l^{-1}$; see Figures 6 and 12). While the model with transporters has been validated experimentally for $N(0)$ in the interval $[0.170, 0.567]\ g.l^{-1}$, we believe the validation of the SOFA model for initial concentrations of nitrogen larger than $0.4\ g.l^{-1}$ might need to be revisited (although our model once calibrated is able to reproduce the SOFA simulations).
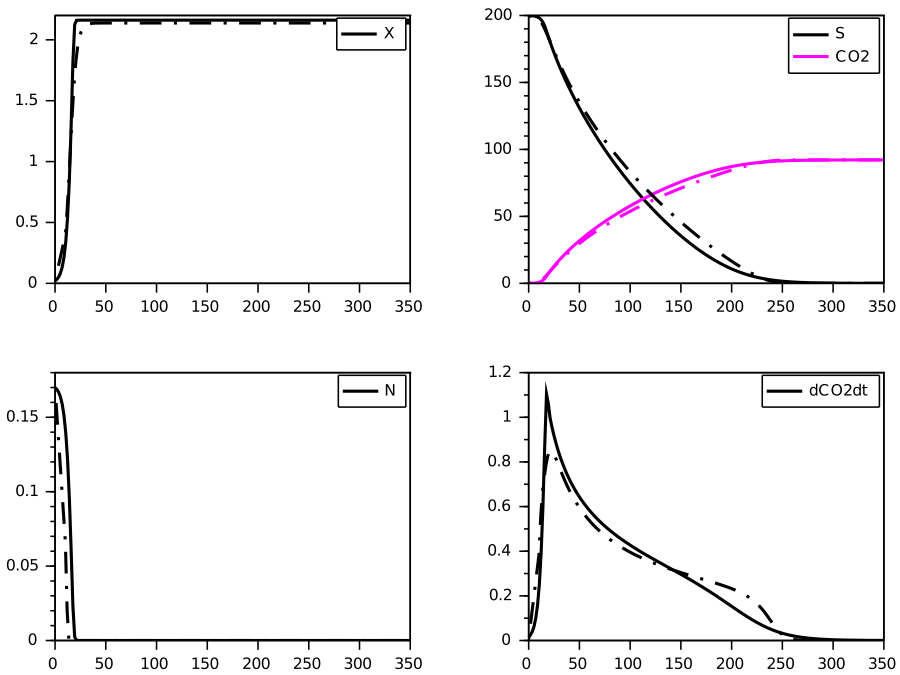
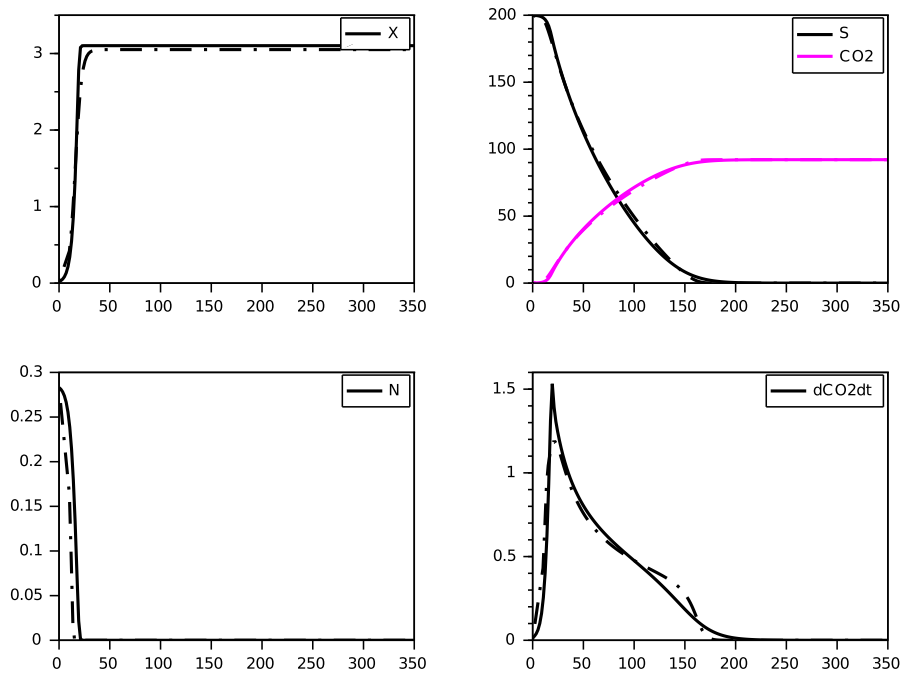Fig. 10. Comparison with the SOFA model (in dashed) for $N(0) = 0.170\,g.l^{-1}$

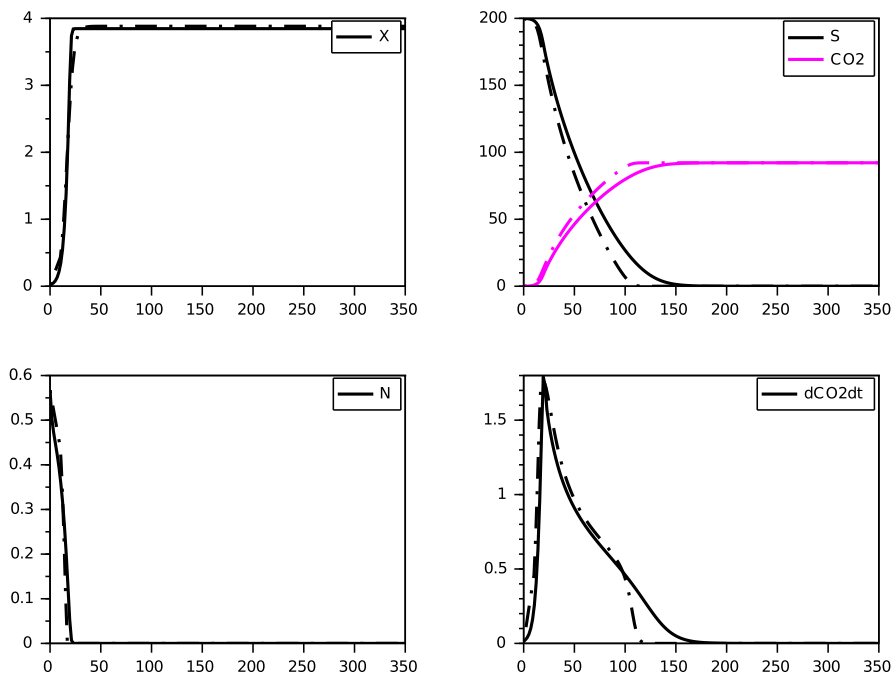Fig. 11. Comparison with the SOFA model (in dashed) for $N(0) = 0.283\,g.l^{-1}$

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Fig. 12. Comparison with the SOFA model (in dashed) for $N(0) = 0.567\,g.l^{-1}$

5   Calibration of the model on real data

We have considered data from experiments conducted at SPO Lab (INRAE, Montpellier, France) in 2004, that have been used to calibrate the model with transporters and the SOFA model (see [6, 13]). These data consist in a set of three experiments with the same operating conditions given in Table 1 and different initial concentrations $N(0)$ of nitrogen, exactly as for the simulations of Sections 4.1 and 4.2. For each experiment, one has

- height measurement points for X,
- no measurement point for N, S or E,
- about 400 measurement points for CO_2 and dCO_2/dt,

We have first calibrated a function $f(\cdot)$ to the data $(N(0), X(T) - X(0))$, with the same expression than in Section 4.2, to determine a yield function $y(\cdot)$ (see Figure 13).
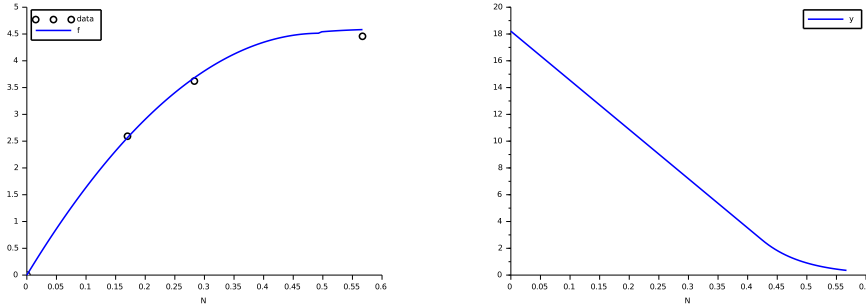

Fig. 13. Fitting the function f on the experimental data (left) and corresponding variable yield function y (right)

As we not have measurements of N over the time, we cannot estimate the Contois parameters independently of the CO_2 measurements, as we did with the synthetic data. All the parameters of the model have been fitted simultaneously with a least square method (values are given in Table 8), excepted for the sugar conversion yield for which we have used the value of the literature $k = 2.17$, as before. Figures 14, 15, 16, show the results of the fitting for the three experiments. One can appreciate the goodness of fit for a unique set of parameters. In particular, the production of biomass and CO_2, as well as the height and date of the peak of dCO_2/dt are well predicted with this model.

μ_N^{max}	$0.175\ h^{-1}$
K_N	$0.0133\ g.l^{-1}$
β	1.622
μ_S^{max}	$0.393\ h^{-1}$
K_S	$19.2\ g.l^{-1}$
K_E	$71.9\ g.l^{-1}$

Table 8
Parameters fitted on the experimental data
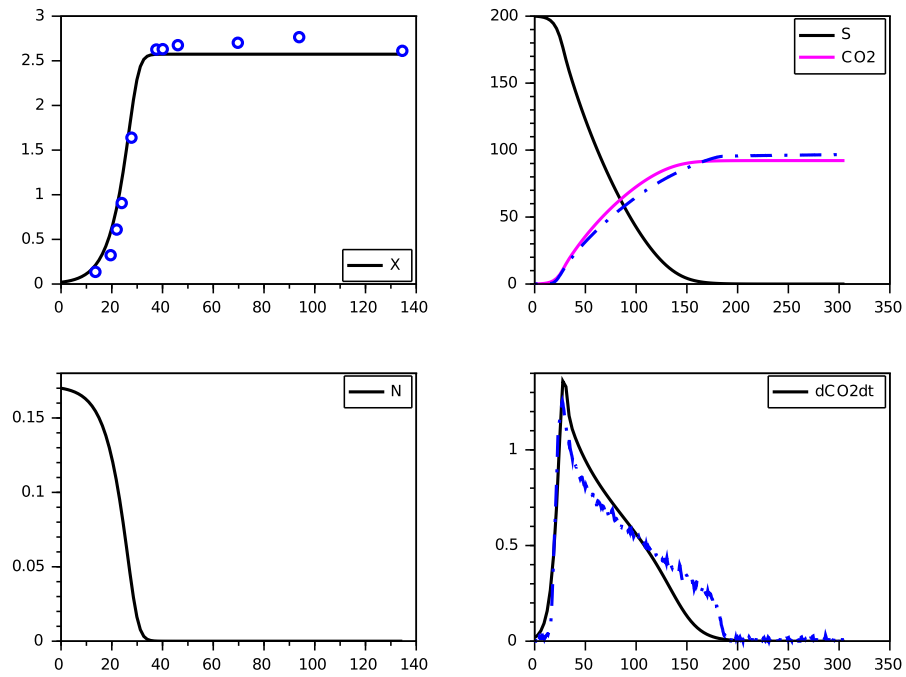

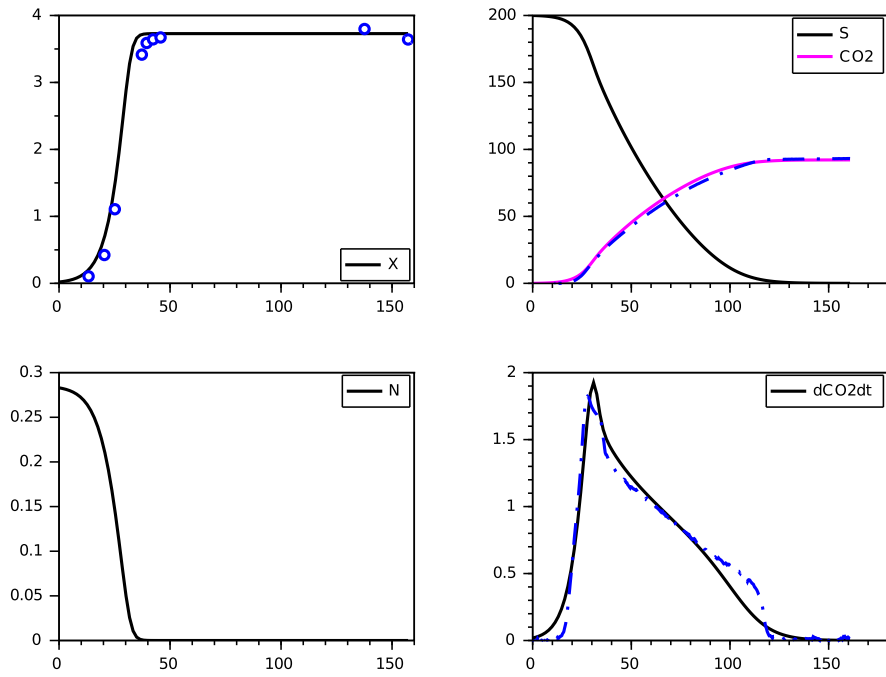Fig. 14. Simulation for $N(0) = 0.170\ gl^{-1}$ (experimental data in blue)

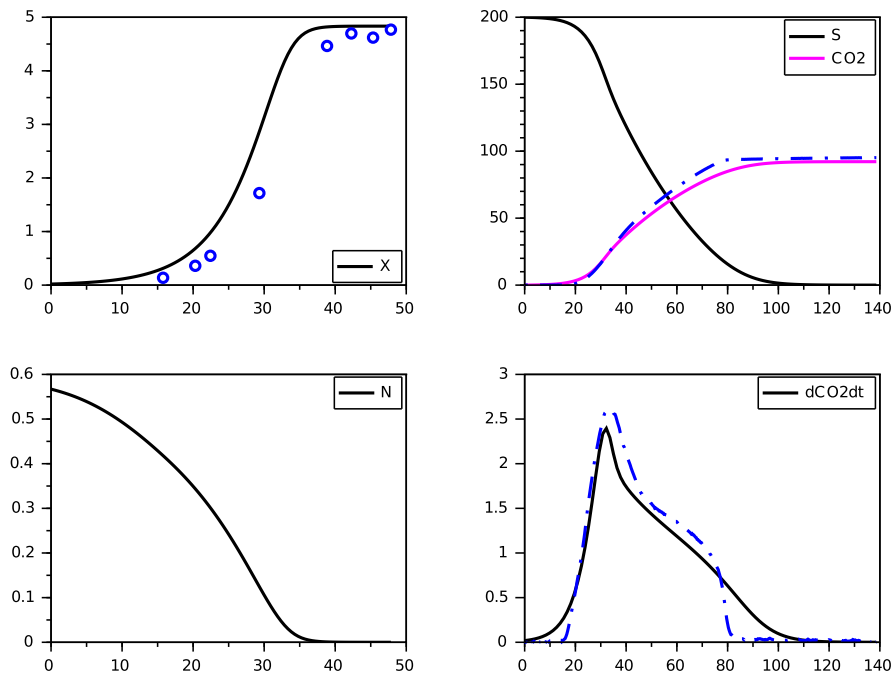Fig. 15. Simulation for $N(0) = 0.283\,gl^{-1}$ (experimental data in blue)

Fig. 16. Simulation for $N(0) = 0.567\,gl^{-1}$ (experimental data in blue)

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6 Conclusion

In this work, we have demonstrated that the consideration of a maintenance term, or equivalently a variable yield, in wine fermenting modeling can satisfactorily replace more sophisticated models with a simpler structure. Indeed, the effects of the underlying mechanisms of transporters, which are difficult to capture experimentally, are translated into a variable yield between biomass and nitrogen. We have shown that this variable yield, as a function of the nitrogen concentration, can be estimated from experimental data of biomass growth and nitrogen depletion. This consideration brings a flexibility to suit to different kind of models or experimental data (once calibrated) with a single common structure, that could correspond to different operating conditions or hypotheses in wine fermentation. This new approach opens new perspectives of control of fermentation with nitrogen addition, based on a simple Markovian model, as well as model extensions with aromatic compounds [14] or multi-strains [4].

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