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High-dimensional variable selection in nonlinear mixed effects models using a stochastic EM spike-and-slab

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High-dimensional variable selection is widely documented in standard regression models, but there are still few tools to address it in nonlinear mixed-effects models, where data is collected repeatedly on several individuals. For all $1 \leq i \leq n$ and $1 \leq j \leq n_i$, y_{ij} the response of individual i at time t_{ij} is modelled as follows:

$$y_{ij} = g(\varphi_i, t_{ij}) + \varepsilon_{ij}, \quad \varepsilon_{ij} \stackrel{\text{i.i.d.}}{\sim} \mathcal{N}(0, \sigma^2),$$
$$\varphi_i = \mu + \boldsymbol{\beta}^\top V_i + \xi_i, \quad \xi_i \stackrel{\text{i.i.d.}}{\sim} \mathcal{N}_q(0, \Gamma),$$

where g is non-linear with respect to an individual parameter φ_i which is q -dimensional. Identifying the relevant covariates for all individual parameters amounts to selecting the support of $\boldsymbol{\beta} \in \mathcal{M}_{p \times q}$, defined by $S^* = \left\{ (\ell, m) \in \{1, \dots, p\} \times \{1, \dots, q\} \mid \beta_{\ell m}^* \neq 0 \right\}$, where $\boldsymbol{\beta}^*$ is the true fixed effects matrix, and p is the number of covariates. To solve this problem in a high-dimensional context, that is when $p \gg n$, the assumption of sparsity is made, that is each row of $\boldsymbol{\beta}^*$ is sparse. The main difficulty here is that variable selection concerns latent variables of the model.

In this work, variable selection is approached from a Bayesian perspective and a selection procedure is proposed, combining the use of a spike-and-slab prior [3] and the SAEM algorithm [2]. The first step of this procedure is to reduce the number of candidate models: similarly to Lasso regression, a grid of values for the spike parameter is explored to obtain a collection of promising sub-models $(\hat{S}_{\nu_0})_{\nu_0 \in \Delta}$. Then, an information criterion can be used to choose the final model: a pragmatic and effective choice is to use the eBIC (extended Bayesian Information Criterion, [1]) which is tailored to the high-dimensional setting.

This approach is much faster than a classical MCMC algorithm and shows very good selection performances on simulated data. The efficiency of the proposed method is illustrated on a problem of genetic markers identification, relevant for genomic assisted selection in plant breeding. The current aim is to achieve consistency in model selection for this problem, which is a work in progress.

References

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