

Model-based approach for treated wastewater reuse strategies focusing on water and its nitrogen content "A case study for olive growing farms in peri-urban areas of Sousse, Tunisia"

Mohamed Kefi, Nesrine Kalboussi, Alain Rapaport, Jérôme Harmand, Hakim

Gabtni

▶ To cite this version:

Mohamed Kefi, Nesrine Kalboussi, Alain Rapaport, Jérôme Harmand, Hakim Gabtni. Model-based approach for treated wastewater reuse strategies focusing on water and its nitrogen content "A case study for olive growing farms in peri-urban areas of Sousse, Tunisia". Water, 2023, 15 (755), 10.3390/w15040755. hal-03983740

HAL Id: hal-03983740 https://hal.inrae.fr/hal-03983740v1

Submitted on 11 Feb 2023 $\,$

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers. L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.



Distributed under a Creative Commons Attribution 4.0 International License





2

3

4

5 6

7

8

9 10

11

12

13

14

15

16

17 18

19

20

21

Article Model-based approach for treated wastewater reuse strategies focusing on water and its nitrogen content "A case study for olive growing farms in peri-urban areas of Sousse, Tunisia"

Mohamed Kefi^{1,*,†}, Nesrine Kalboussi^{2,†}, Alain Rapaport³, Jérôme Harmand⁴ and Hakim Gabtni¹

- ¹ Laboratory of Georesources, Water Research and Technologies Center of Borj Cedria (CERTE), Technopark of Borj Cedria, Tunisia ; Mohamed Kefi (M.K.) : mohamed.kefi@certe.rnrt.tn ; Hakim Gabtni (H.G.) : ha-kim.gabtni@gmail.com
- ² Laboratory of Desalination and Natural Water Valorization, Water Research and Technologies Center of Borj Cedria (CERTE), Technopark of Borj Cedria, Tunisia ; Nesrine Kalboussi (N.K.) : nesrinekalboussi@gmail.com
- ³ MISTEA (Mathématiques, Informatique et Statistique pour l'Environnement et l'Agronomie), University of Montpellier, INRAE, Institut Agro, Montpellier, France ; Alain Rapaport (A.R.) : alain.rapaport@inrae.fr
- LBE, University of Montpellier, INRAE, 102 Avenue des étangs, F-11100 Narbonne, France ; Jérôme Harmand (J.H.) : jerome.harmand@inrae.fr
- * Correspondence: mohamed.kefi@certe.rnrt.tn
- [†] These authors contributed equally to this work

Abstract:

One of Tunisia's main challenges is to conserve and protect water ressources for current and 22 future generations. Using non-conventional water in agriculture, such as treated wastewater, can be 23 a sustainable water-saving solution. Therefore, The objectives of this study are (i) to analyze the value 24 chain of treated wastewater for olive growing farms production and (ii) to apply mathematical mod-25 eling to maximize the olive production in optimizing irrigation distribution and nitrogen amend-26 ment in olive growing farms. The work is carried out in a peri-urban irrigated perimeter of Masken, 27 Sousse which is mainly occupied by olive trees and irrigated by treated wastewater. A SWOT anal-28 ysis is also applied to identify the strengths and weaknesses of reuse in this study area. Moreover, 29 mathematical models are used to determine the optimal schedule for fertigation with treated 30 wastewater. In this process, data on rainfall, soil, water quality and olive production were collected 31 from local farmers, local decision makers, field and laboratory experiments. SWOT results deter-32 mine farmers' perceptions of reusing treated wastewater for irrigation. The viability analysis, in 33 terms of soil humidity and nitrogen, shows that the nitrogen stress is not a limiting factor for olive 34 biomass production, but water stress is. This analysis provides numerical values for the maximum 35 irrigation rate and total amount of irrigation water to ensure maximum olive production. It was 36 found that the maximum irrigation could be 5.77 m3/day/ha and the total annual water requirement 37 is 1240 m3/ha. 38

Modeling appears to be an important tool to help local decision makers and to support and encour-39age local farmers to reuse treated wastewater under safe conditions and without environmental40risks.41

Keywords: Olive; Mathematical Modelling; Nitrogen; Reuse; Viability theory, Farmers' perception 42

Citation: To be added by editorial staff during production.

Academic Editor: Firstname Lastname

Received: date Revised: date Accepted: date Published: date



Copyright: © 2022 by the authors. Submitted for possible open access publication under the terms and conditions of the Creative Commons Attribution (CC BY) license (https://creativecommons.org/license s/by/4.0/).

1. Introduction

Population growth and its high concentration in urban and peri-urban areas com-44 bined with climate change induce an increasing pressure on water resources and an im-45 portant impact on the degradation of water quality [1,2]. It is estimated that about 2.3 46 billion people are in water-stressed countries, of which 733 million people are located in 47 high water-stressed countries [3]. Indeed, the highest stress levels occur in Northern Af-48 rica and in Western, Central and Southern Asia [4]. Due to the gap between water supply 49 and demand and the competition between economic sectors, water scarcity situation is 50 becoming more severe. Agriculture sector is the largest water consumer with more than 51 70% of all withdrawals globally and the water withdrawal ratio for agriculture can reach 52 90% in some arid countries [4]. Indeed, irrigated agriculture is essential to preserve agri-53 culture productivity, food security, to attenuate the effect of climate and to contribute to 54 the national economy. In this context, international communities are more conscious 55 about water issues and the United Nations has included among the 17 Sustainable Devel-56 opment Goals (SDGs), goal 6 which is dedicated to water and sanitation. Additionally, 57 climate change and anthropogenic activities have significant effects on water availability 58 which may cause decision and policy makers to focus on new strategies for water resource 59 management and water security for sustainable allocation and use [5]. 60

In water-scarce countries and regions, the reusing of wastewater provides a signifi-61 cant opportunity to substitute limited freshwater resources with reclaimed water for spe-62 cific purposes [6][7]. In addition to efficient water distribution systems and sustainable 63 agriculture, reuse of wastewater is a relevant action in reducing water stress [4]. Certainly, 64 wastewater is a possibly inexpensive and sustainable source of water, energy, nutrients, 65 organic matter and other useful by-products [8]. However, several barriers such as public 66 perception, pricing, technical and regulation are affecting the possibility of implementing 67 efficient water reuse strategies [9]. Like many countries in the MENA regions, Tunisia also 68 suffers from the problem of water shortage. Annual water resource potential is estimated 69 at 4898 million m³ with about 2700 million m³ is surface water and 2198 m³ is groundwater 70 [10] [24]. In fact, the total renewable water resource per capita is estimated at 420 m³/in-71 habitant/year which is considered a Key indicator of water scarcity [10]. Freshwater is not 72 used only for domestic purposes such as drinking but also for economic activities such as 73 agriculture or Industry. Furthermore, the agriculture sector has a great importance due to 74 its social impact. Agriculture is the first user of water compared to the other sectors, ac-75 counting for about 79% of freshwater [11]. However, water drinking is estimated at 15%, 76 Industry at 3% and tourism sector at 1% and other use at 2% [11]. In addition, population 77 growth and rapid development of the economic sectors have increased the problem of 78 water scarcity in Tunisia. Therefore, the government is facing a major challenge that deals 79 with preserving and protecting this scarce resource to fit the supply and demand of water. 80 For this reason, the government adopted several strategies to protect it and to maintain 81 balance between water demand and supply. The main strategies can be summarized as (i) 82 water surface mobilization through appropriate infrastructures such as dam; (ii) support 83 farmers to adopt techniques of water saving with incentive allowance ; (iii) implementa-84 tion of appropriate legislation and institutional systems for water resource management; 85 (iv) promote non-conventional water use in agriculture such as treated wastewater reuse 86 or brackish water desalination (v) improvement the involvement of local people in the 87 strategy through the etablishement of local water user association. Additionally, the Tu-88 nisian government developed two key strategies for the year 2050 related to water re-89 source management "Water 2050" and reuse "WATER REUSE 2050". Both strategies focus 90 on developing appropriate action plans to support and guide decision makers and water 91 managers. The Water 2050 strategy included several recommendations for water re-92 sources management based on forecasting models of supply and demand. These recom-93 mendations ar primerly related to water, infrastructure, governance, economy, and ecol-94 ogy [12]. However, the WATER REUSE 2050 focuses on reuse as an alternative solution 95

to conserve freshwater. The goal of this strategy is to implement a sustainable action plan 96 in terms of assessment, technologies, regulation, financing of treated wastewater [13] 97

The reuse framework in Tunisia started by launching research programs, the con-98 struction of several WasteWater Treatment Plants (WWTP) with advanced technologies 99 and appropriate sanitation systems, the involvement of several actors and the adoption of 100 several standards and guidelines for safe use [14]. Despite the efforts provided by the Tu-101 nisian government, the reuse rate is still low compared to potential treatment of 102 wastewater. Among 122 WWTP, only 61 treated plants are designed for reuse. In 2019, 103 about 284 million m3 were generated but only 13,4 million m3 are recycled for agriculture 104 purposes [15]. 105

From a circular economy perspective, recycling and reuse are the central concern and 106 water supply can be improved through better wastewater management strategies [16]. 107 Conversely, risks associated with water quality and human health must also be taken into 108 account [16]. Furthermore, it was estimated that 80% of all industrial and municipal 109 wastewater are rejected to the environment without treatment affecting overall water 110 quality, leading to negative impacts on human health and ecosystems [8]. Therefore, the 111 focus on appropriate technologies for an efficient water treatment is important to deter-112 mine reuse purpose [9]. Wastewater treatment is based on a combination of physical, 113 chemical, and biological processes to eliminate wastewater components [8]. Several tech-114 niques and methods for wastewater treatment are applied. Indeed, conventional methods 115 for removing metals are becoming inappropriate to meet rigorous permissible effluent 116 standards for an intended use [17]. Additionally, the implementation of advanced tech-117 niques as a tertiary treatment process may lead to good water quality for supplying irri-118 gation or domestic uses [18]. For example, Kalboussi et al. [19] conducted a life cycle as-119 sessment study to evaluate the environmental efficiency of water reclamation for agricul-120 tural irrigation among other conventional options. They found that the environmental im-121 pact of reclaimed water depends directly on the type of tertiary treatment technology and 122 the location of the treatment plant in relation to the field and other water sources. Natural 123 landscapes such as forests and wetlands have an important contribution in improving 124 water quality by decreasing sediment loadings, capturing and holding pollutants and re-125 cycling nutrients [8]. Nature-Based Solution (NBS) creates opportunities as an innovative 126 solution to improve ecosystem services, boost resilience and livelihood in water planning 127 and management [8]. 128

Treatment may improve the quality of treated wastewater to meet standards, but, 129 should also preserve nutrients. As wastewater is rich in nitrogen and phosphorus which 130 can provide nutrients to crops, the serious challenge for reuse agricultural irrigation is not 131 only to preserve quantities of nitrogen and phosphorus contained in the wastewater, be-132 cause these nutrients are essential for plant growth [20] but also to respect appropriate 133 guidelines for safe use [21], [22]. In order to implement sustainable and effective reuse 134 strategies, a good knowledge of soil-plant-water interactions is required. In this context, 135 crop models have been developed by several teams and have led to several software such 136 as AquaCrop [23], STICS [24], OPTIRRIG [25]among other ones. The simulations pro-137 vided by these models serve as predictive and decision support tools for agricultural prac-138 tices. More complex and comprehensive models have been developed as Global Change 139 decision support system DANUBIA [26]. For the processing, DANUBIA crop growth 140 model needs several data such as meteorological date, site-specific information, soil char-141 acteristics and farming practices. Additionally, the Nitrogen cycle was also integrated in 142 DANUBIA model to determine nitrogen turnover, nitrogen fluxes and storages [27]. These 143 approaches are based on relatively complex models with many variables and parameters, 144 which provide quite precise descriptions of the state of the soil-crop-climate system, but 145 are also quite heavy to conduct intensive optimization over a tactic time horizon [23,24]. 146 Other approaches are based on much simpler models (i.e. reduced models) that do not 147 intend to give a precise description of the internal functioning of the soil-crop system, but 148 rather focus on flux balance, and can therefore predict soil composition, water consump-tion, and biomass production at the field scale only [28,29,30,31,32]. This kind of models is thus better suited to apply optimization tools, because of their relatively small size. Moreover, the manipulated variables that typically describe irrigation and fertilization, and measurements such as soil humidity and crop water demand are usually considered at the field scale by practitioners. These reduced models can be validated on the more sophisticated models, which can also provide parameters sensitivity [28]. In this context, Pelak et al. [29] focused on the relationship between canopy cover, soil moisture and soil nitrogen content to optimize strategies of fertilization and irrigation. Moreover, Kalboussi et al. [30], [31] proposed a generic crop model named "TOYCROP" which is the basic ver-sion of the more advanced model "OPTIRRIG model". TOYCROP was developed to de-

termine optimal irrigation and nitrogen management via treated wastewater [31], [32]. Considering water scarcity in Tunisia, this research focuses on promoting reuse as an alternative solution to water saving and implementing of crop models for a sustainable reuse scheme. A feature of this study is the development of a model based on the combi-nation of treated wastewater and nitrogen as nutrient for olive production. Therefore, the main objectives of this study are (i) to analyze the value chain of treated wastewater for olive growing farm and (ii) to apply a mathematical model considering water and nitro-gen content in order to maximize olive yield in the treated wastewater (TWW) irrigated perimeter of Msaken, Sousse (Tunisia). This research may be useful for local decision mak-ers to provide appropriate guidance and recommendations for fertigation scheduling.

The next section presents the research framework and the description of the study area, as well as the approach used to characterize the optimal irrigation and nitrogen strat-egy. The main results related to the value chain and modeling are proposed and discussed in Section 3. Finally, section 4 summarizes the main outcomes of this research.

2. Materials and Methods

2.1 Research Framework

In this study, we focused on the reuse of treated wastewater in the irrigated perimeter in Msaken, Sousse. Figure 1 illustrates the main components of the approach applied. Specific parameters and datasets were used to implement the wastewater value chain and detect the interaction between irrigation and nitrogen based on a crop model analysis.

4 of 29

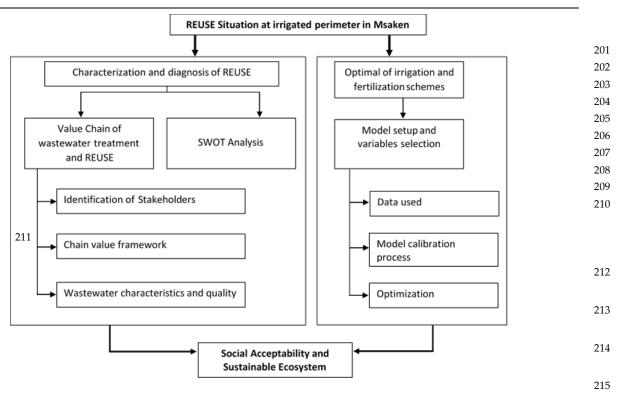


Figure 1. Framework of the applied approach

216

2.2 Study area description

The irrigated perimeter of Msaken from Sousse governorate is selected as a study 219 area. Sousse is characterized by water stress and overexploited and saline groundwater. 220 In order to provide safe water for users and to ensure water security, the local decision 221 makers adopted a strategy based on a transfer of water from neighboring governorates 222 (Zaghouan and Kairouan)[33]. It was estimated in 2021 that about 65% of distributed wa-223 ter resources is from internal resources including water surface, groundwater and treated 224 wastewater [33]. However, about 35% are external water resources. Among the internal 225 resources distributed, only 7% are coming from treated wastewater [33]. For this reason, 226 the reuse for agriculture purposes can be a way of mitigating water shortage problems in 227 Sousse. This irrigated perimeter of Msaken is located between 10°36"- 10°38" N latitude 228 and 35°45"-35°43"E longitude (figure 2). This perimeter was implemented in 2002 and it 229 was developed to reuse treated wastewater. This region is characterized by a semi-arid 230 climate with mild winter. Average annual rainfall is about 319 mm. The average monthly 231 maximum temperature is around 35°C in July and the lowest monthly average tempera-232 ture is around 6°C in January [34]. The geological formation in Msaken is dominated by 233 quaternary system and the Early Pleistocene. Soil is classified into two classes according 234 to the French soil classification : Poorly developed soil and Isohumic soils [34]. Due to its 235 nature, the soil is considered light soil. Texture varies with depth.Sandy clay texture is 236 dominant. The main rivers obsersed in the study area are Oued Melah, Oued Joubi and 237 Oued Manar [34]. The main productions of the perimeter are olive trees and fodders for 238 livestock. The area of this perimeter is approximately 178 km². WWTP of Msaken which 239 is managed by the National Sanitation Utility (ONAS) serves for treated wastewater sup-240 ply. The local water user association (GDA) is in charge of water distribution to local farm-241 ers through a volume-based cost process [34]. 242

242 243

5 of 29

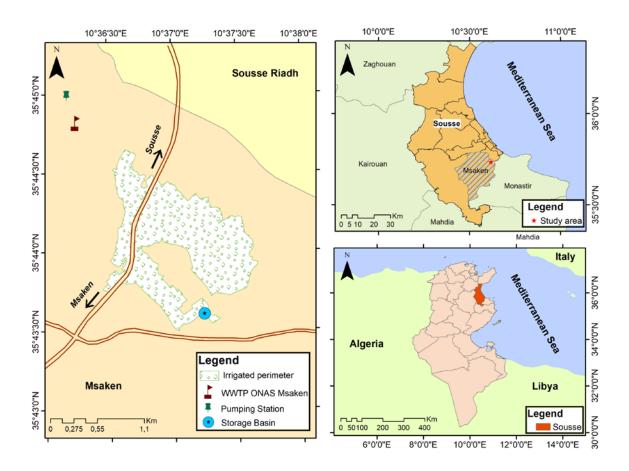


Figure 2. Study area location

2.3 Description of the applied approach

2.3.1 Treated wastewater reuse value chain

The concept of value chain is defined as all activities required to take a product from 248 the initial input-supply phase, through numerous stages of production, to its final market 249 destination [35]. In addition, value chain analysis is a process of breaking a chain into its 250 component parts to understand its structure and operation in detail [35]. In the case of 251 treated wastewater reuse, value chain was required to (i) identify the main actors involved 252 in the process from the wastewater collection to reuse; (ii) describe the main components 253 of the wastewater treatment system; (iii) monitor the water quality and quantity used; (iv) 254 identify local farmers' perceptions of treated wastewater. The value chain analysis was 255 useful in providing a SWOT (Strengths, Weaknesses, Opportunities and Threats) analysis for reuse in our study area. Moreover, SWOT analysis was conducted to identify the main 257 gap of reuse. 258

2.3.2 Crop Simulation model

- Crop model description: Crop models are an important tool for optimizing irriga-261 tion and fertilization strategies to maximize yields. In this context, a dynamic system, 262 based on the "ToyCrop" model [30] and the model of Pelak et al. [29], was developed 263 to describe the interaction of three main components: Soil moisture S(t), total soil 264 nitrogen content N(t) and olive biomass production B(t). The model is interpreted 265 on the daily timescale and applied over the course of a single growing season. 266
- Soil water balance: The relative soil humidity in the root zone (dimensionless between 268 0 and 1) is modeled as a balance between gains from rainfall (R) and irrigation (I) and 269

244 245

246 247

- 256
- 259
- 260

$$\frac{dS}{dt} = \frac{1}{\alpha \ Z} (R(t) + I(t) - T(t,S) - E(t,S) - Q_p(t,S))$$
(1)

276

272

Where α *Z* is the field capacity with α is soil porosity and *Z* is the root depth. 274 Transpiration rate (*T*) and evaporation (*E*), are given by equation 2 and 3 [30]: 275

$$T(t,S) = K_S (S) \phi(t) ET_0(t)$$
(2)

277

$$E(t,S) = K_R (S) (1 - \phi(t)) ET_0 (t)$$
 (3)

278

281

The function K_S is used to capture the plant stomatal response to soil moisture condition, as given by equation 4 [30]: 280

$$K_{S} = \begin{cases} 0, & S \leq S_{w} \\ \frac{S - S_{w}}{S^{*} - S_{W}}, & S_{w} < S \leq S^{*} \\ 1, & S > S^{*} \end{cases}$$
(4)

282

where S_w is the wilting point and S^* is the point at which stomata closure starts.283A similar function, K_R , is used to module evaporation, depending on the hygroscopic284point of soil, S_h , below which no soil moisture losses occur (equation 5).285A diagram of K_S and K_R as a function of S is shown in Figure 3 [30]:.286

$$K_{R} = \begin{cases} 0, & S \le S_{h} \\ \frac{S - S_{h}}{1 - S_{h}}, & S > S_{h} \end{cases}$$
(5)

287

288

7 of 29



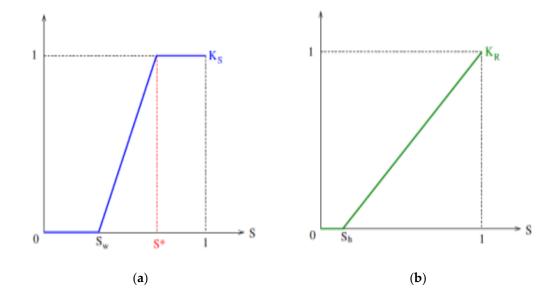


Figure 3. (a) Transpiration limitation function, (b) Evaporation limitation function

 $ET_0(t)$ is the reference evapotranspiration, which is calculated from meteorological data. There are several methods of estimating ET_0 but for our work we used the Blaney-Criddle formula, given by equation 293 6. 294

$$ET_0(t) = K_t (45.7 \ T_m + 813) \ p/100$$
 (6)

296

295

289

290 291

Where K_t is a climatic coefficient, T_m is the mean monthly temperature (°C) and p is the mean daily 297 percentage of annual daytime hours. The transpiration of olive is assumed to be proportional to the crop 298 radiation interception efficiency $\phi(t)$, which is a function between 0 and 1 that reflects the plant cover, 299 as mentioned in equation 7. 300

$$\phi(t) = \phi_{olive}(t) + \phi_{olive_{tree}}(t)$$
(7)

302

301

The soil evaporation is considered proportional to the uncovered part of the soil $(1-\phi(t))$. Deep percolation occurs through the water table, which is assumed to be deep enough not to intersect with the root zone. Water leakage Q_p calculation is based on formulation given by Pelak et al. [20], where k_L is the saturated hydraulic conductivity [m/d], d_L [Dimensionless] is leakage parameter and *S* is the soil moisture (equation 8).

308

$$Q_p = k_L \cdot S^{d_L} \tag{8}$$

• Soil nitrogen balance: The soil nitrogen balance estimates the full range of nutrient 310 inputs to and removals (offtakes) from soils. The input source is from fertigation, 311 which in the context of reuse irrigation, is taken as the product of the irrigation flow 312 rate I and the nitrogen concentration of the irrigation water C_N . The main removal 313 sources are leaching and plant uptake U for crop production, as presented in 314 equation 9 [29]. 315

316

$$\frac{dN}{dt} = C_N^{in}(t)I(t) - U(t, N, S) - L_N(t, N, S)$$
(9)

317

where N is the total mineral nitrogen content per unit area of soil. The plant uptake of 318 nitrogen *U* is taken as the product of transpiration and a nitrogen uptake limitation 319 function $f\left(\frac{N}{s}\right)$, which limits the nitrogen uptake above a certain critical concentration η_c 320 (equation 10) [29] 321

$$U(t,S) = \frac{1}{\alpha Z} T(t,S) f(\frac{N}{S})$$
(10)

323

322

 The function of nitrogen uptake limitation is given by equation 11 [29].
 324

 325

$$f\left(\frac{N}{S}\right) = \begin{cases} \frac{N}{\eta_c \ S}, & \frac{N}{S} \epsilon[0, \eta_c] \\ 1, & \frac{N}{S} \ge \eta_c \end{cases}$$
(11)

326

The nitrogen leaching L_N is proportional to the water percolation, Q_p , and the nitrogen concentration *N/S* as indicated in equation 12 [29]. 328

$$L_N = Q_p \frac{N}{\alpha \ Z \ S} \tag{12}$$

329

 Crop biomass: The model assumes that the biomass production is proportional to olive transpiration *T_{olive}*, with growth restriction in the case of water and nitrogen
 limitations (equation 13)
 332

333

$$\frac{dB}{dt} = W^* \ T_{olive}(t,S) \ f\left(\frac{N}{S}\right)$$
(13)

334

Where W^* is the normalized daily water productivity and olive transpiration is given335by equation 14.336

$$T_{olive}(t,S) = K_S (S) \varphi_{olive}(t) ET_0(t)$$
(14)

2.3.3 The sensitivity analysis

All mathematical models are approximate and their usefulness depends on the under-339 standing of the uncertainty associated with the predictions [36]. Uncertainty can affect 340 the accuracy of the results at every calculation stage [36]. Sensitivity analysis can deter-341 mine how variability in inputs leads to variability in outputs. In other words, it is an 342 approach to determine which parameters have the most or least impact on the output 343 solution. It quantifies the ratio of output disturbances to input disturbances. 344 A sensitivity analysis was conducted to investigate the behavior of the crop model re-345 sponse with respect to the uncertainty of the model parameters. A random bias of $\pm 10\%$ 346 was introduced in the calibrated parameters in order to generate a set of disturbed sys-347 tems. Then, the percentage of deviation from the error value using the parameters of the 348 nominal system is calculated according to the equation 15 349

350

Error on J (%) =
$$\frac{J_{nominal} - J_{pert}}{J_{nominal}}$$
 (15)

351

354 355

356

where $J_{nominal}$ is the quadratic error for the calibrated model and J_{pert} is the quadratic 352 error resulting from parameter perturbation. 353

2.3.4 The viability analysis

When dealing with decision support for irrigation, decision making faces the dilemma of 357 nitrogen concentration. While water supply is beneficial for crops, it can also dilute the 358 nitrogen concentration in soil which is penalizing for the plant to satisfy its nitrogen needs. 359 This dilemma needs to be reconsidered, especially in the context of reused water, since 360 additional nitrogen can be provided by the irrigated water. To better understand this new 361 water/nitrogen trade-off, we propose an approach based on the viability theory [37] rather 362 than pure optimization. The idea is to first formulate based on a model, the constraints to 363 be satisfied over the time season -in terms of soil humidity and nitrogen concentration- to 364 ensure the best biomass production at harvest. Then, the viability analysis consists in stud-365 ying the conditions under which it is possible for the system to meet these constraints at 366 any time with three manipulated variables: 367

The initial fertilization i.e., the amount of nitrogen at the time of seeding
 The nitrogen concentration in the irrigation water
 The maximal flow rate of the irrigation water
 370

We considered the crop model described in section 2.3.2 for which the state vector at time 371 t is composed of three variables: soil humidity S(t) (in percent), nitrogen quantity N(t) (in 372

mass per hectare), and biomass produced B(t) (in mass per hectare). The dynamics of these373variables are given by Eq.1, Eq.9 and Eq.13. Equation.13 indicates that biomass produc-374tion is maximum when its derivative is maximum at any time t, which means that the375following two conditions are satisfied:376

- S(t) is above the threshold S* for any t. This means that there is no hydric stress 377
- The ratio N(t)/S(t) is above the threshold η_c at any t. This means that there is no 378 nitrogen stress 379

Therefore, the viability problem is to investigate how to maintain the state (S(t), N(t)) in380the constraint's domain defined as follows:381

$$K := \left\{ (S, N) \; ; \quad S \ge S^* \; and \quad \frac{N}{S} \ge \eta_c \right\}$$
(16)

382

at any time $t \in [0,tf]$ with a control function I(.), depending on the initial state (where by 383 convention t=0 and t= tf are the seeding and harvesting dates). In particular, the maximum 384 value of the irrigation flow rate Imax plays an important role in forcing the trajectory solu-385 tion (S(.), N(.)) not to exceed the limits S=S* and N= η_c S of the constraints set K. A geometric 386 condition to stay within this domain is to find a value of control I everywhere on the bound-387 aries of K such that the velocity vector is within this set at all times. From the equations, this 388 implies a condition on Imax, that is called a "viability condition". For a given initial condi-389 tion (S0, N0), one can consider the null control I=0 (i.e., no irrigation) from the initial date 390 and determine by integration whether it first touches the boundary S=S* or the boundary 391 N/S= η_c . Depending on which boundary is touched first, we determine that hydric stress or 392 nitrogen stress dominates. We can then distinguish initial conditions for which the hydric 393 or the nitrogen stress is dominant (Figure 4 as an example). 394

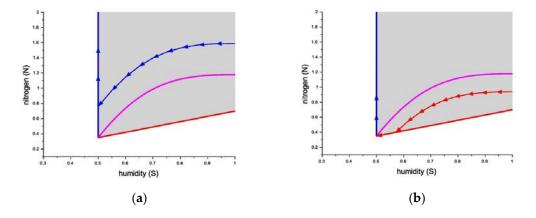


Figure 4. (a) Water stress dominant trajectory; (b) Nitrogen stress dominant trajectory

Once on the boundary of the constraint set, a control I(.) can be considered to keep the tra-396 jectory solution on the boundary up to the final state. The grey area in Figure 4 is the domain 397 K where biomass is maximum. The vertical line in blue is the water stress defined by the 398 constraint S=S^{*}, and the horizontal line in red is the nitrogen stress given by N/S= η_c . The 399 magenta curve represents the separation between the hydric and nitrogen stress. If we as-400 sume a waterlogged soil (S=1) and a high nitrogen stock at t=0 (Figure 4.a), the trajectory 401 (blue line with arrows) is toward water stress. At this point, irrigation is required to stay at 402 S=S*. On the other hand, if we assume S=1 and a low nitrogen stock at t=0 (Figure 4.b), the 403 trajectory (red line with arrows) first hits nitrogen stress. Finally, by integrating the control 404I(.) over time, we obtain the quantity of water required by this strategy to ensure that it 405 remains in the K region, that is to ensure maximum biomass production at the harvesting 406 date. This analysis was performed for the parameters of the model calibrated for the case 407 study of Msaken olive trees. 408

409

410 411

420

429

2.3.5 Data used and processing

Several data are used and generated for this research. A comprehensive literature review was con-412 ducted to obtain the useful documents related to the irrigated perimeter of Msaken. In addition, a 413 field survey is managed in the study area to gather detailed information on the functioning and 414 structures of the sewage treatment system. Two-level interviews were coordinated to make reliable 415 diagnoses of reuse situations and their impact, and to assess appropriate variables useful for math-416 ematical simulation. A representative sample of decision makers and end-users was selected based 417 on the implication to treated wastewater, reuse level and olive production. The two levels are de-418 scribed below: 419

- Level 1: Local decision makers. The main targets of the discussion were (i) to identify the 421 role of each stakeholder involved in major process of reuse in the study area; (ii) to collect 422 historical records related to monitoring the quantity and quality of treated water ; (iii) to 423 distinguish between the main steps of processing, treatment, distribution and reuse; (iv) to 424 indicate principal obstacles and barriers of reuse. 425
- Level 2: Farmers at the olive growing farms. Farmers surveyed were selected based on water
 reuse and agriculture production. The main questions are about reuse, land use, crops characteristics, agricultural practices and farmer's perceptions and behaviors towards reuse.
 428

Data required for the estimation of variables in each equation of the mathematical simulation were obtained from the field survey and laboratory experiments. For this purpose, soil and water sampling campaigns were carried out and appropriate laboratory analysis were conducted. Data related to the characteristics of treated wastewater and volumes used for irrigation are obtained from local partners GDA, CRDA and ONAS. We used data of 2020 in particular. We focused on the concentration of chemical properties of treated wastewater such as conductivity, Biochemical Ox-435

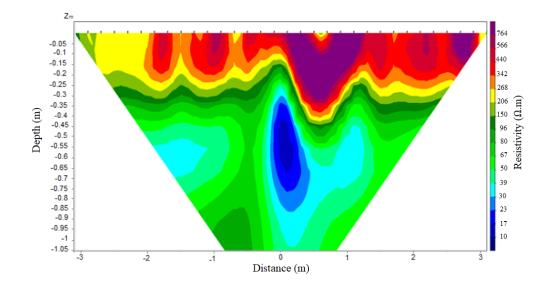
ygen Demand (BOD5), Chemical Oxygen Demand (COD) and Total Suspended Solids (TSS). Sev-	436
eral guidelines and standards are developed for wastewater reuse. At the local level, Tunisian	437
standard NT 106-03 refers to wastewater reuse in agriculture [38]. At the international level, FAO	438
has provided specific guideline and recommendations regarding to the use of wastewater in agri-	439
culture [39] . Recently, the European Parliament and of the Council adopted Regulation n° 2020/741	440
on minimum requirements for water reuse [40]. In this study, water quality parameters were sub-	441
sequently compared with Tunisian standards and guidelines to evaluate the performance effi-	442
ciency of wastewater treatment. Specific techniques and methods are used to measure the param-	443
eters. Conductivity is measured by conductivity meter. TSS is obtained by flitration, DCO is meas-	444
ured by titration[41] and DBO5 is developed by Dilution and seeding method[42].	445
Data related to rainfall was collected from the rainfall station of Msaken.	446
The required data for soil are soil texture, physicochemical parameters, root depth, soil nitrogen,	447
soil humidity and permanent wilting point.	448
A soil sampling campaign was conducted in January 2022 to determine the impact of treated	449
wastewater, focusing on changes in soil nitrogen and phosphorus concentrations. The plots were	450
selected according to the degree of irrigation. For each plot, Three soil samples were collected at	451
three depths (Depth 1: 0-20 cm; Depth 2: 20 – 40 cm; Depth 3: 40 – 60 cm)	452
✓ Plot 1: No irrigation for more than 3 years	453
✓ Plot 2: Moderate irrigation schedule and only olive trees were irrigated	454
✓ Plot 3: Substantial irrigation. Crops system is based on olive trees intercropped with fod-	455
der	456
	457
As Nitrogen is an important factor for plant growth and it is asle included in the simulation we	150

As Nitrogen is an important factor for plant growth and it is aslo included in the simulation, we 458 focus on the nitrogen in the soil. In this context, six additional soil samples were taken at a 459 selected farm from May to October 2022, to monitor the temporal variation of soil Nitrogen. this 460 nutrient was determined using the Kjeldhal method[43]. 461

Moreover, the root depth estimation was performed using Electrical resistivity tomography (ERT) 463 method. This method is applied to measure electrical resistivity which can lead to identify poten-464 tial freshwater and groundwater [44], [45]. However, the resistivity can be affected by several fac-465 tors such as soil water content, groundwater level, geological structure and other causes [46]. In 466 our study, ERT survey and prospecting was conducted by using ABEM SAS4000 multi-electrode 467 Earth Resistivity Meter and 32 electrodes chain with a 0.2 m inter-electrode spacing. A Wenner-468 Schlumberger array was adopted. Based on this approach and considering the value of resistivity 469 (localization of a prominent elongated low resistivity beneath the tree), it was detected that the 470average root depth in the selected olive growing farm is about 0,8 m. Figure 5 shows the ERT 471 profile related to the analysis. 472

473

- 474
- 475
- 476



3. Figure 5. ERT profile to assess root depth Results and discussion

In this section, the results of value chain analysis were presented and the SWOT was also elaborated. 479 Then, the optimal irrigation and nitrogen plan is developed through the mathematical simulation. 480

3.1 Value Chain of Treated wastewater reuse

The value chain analysis framework is illustrated by Figure 6. Three phases were determined.

Phase 1: Wastewater collection and treatment. ONAS is the main actor involved in this phase. It has
 the responsibility to collect raw water and to do the appropriate treatment in WWTP of Msaken.
 This WWTP was constructed in 1996. The treated plant includes a secondary treatment based on
 activated sludge process. The daily treatment capacity of domestic and industrial sewage is 7844 m3.
 The final effluent is reused in olive tree irrigation but the major portion of effluent is discharged in
 the environment.

Phase 2: Reuse. Several actors are involved in this action at local (Farmers/GDA), regional 489 (CRDA) and central (DGGREE) level. Farmers are the users of treated wastewater. The role of GDA 490 is to distribute water for the registered end-users with adequate pricing schemes to encourage water 491 reuse schemes. The fixed price is 0,035 DT/m3. The Msaken irrigated perimeter is created in 2022. The 492 total area of the perimeter is 178 hectares. The registered farmers in the GDA are about 77. Addition-493 ally, the main role of CRDA is to supervise the functioning of the irrigated perimeter and water dis-494 tribution. CRDA Staff has also the responsibility to implement extension services programs for farm-495 ers. However, the main activities of DGGREE are to implement the national strategies of reuse. 496

Phase 3: Control authorities. The main role of these institutions is to control the quality of treated 497 wastewater considering the Tunisian standard and guidelines. NT 106.03 of 1989 is the national stand-498 ard for reuse for agriculture purposes. NT106.02 of 1989 and the updated version of the Ministerial 499 decree of 2018 were produced for the control of effluent loaded in the environment. 500

478

481

482

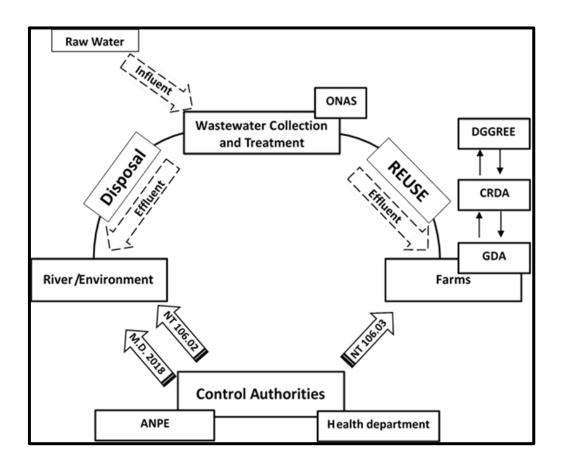


Figure 6. Framework of Value Chain of treated wastewater

ONAS : National Sanitation Utility ; DGGREE : General Directorate of Rural Engineering and Water Exploitation ; CRDA : Regional Office for Agricultural Development ; GDA : Water User Association ; ANPE : National Environment Protection Agency ; M.D.: Ministerial Decree

3.2 Monitoring of treated wastewater reuse

The reuse was assessed based on water volume and water quality.

3.2.1 Volume of effluent reused

Figure 7 shows the variation of the volume of effluent consumed by the farmers. We found that the 511 amount of treated wastewater that farmers consume varies. The annual average from 2012 and 2020 is 512 185 277 m3. The highest usage was in 2016 and the lowest is in 2020. The volume in 2020 was estimated 513 to be 69650 m3. This volume is only about 2% of overall treated wastewater provided by WWTP of 514 Msaken. Based on the survey and discussions with local users and managers, we found that farmers 515 mainly used TWW to irrigate their olive growing farms, and the main cultivar is Chemlali olive (Olea 516 europaea L.). The irrigation scheme depends on rainfall and the amount of TWW provided by ONAS. 517 In fact, olive trees can grow in difficult climatic conditions and with poor water quality [47]. Addition-518 ally, olive trees are an alternate bearing species which is characterized by low-yield "off-year" followed 519 by a high-yield "on-year" [48]. This situation can explain the fluctuations in water consumption in 2014, 520 2019 and 2020. However, water usage in 2016 was exceptional. This is because in the past, several local 521 farmers were dairy producers and they irrigated their land to grow pastures for their livestock. How-522 ever, due to various reasons such as livestock insecurity and declining subsidies for seeds, many farm-523 ers stopped this activity and focused solely in irrigating their olive trees in appropriate period. In fact, 524 supplemental irrigation of the Chemlali olive cultivar helps ensure and maintain olive yields [49]. As it 525 was presented in figure 8 ((a);(b)), few olive growing farms were irrigated. Indeed, there are only 32 526

501

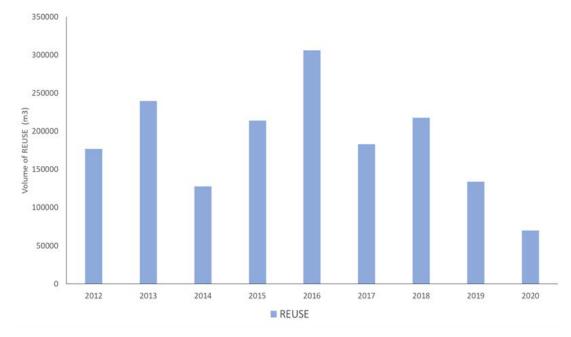
502 503 504

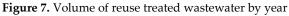
- 505
- 506 507

508

509

farmers in 2019 and 22 farmers in 2020. Due to several problems such as high price of forage seeds, 527 breakdown of pumping station or workers availability, the crop system in the irrigated farm is only 528 based on olive trees and small plots of fodder for livestock. For this reason, local farmers have developed irrigation strategies based on a complementary irrigation schedules at appropriate times. 530





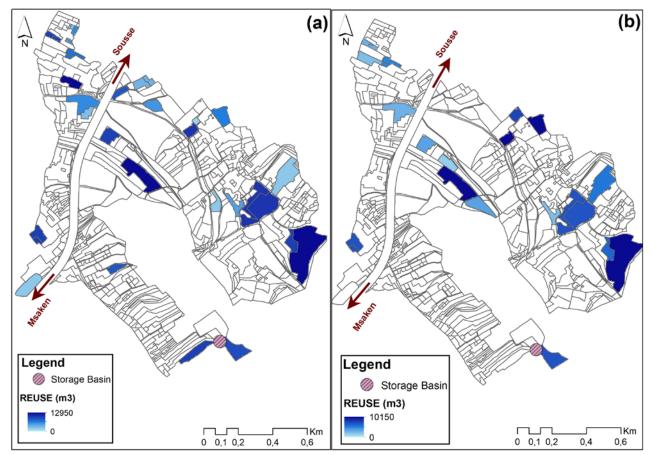


Figure 8. Spatial distribution of treated wastewater in (a) 2019 and (b) 2020

0

Jan

Mar

May

Influent

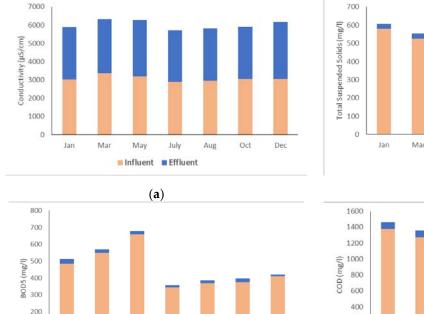
July

(c)

Effluent

3.2.2 Quality of effluent reused

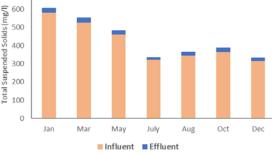
The treated wastewater used on this irrigated perimeter was monitored for the year 2020 to evaluate the 537 efficiency of the treatment plant of Msaken and its appropriateness for use on agricultural irrigation. In 538 this study, we focused on the 4 important parameters (Conductivity, Total Suspended Solids (TSS), BOD5 539 and COD). It was observed that the concentrations of these parameters were high before treatment and 540 they reduced after treatment as described in Figure 9. The conductivity is varied from 2830 to 3365 µS/cm 541 before treatment and after treatment, the conductivity of treated wastewater is from 2839 to 3104 µS/cm. 542 The removal efficiency of conductivity is 4%. For the case of TSS, the amount is varied from 274 to 579 543 mg/L before treatment but the concentration decreases after treatment and it is ranged from 16 to 27 544 mg/L. The removal efficiency of TSS is 95%. However, BOD5 before treatment is varied from 344 to 660 545 mg/L. After treatment, the value of BOD5 is from 9 to 30 mg/L. The performance of the BOD5 treatment 546 is high, about 96%. In addition, the amount of COD before treatment varies from 414 to 1377 mg/L. This 547 value has decreased drastically: COD ranges from 50 to 86 mg/L after treatment. The removal efficiency 548 is about 93%. The high efficiency of the treated plant is in accordance with the Tunisian standard (NT 549 106-03) for reuse in agriculture, as shown in Table 1. We can confirm that the quality of treated 550 wastewater is suitable for irrigation and does not pose any risk to human health. However, the salinity 551 of the soil must be monitored because the conductivity value is high. In this context, the impact of treated 552 wastewater on soil properties is also important. 553



Aug

Oct

Dec



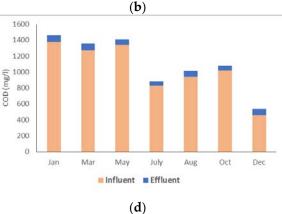




Figure 9. Monitoring influent and effluent flow of WWTP (a) Conductivity; (b) Total Suspended Solids (TSS); (c) DBO5; (d) COD

536

556

554

Parameter	Unit	Min	Max	Mean	Std. Devia- tion	Tunisia Standards NT 106-03
Conductivity	μS/cm	2839	3104	2919	90.84	7000
TSS	mg/l	16	27	22	3.36	30
DBO5	mg/l	9	30	20.08	6.52	30
COD	mg/l	50	89	69.45	14.02	90

Table 1. Treated wastewater effluent used for irrigation

3.2.3 Soil properties

Nitrogen and phosphorus are two important and basic natural components for the growth of living 560 organisms [50]. Additionally, in the case of soil nutrients deficiency, the use of synthetic fertilizers is a 561 significant factor in securing and increasing global food production[51]. Moreover, the high potentials 562 of the recuperated nutrient for reuse as fertilizer in agriculture is recognized[52]. In our research, we 563 focus on the variation of Total Nitrogen (N) and Phosphorus (P2O5)in soil as a function of irrigation 564 with TWW. The results presented in Table 2 show that the nutrients concentration increased under the 565 effect of irrigation. It is found that the total Nitrogen content at 0-20 cm depth in plot 1 (without irriga-566 tion) is 440 mg/kg, while in the most irrigated plot it was 1120 mg/kg. The same tendency is observed 567 for phosphorus. The highest concentration was obtained in plot 3 compared to the amounts in plots 2 568 and 1. Similar results were found in the research work of Hidri et al. [53]. The authors confirmed the 569 impact of treated wastewater reuse for irrigation and the increase in the amount of nutrients in the soil 570 after irrigation. Moreover, the application of excess amounts of nitrogen and phosphorus in the soil can 571 lead to groundwater contamination and eutrophication of surface water[54]. The optimal use of treated 572 wastewater can be a solution to reduce soil and water pollution. For this reason, the simulation of 573 nitrogen supply based on an optimal fertigation schedule can ensure olive yields and protect the envi-574 ronment. 575

Table 2. Monitoring soil nutrients

	<u> </u>	Plot 1 (No irrigation)		Plot 2 (Moderate irrigation)		Plot 3 (High Irrigation)	
-		Ν	P ₂ O ₅	Ν	P ₂ O ₅	N	P2O5
	Depth	(mg/kg)	(mg/kg)	(mg/kg)	(mg/kg)	(mg/kg)	(mg/kg)
-	0-20	440	3.2	710	3.2	1120	22.4
	20-40	320	1.8	350	0.8	810	10.5
	40-60	360	2.9	220	6.5	680	10.2

3.3 SWOT Analysis

The main outcomes of the SWOT analysis are presented in Table 3. The SWOT analysis pointed out 578 several advantages and barriers to the development of the reuse in the irrigated perimeter of Msaken. 579 Indeed, the application of reuse based on mathematical simulation can lead to ensuring sustainable irrigation and fertilization schedules. 581

557

558

559

576

580

577

582

587

Strengths	Weaknesses
- High treatment efficiency of TWWP	- Low Reuse rate
- Great collaboration between the actors	s - Land fragmentation
involved in the reuse value chain	- Crop system dominated by a monoculture
- Experienced staffs and motivated farmers	practice, mainly olive trees
- High productivity of Olive growing farms	- Breakdown of pumping station
- Appropriate regulations and standards pro- cedures	Low level of youth participation in agriculture practice
- Nutrients recovery benefit	
- Very Low price of treated wastewater	
Opportunities	Threats
- Reuse is an asset to develop various agricul-	High proportion of abandoned and unculti-
ture activities	vated lands
1 C	vated lands
ture activities	vated lands Increase of population in surrounded areas
ture activities - Geographic location of Msaken irrigated pe-	vated lands - Increase of population in surrounded areas n can affect the treatment performance of
ture activitiesGeographic location of Msaken irrigated perimeter between Sousse and Monastir can	vated lands - Increase of population in surrounded areas n can affect the treatment performance of s TWWP

3.4 Crop	model	Simulation

3.4.1 Model calibration

clude research activities and extension ser-

In order to calibrate the crop model, the simulation time considered for our analysis is the annual development cycle of the olive tree. It was considered from 1st January 2022 to 30 November 2022. The data used related to soil parameters are summarized in Table 4. 592

Table 4. Soil parameters

vices

-				
Parameter	Name	Value	Units	Source
S*	Point of incipient stomatal closure	0.62	-	Soil analysis
Sw	Wilting point	0.02	-	Assumption
Sh	Hygroscopic point	0.02	-	Soil analysis
Ζ	Root Depth	0.8	m	ERT method
α	Soil porosity	0.21	-	Soil analysis

594

599

588

589

593

The parameters of the crop model shown in table 5 were estimated by the least-squares fitting 595 to experimental data using the MATLAB optimization function "fminsearch". The experimental data used for the calibration of the model are mineral nitrogen content in the soil obtained by laboratory analysis and the biomass of olives at harvesting period. 598

Table 5. Estimated parameters

Parameter	Name	Value	Units
η_c	Maximum N concentration taken up	0.047	Kg N/m3
w*	Normalized daily water productivity	5539.8	Kg B/m2/day

k_L	Saturated hydraulic conductivity	15.25	m/d
d_{L}	Leakage parameter	9.03	-

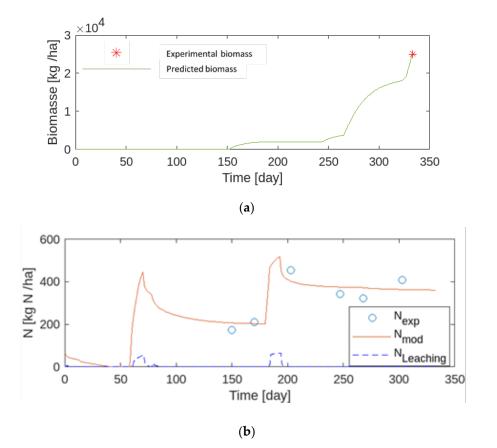
Figure 10 shows the results of the model compared to the data used. The results show a good602fit of the model to the field data. In fact, the olive biomass production simulated by the model603is quite similar to the field production. In addition, the soil nitrogen content determined in the604laboratory is very close to the model results.605



601

607





609

Figure 10. (a) Time series of olive's biomass production (Green solid line represent the modelled biomass and star610point represent the experimental amount of biomass obtained at the harvesting time); (b) Time series mineral ni-611trogen content in the soil (circular markers is the measured nitrogen; solid line represents the modeled nitrogen612content in the soil; dashed line represents the amount of nitrogen leached)613

614

615

The model is also applied to simulate soil moisture. Namely, this parameter is estimated based 617 on water inputs from rainfall and irrigation, and losses from evaporation, transpiration, and 618 deep percolation. The variation of soil humidity over time is illustrated in Figure 11. Due to 619 the increase of drought period and rainfall deficit, the selected farmer applied two intensive 620 rounds of irrigation with 350 m3 of TWW per day per hectare: 12 days for the first round and 621 13 days for the second one. According to the simulation results, the volumes brought by each 622 irrigation overflow the soil and may induce to deep percolation of water. Soil evaporation and 623 crop transpiration simulated by the model are shown in Figure 12.b. In this context, data on 624 the reference evapotranspiration ET0 and the radiation interception efficiency of olive crop 625 (that is the total ϕ (*t*)) and the one specific to olive production $\phi_{olive}(t)$) are required (cf. 626 Figure 12.a). However, the soil humidity being simulated by the model was not compared 627 with real values due to the lack of experimental data. This is the subject of future work, where 628 we will intend to s soil moisture sensors in the irrigated area of Msaken to improve the model 629 calibration following the procedure proposed in [55]. 630

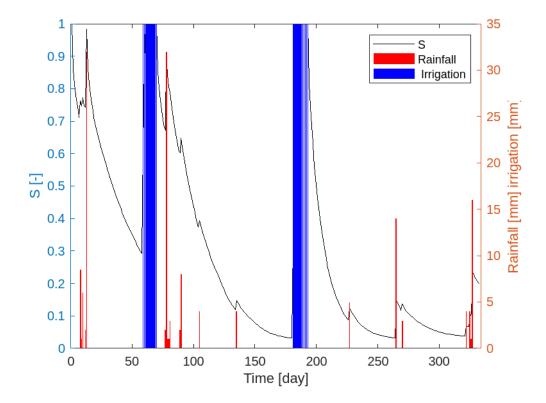


Figure 11. Soil humidity (black color), Rain (red color) and irrigation (blue color) over the olive farming season

633

632

631

634

635

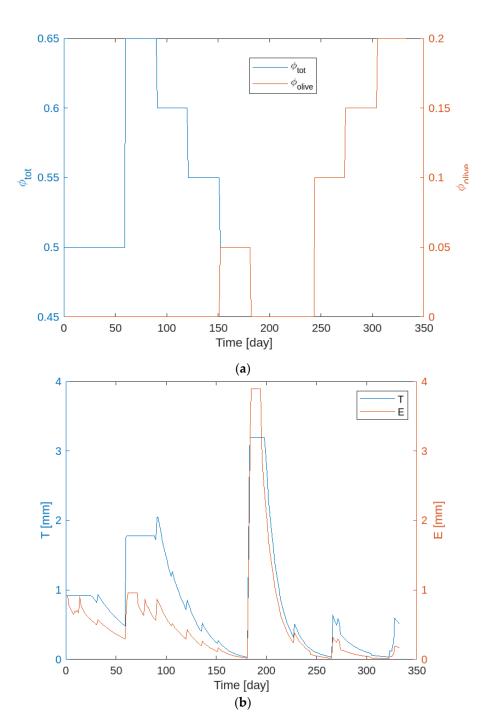


Figure 12. (a) Olive crop and olive radiation interception efficiency over time ; (b) Time series of transpiration and evaporation of olive crop

3.4.3 Soil Nitrogen content simulation

The nitrogen content of the soil was also increased by fertigation (cf. Figure 10.b). The treated wastewater 643 used for irrigation is rich in mineral nitrogen. In fact, water analysis shows that the average concentration 644 of mineral nitrogen is about 0.2 kg N/ha. Over-irrigation with TWW leads to nitrogen leaching, especially 645 when the nitrogen concentration in the TWW exceeds the uptake capacity of olive trees. The amount of 646 mineral nitrogen uptake of very productive olive trees in a year is estimated to be 60 -70 kg/ha [56]. 647

639 640

- 641
- 642

659

However, simulation results show that the total amount of nitrogen leached into the soil during an agricultural year is estimated at 1209 kg N/ha/year, which may be a source of soil and groundwater pollution.
Efficient and sustainable management of nitrogen in wastewater is very complex. The use of TWW can
be considered as a "natural" fertilizer source which may provide specific elements necessary for plant
growth, without excess or deficits. In addition, the use of treated wastewater for irrigation should always
consider the evaluation of environmental risks versus the benefits of nitrogen for crop growth.

3.4.4 Sensitivity analysis results

From 100 iterations, the results shown in figure 13 reveal that the biomass is sensitive to the normalized 655 daily water productivity (W*). However, the nitrogen response is sensitive to both parameters of the 656 nitrogen leaching function (d_L and k_L). On the other hand, a perturbation of the initial soil N concentration of the plant N uptake limit does not affect the model output. 658

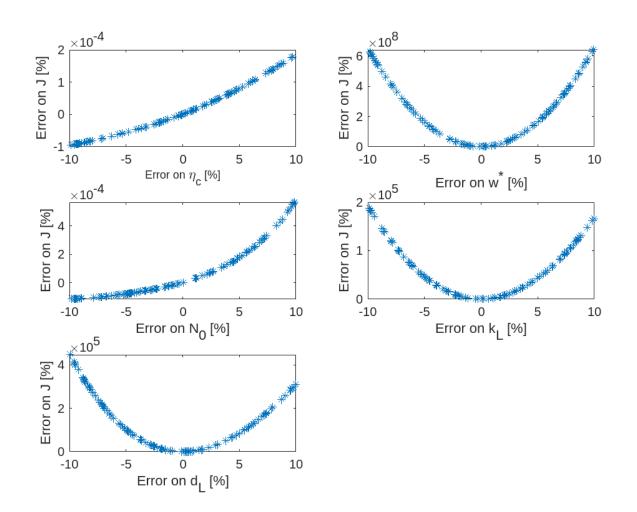


Figure 13. Sensitivity analysis. The deviation of the *sum of squared errors J of the calibrated model* based on 100 iterations for different biased values of parameters of the model

- ...
- 663
- 664 665

3.4.4 Viability analysis

For the analysis of viability, we found that nitrogen stress is always largely overcome by water stress, 667 which is then the only limiting factor for biomass production. Figure 14 shows the domain K of maximum 668 biomass production in grey and two boundaries: the red boundary for nitrogen stress and the blue for 669 hydric stress. The finding indicates that the magenta curve representing the separation between the hydric 670 and nitrogen stresses, does not belong to the domain K. Therefore, any trajectory of the system depicted in 671 the (S,N) plane that starts in the domain K will only touch the S=S* boundary of the hydric stress and never 672 the S/N= η c boundary of the nitrogen stress. Moreover, due to the fertigation, we can observe that the 673 trajectory which remains on the S=S* boundary goes upward. This means that the amount of nitrogen in-674 creases with irrigation, which implies that irrigation with TWW can stay away from the nitrogen stress. 675 This result is corrobored by Fernández-Escobar et al., [57] 676

> nitrogen (N) 0.45 0.5 0.55 0.6 0.65 0.7 0.75 0.8 0.85 0.9 0.95

Figure 14. Result of the Viability analysis: Viable trajectories may only touch the water stress boundary (blue)

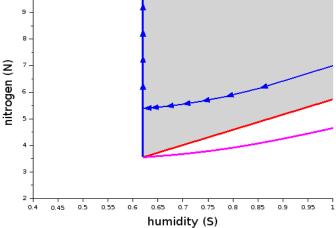
683 684 685

686 687

From the humidity and nitrogen assessment, we deduced that only the hydric stress needs attention 688 and we should adopt the minimum irrigation strategy to remain in the domain K. It consists in two 689 successive phases: 690

- Phase 1 : No irrigation until the trajectory touches (or is very close) the boundary of the do- \checkmark 691 main S=S* 692
- √ Phase 2 : Minimum irrigation strategy to keep the trajectory on the blue boundary S=S*, which 693 is determined such that $\frac{dS}{dt} = 0$ with S=S*. 694

In order to suggest some recommendations for local farmers, we developed the Figure 15, which 695 presents the strategy at the initial condition S0=1 and N0=57.1 kgN/ha. These theoretical trajectories 696



shown in Figure 15 are determined without rain precipitations and for the chronicle of the function 697 (.) that has been identified previously (and that we assume to be representative of the usual climate 698 for the considered farm), and serve as reference values. From this simulation, the theoretical recommended values for irrigation were the maximum flow rate Imax = 5.77 m3/day/ha and the total water 700 required per year V_{tot} = 1240 m3/ha. These values intend to help practitioners for designing the 701 irrigation system (maximum flow rate Imax) and determining the total quantity of water for the 702 season (V_{tot}). 703

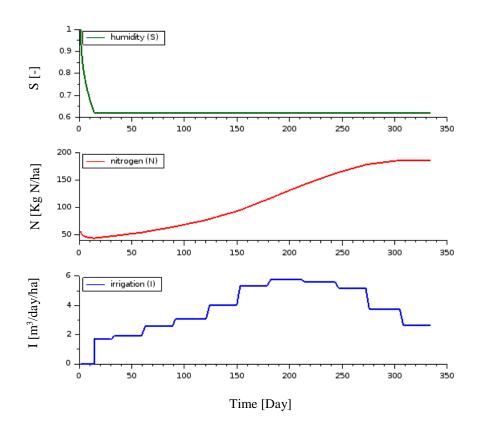


Figure 15. Simulation of the viable trajectory with the minimal irrigation strategy

4. Conclusions

Wastewater reuse is a sustainable solution for water resource management to cope 732 with water scarcity. In addition, treated wastewater is also considered as a fertilizer source 733 that can provide necessary inputs for plant growth. This study investigated local 734 farmers' perceptions of the use of treated wastewater in agriculture in irrigated perimeter 735 of Msaken. We also applied a crop model and mathematical simulations to identify 736 optimal and safe conditions for wastewater reuse. 737

Results related to the reuse value chain show that the quality of TWW is suitable for 738 irrigation and does not have a risk to human health. However, local farmers only focus on 739 supplemental irrigation to ensure the olive production. Moreorer, the viability analysis 740 indicates that nitrogen is not a limiting factor for olive production in the Msaken irrigated 741

704 705

706

707

708

709

710

711

712

713

714

715 716

717

718

719

720

721 722

723

724

725 726

727

728 729

area. In addition, in this study, we have identified a theoretical minimum irrigation scheme742that could guarantee maximum olive production, taking into account soil and water reuse743characteristics. We found that maximum irrigation is 5.77 m³/day/ha and the total water744required per year is 1240 m³/ha.745

Further viability analysis can be elaborated in the future studies to investigate the 746 minimal total quantity of water or total supplied nitrogen to ensure a given biomass 747 production and to consider phosporus needs. 748

The next step of the research is to calculate in real conditions optimal trajectories that 749 maximize olive production (both in terms of water and nutrient content), taking into account weather effects. It could even be interesting to intervene in the reuse chain (water 751 treatment system) and act at that level to irrigate olive trees with optimal quality water. 752 In other words, it would be possible to treat water so that it exactly meets the needs of 753 olive trees. 754

Finally, this study could be improved with additional experimental data. For example, the use of appropriate sensors could provide more accurate estimation of soil moisture and thus, model calibration and prediction. 757

Author Contributions : Conceptualization, M.K., N.K., A.R. and J.H.; methodology, M.K., N.K. and760A.R. ; validation, M.K., N.K. and A.R. ; formal analysis, M.K., N.K. and A.R., investigation, M.K., N.K.761and H.G.; data curation, M.K. and N.K.; writing—original draft preparation, M.K., N.K. and A.R. ;762writing—review and editing, M.K., N.K., A.R., J.H. and H.G. ; project administration, A.R., M.K. and763J.H. funding acquisition, A.R., M.K. and J.H. All authors have read and agreed to the published version764of the manuscript.765

Funding: This research was supported by Agropolis Foundation, Montpellier, France through the pro-766ject "Integrated VAlorization of liquid and solid WASTE "IVA-WASTE".767

Data Availability Statement: Some data used in this study are available on request from the768corresponding author.769

Acknowledgments: Special thanks to the staff of Commissariat Régional au Développement Agricole 770 (CRDA) of Sousse and Office National de l'Assainissement (ONAS) of Sousse for their cooperation 771 during the field survey and data. The authors are grateful to the local user association (GDA) and 772 farmers for their help during the data collection phase. Special thanks to the IWA-WASTE team in-773 volved in the project. The authors also thank the ICIREWARD International UNESCO Center on Water 774 of Montpellier and the TREASURE international research network (www6.inrae.fr/treasure) for their 775 financial supports. This work has been achived in the framework of the I-Site MUSE, Montpellier Uni-776 versité d'Excellence (ANR 16-IDEX-0006). 777

Conflicts of Interest: Declare conflicts of interest or state "The authors declare no conflict of interest." 778

779

758 759

References

781

27 of 29

782 783 784

785

786

787

788

789

790

791

792

793

794

795

796

800

801

802

803

804

805

806

807

808

817

818

819

820

821

822

823

824

825

826

827

828

829

- 1. Miller, J.D. ; Hutchin, M. The impacts of urbanisation and climate change on urban flooding and urban water quality: A review of the evidence concerning the United Kingdom, J. Hydrol. Reg. Stud. 2017, 12, 345-362 https://doi.org/10.1016/j.ejrh.2017.06.006
- 2. Cullis, J.D. S. ; Horn, A.; Rossouw, N.; Fisher-Jeffes, L.; Kunneke M. M.; Hoffman W. Urbanisation, climate change and its impact on water quality and economic risks in a water scarce and rapidly urbanising catchment: case study of the Berg River Catchment. H2Open J. 2019, 2 (1): 146–167. https://doi.org/10.2166/h2oj.2019.027
- 3. UN-Water, Summary Progress Update 2021: SDG 6 Water and Sanitation for All | UN-Water Available online: https://www.unwater.org/publications/summary-progress-update-2021-sdg-6-water-and-sanitation-all (accessed on 26 December 2022).
- 4. UN-Water, SDG 6 Synthesis Report 2018 on Water and Sanitation | UN-Water Available online: https://www.un-water.org/publications/sdg-6-synthesis-report-2018-water-and-sanitation (accessed on 26 December 2022).
- 5. UN, United Nations. Transforming our world: the 2030 Agenda for Sustainable Development. Resolution adopted by the General Assembly on 25 September 2015, A/RES/70/1
- 6. Helmecke, M.; Fries, E.; Schulte, C. Regulating Water Reuse for Agricultural Irrigation: Risks Related to Organic Micro-Contaminants. Environ. Sci. Eur. 2020, 32, doi:10.1186/S12302-019-0283-0.
- Ait-Mouheb, N.; Bahri, A.; Thayer, B.; Benyahia, B.; Bourrié, G.; Cherki, B.; Condom, N.; Declercq, R.; Gunes, A.; Héran, M.; et al. The Reuse of Reclaimed Water for Irrigation around the Mediterranean Rim: A Step towards a More Virtuous Cycle? Reg. Environ. Change 2018, 18, 693–705, doi:10.1007/s10113-018-1292-z.
- 8. The United Nations World Water Development Report 2018: Nature-Based Solutions for Water. UNESCO 2018, 1– 139.
- 9. Van Rensburg, P. Overcoming Global Water Reuse Barriers: The Windhoek Experience. Int J Water Resour Dev 2016, 32, 622–636, doi:10.1080/07900627.2015.1129319.
- 10. BPEH, Bureau de la Planification et des Equilibres Hydrauliques, 2020. Rapport National du Secteur de l'Eau de 2020. Ministère de l'Agriculture, des Ressources Hydrauliques et de la Pêche.
- 11. African Water Facility, 2016. Elaboration de la vision et de la stratégie du Secteur de l'Eau à l'horizon 2050 pour la Tunisie «Eau 2050», Rapport d'evaluation. African Development Bank Group,
- STUDI International/ GKW, 2020. Elaboration de la vision et de la stratégie du secteur de l'eau à l'horizon 2050
 pour la Tunisie, EAU 2050. Etape 3: Réalisation des Etudes Prospectives Multithématiques et Etablissement de
 Modèles Prévisionnels Offre-Demande (Bilans), Volume I: Réalisation des Etudes Prospectives Multithématiques,
 Version provisoire, Ministère de l'Agriculture, des Ressources Hydrauliques et de la Pêche Maritime Bureau de la
 Planification et des Equilibres Hydrauliques, République Tunisienne, KFW, GIZ
- BRL Ingenierie, Baastel, ONF International, 2022. Elaboration du Plan Directeur National de Réutilisation des Eaux
 Usées Traitées en Tunisie WATER REUSE 2050, Phase 2 Prospective de la filière à l'horizon 2050. Ministère de
 l'Agriculture, des Ressources Hydrauliques et de la Pêche, DG/GREE, AFD
- 14. Bahri, A. Water reuse in Tunisia: stakes and prospects. In Atelier du PCSI (Programme Commun Systèmes Irrigués) sur une Maîtrise des Impacts Environnementaux de l'Irrigation (pp. 11-p). Cirad-IRD-Cemagref 2001.
- 15. ONAS (Office National de l'Assainissement) Annual Report 2019, Tunisia, 2019.
- 16. Voulvoulis, N. Water Reuse from a Circular Economy Perspective and Potential Risks from an Unregulated Approach. Curr Opin Environ Sci Health 2018, 2, 32–45, doi:10.1016/J.COESH.2018.01.005.
- 17. Rajasulochana, P.; Preethy, V. Comparison on Efficiency of Various Techniques in Treatment of Waste and Sewage Water–A Comprehensive Review. Resour.-Effic. Technol. 2016, 2, 175–184.
- Kesari, K.K.; Soni, R.; Jamal, Q.M.S.; Tripathi, P.; Lal, J.A.; Jha, N.K.; Siddiqui, M.H.; Kumar, P.; Tripathi, V.; Ruokolainen, J. Wastewater Treatment and Reuse: A Review of Its Applications and Health Implications. Water Air Soil Pollut 2021, 232, doi:10.1007/S11270-021-05154-8.
- Kalboussi, N.; Biard, Y.; Pradeleix, L.; Rapaport, A.; Sinfort, C.; Ait-mouheb, N. Life Cycle Assessment as Decision Support Tool for Water Reuse in Agriculture Irrigation. Sci. Total Environ. 2022, 836, 155486, doi:10.1016/J.SCI-TOTENV.2022.155486.
- Maquet, C. Wastewater reuse: a solution with a future. Field Actions Science Reports. The journal of field actions 830 2020, (Special Issue 22), 64-69.
 831
- 21. WHO Safe Use of Wastewater, Excreta and Greywater Guidelines for the Safe Use Of. World Health 2006, II, 204, 832
- Qadir, M.; Galibourg, D.; Drechsel, P.; Qadir, M.; Galibourg, D. The WHO Guidelines for Safe Wastewater Use in Agriculture: A Review of Implementation Challenges and Possible Solutions in the Global South. Water 2022, 14(6), 834
 844 doi:10.3390/w14060864.
- Steduto, P.; Hsiao, T.C.; Raes, D.; Fereres, E. AquaCrop—The FAO Crop Model to Simulate Yield Response to Water: I. Concepts and Underlying Principles. Agron. J. 2009, 101, 426–437, doi:10.2134/AGRONJ2008.01395.

797 798 799

- 24.
 Brisson, N.; Gary, C.; Justes, E.; Roche, R.; Mary, B.; Ripoche, D.; Zimmer, D.; Sierra, J.; Bertuzzi, P.; Burger, P. et
 838

 al. An Overview of the Crop Model STICS. Eur J Agron 2003, 18, 309-332, https://doi.org/10.1016/S1161 839

 0301(02)00110-7
 840
- Cheviron, B.; Vervoort, R.W.; Albasha, R.; Dairon, R.; le Priol, C.; Mailhol, J.C. Framework to Use Crop Models for Multi-Objective Constrained Optimization of Irrigation Strategies. Environ. Model. Softw. 2016, 86, 145-157, doi:10.1016/j.envsoft.2016.09.001
- 26. Lenz-Wiedemann, V.I.S.; Klar, C.W.; Schneider, K. Development and Test of a Crop Growth Model for Application 844 within a Global Change Decision Support System. Ecol. Modell. 2010, 221. 314-329. 845 doi:10.1016/j.ecolmodel.2009.10.014. 846
- 27. Klar, C.W.; Fiener, P.; Neuhaus, P.; Lenz-Wiedemann, V.I.S.; Schneider, K. Modelling of Soil Nitrogen Dynamics within the Decision Support System DANUBIA. Ecol. Modell. 2008, 217(1-2), 181-196.
- Haddon, A., Rapaport, A., Roux, S., Harmand, J. Multi-objective Dynamic Optimization of Crops Irrigated with Reused Treated Wastewater. SIMS EUROSIM 2021 conference on Modelling and Simulation, Finnish Society of Automation, Sep 2021, Helsinki,
- Pelak, N.; Revelli, R.; Porporato, A. A Dynamical Systems Framework for Crop Models: Toward Optimal Fertilization and Irrigation Strategies under Climatic Variability. Ecol. Modell. 2017, 365, 80–92, 853 doi:10.1016/j.ecolmodel.2017.10.003.
- 30. Kalboussi, N.; Roux, S.; Cheviron, B.; Harmand, J.; Rapaport, A.; Sinfort, C. Apport de La Modélisation Pour l'aide à La Décision En Vue de La Réutilisation Agricole Des Eaux Usées Traitées. Journal International Sciences et Techniques de l'Eau et de l'Environnement, 2018, 3 (1), 102-107
- 31. Kalboussi, N.; Roux, S.; Boumaza, K.; Sinfort, C.; Rapaport, A. About Modeling and Control Strategies for Scheduling Crop Irrigation. IFAC Workshop on Control Methods for Water Resource Systems - CMWRS2019, Sep 2019, Delft, Netherlands. Appeared in IFAC-PapersOnLine 2019, 52, 43–48, doi:10.1016/J.IFACOL.2019.11.
- 32. Boumaza, K.; Kalboussi, N.; Rapaport, A.; Roux, S.; Sinfort, C. Optimal control of a crop irrigation model under water scarcity. Optim. Control Appl. Methods 2021, 42 (6), 1612-1631, doi:10.1002/oca.2749
- CRDA (Commissariat Régional au Développement Agricole), S.; Department of Water resource. Annual Report ; 863 Sousse, 2021; 864
- 34.
 GEREP Environnement. Programme de Veille Environnementale de la phase "exploitation » du périmètre irrigué
 865

 par les Eaux Usées Traitées de Msaken, 2016. Ministère de l'Agriculture, des Ressources Hydrauliques et de la
 866

 pêche, Commissariat Régional de Développement Agricole (CRDA) de Sousse.
 867
- 35. UNIDO (United Nations Industrial Development Organization). Agro-value chain analysis and development: The UNIDO approach, 2009.
- 36. Chowell, G.; Hyman, J. M.; Bettencourt, L. M. A.; Castillo-Chavez, C. Mathematical and statistical estimation approaches in epidemiology. Springer Netherlands, 2009. doi: 10.1007/978-90-481-2313-1.
- Aubin, J.; Bayen, A.; Saint-Pierre, P. Viability Theory: New Directions. Springer Science & Business Media 2011, doi:10.1007/978-3-642-16684-6.
 873
- INNORPI. Protection de l'Environnement, Utilisation des Eaux Usées Traitées a des fins agricoles specifocations
 physico-chimiques et biologiques, NT 106:03, 1989
 875
- Pescod, M.B. Wastewater treatment and use in agriculture, 1992. FAO irrigation and drainage paper 47. Food and Agriculture Organization of the United Nations, Rome, Italy.
 877
- 40. Official Journal of the European Union, Regulation (EU) 2020/741 of the European Parliament and of the Council 878 on minimum requirements for water reuse. L 177/32 5.6.2020 879
- 41. EPA, United States Environmental Protection Agency. Method 410.3: Chemical Oxygen Demand (Titrimetric, High Level for Saline Waters) by Titration, Editorial Revision 1978
- 42. Delzer, G.C.; McKenzie, S.W. Five-Day Biochemical Oxygen Demand, 2003. USGS TWRI Book 9–A7 (Third Edition)
- 43. Rhee, K. C. Determination of Total Nitrogen. Curr. protoc. food anal. chem. 2001, 00(1), B1.2.1–B1.2.9.
- Greggio, N.; S Giambastiani, B.M.; Balugani, E.; Amaini, C.; Antonellini, M. High-Resolution Electrical Resistivity
 Tomography (ERT) to Characterize the Spatial Extension of Freshwater Lenses in a Salinized Coastal Aquifer. Water 2018, 10(8), 1067. doi:10.3390/w10081067.
- Hasan, M.; Shang, Y.; Jin, W. Delineation of Weathered/Fracture Zones for Aquifer Potential Using an Integrated 887 Geophysical Approach: A Case Study from South China. J. Appl Geophy. 2018, 157, 47–60, 888 doi:10.1016/J.JAPPGEO.2018.06.017.
- Hung, Y. C.; Chou, H. S.; Lin, C. P. Appraisal of the Spatial Resolution of 2D Electrical Resistivity Tomography for
 Geotechnical Investigation. Appl. Sci. 2020, 10(12), 4394.
 891
- Melgar, J.C.; Mohamed, Y.; Serrano, N.; García-Galavís, P.A.; Navarro C.; Parra M.A.; Benlloch M.; Fernández-Escobar R.; Long Term Responses of Olive Trees to Salinity. Agric. Water Manag. 2009, 96(7), 1105-1113., 893 doi:10.1016/j.agwat.2009.02.009.
- Fichtner, E.J.; Lovatt, C.J. Alternate Bearing in Olive. Acta Hortic 2018, 1199, 103–108, doi:10.17660/ACTA-895 HORTIC.2018.1199.17.Ben Ahmed, C.; ben Rouina, B.; Boukhris, M. Effects of Water Deficit on Olive Trees Cv. 896

848

855

856

857

858

859

860

861

862

868

869

870

871

880

881

882

	Chemlali under Field Conditions in Arid Region in Tunisia. Sci Hortic 2007, 113, 267–277, doi:10.1016/J.SCI-	897 808
10	ENTA.2007.03.020.	898
49.	Rodríguez-Eugenio, N.; McLaughlin, M.; Pennock, D. Soil Pollution: A Hidden Reality. FAO 2018.	899
50.	Tilman, D.; Cassman, K.G.; Matson, P.A.; Naylor, R.; Polasky, S. Agricultural Sustainability and Intensive Produc-	900
	tion Practices. Nature 2002, 418, 671–677, doi:10.1038/NATURE01014.	901
51.	Saliu, T.D.; Oladoja, N.A. Nutrient Recovery from Wastewater and Reuse in Agriculture: A Review. Environ Chem	902
	Lett 2021, 19, 2299–2316, doi:10.1007/S10311-020-01159-7.	903
52.	Hidri, Y.; Hibar, K.; Bchir, A.; Werheni, R.; Jedidi, N.; Hassen, A. Changes in the Microbial Properties of Olive	904
	Cultivated Soils under Short, Medium and Long-Term Irrigation with Treated Wastewater. Asian J. Soil Sci. 2021,	905
	5, 1–20, doi:10.9734/ASRJ/2021/v5i130097.	906
53.	Carpenter, S.R.; Caraco, N.F.; Correll, D.L.; Howarth, R.W.; Sharpley, A.N.; Smith, V.H. Nonpoint Pollution of	907
	Surface Waters with Phosphorus and Nitrogen. Ecol. Appl. 1998, 8, 559-568, doi:10.1890/1051-	908
	0761(1998)008[0559:NPOSWW]2.0.CO;2.	909
54.	Haddon, A.; Kechichian, L.; Harmand, J.; Dejean, C. Linking Soil Moisture Sensors and Crop Models for Irrigation	910
	Management, 2022, https://hal.inrae.fr/hal-03909071 .	911
55.	Fertilisation - FRANCE OLIVE - AFIDOL Available online: https://afidol.org/oleiculteur/fertilisation/ (accessed on	912
	27 December 2022).	913
56.	Fernández-Escobar, R.; García-Novelo, J.M.; Molina-Soria, C.; Parra, M.A. An approach to nitrogen balance in	914
	olive orchards, Sci. Hortic., 2012, 135, 219-226,	915
		916
		917
		918
		919
		919